

Delhi CET 2019 Question Paper With Solutions

Time Allowed :2 Hours	Maximum Marks :600	Total questions :150
-----------------------	--------------------	----------------------

General Instructions

Read the following instructions very carefully and strictly follow them:

1. **Mode of Examination:** Online (Computer Based exam)
2. **Number of Questions:** 150
3. **Type of Questions:** MCQ (Multiple Choice Questions)
4. **Duration:** 2 hours
5. **Negative Marking:** - 1 mark

1. The area of the triangle with vertices $(0, 0)$, $(6, 0)$, and $(0, 5)$ is:

- (1) 11 Square units
- (2) 12 Square units
- (3) 13 Square units
- (4) 15 Square units

Correct Answer: (4) 15 Square units

Solution:

Step 1: Identify the type of triangle.

The given vertices are $(0, 0)$, $(6, 0)$, and $(0, 5)$.

The vertex $(0, 0)$ is the origin.

The vertex $(6, 0)$ lies on the x-axis.

The vertex $(0, 5)$ lies on the y-axis.

Since two sides of the triangle lie along the x and y axes, this is a right-angled triangle.

Step 2: Determine the base and height of the triangle.

The length of the base can be calculated as the distance between $(0, 0)$ and $(6, 0)$ along the x-axis.

Base $(b) = 6 - 0 = 6$ units.

The height of the triangle can be calculated as the distance between $(0, 0)$ and $(0, 5)$ along the y-axis.

Height $(h) = 5 - 0 = 5$ units.

Step 3: Calculate the area of the triangle.

The formula for the area of a triangle is $\frac{1}{2} \times \text{base} \times \text{height}$.

$$\text{Area} = \frac{1}{2} \times b \times h$$

$$\text{Area} = \frac{1}{2} \times 6 \times 5$$

$$\text{Area} = \frac{1}{2} \times 30$$

$$\text{Area} = 15 \text{ Square units.}$$

Alternatively, using the determinant formula for the area of a triangle with vertices (x_1, y_1) , (x_2, y_2) , and (x_3, y_3) :

$\text{Area} = \frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)|$ Let $(x_1, y_1) = (0, 0)$, $(x_2, y_2) = (6, 0)$, and $(x_3, y_3) = (0, 5)$.

$$\text{Area} = \frac{1}{2} |0(0 - 5) + 6(5 - 0) + 0(0 - 0)|$$

$$\text{Area} = \frac{1}{2}|0 + 6(5) + 0|$$

$$\text{Area} = \frac{1}{2}|30|$$

$$\text{Area} = 15 \text{ Square units.}$$

Step 4: Compare with the given options.

The calculated area is 15 Square units, which matches option (4).

(4) 15 Square units

Quick Tip

For a triangle with one vertex at the origin $(0, 0)$ and the other two vertices on the axes (e.g., $(a, 0)$ and $(0, b)$), the area is simply $\frac{1}{2} \times |a| \times |b|$. This is a special case of a right-angled triangle.

2. The value of p for which the points $(-5, 1)$, $(1, p)$, and $(4, -2)$ are collinear is:

(1) 1

(2) -2

(3) -1

(4) 3

Correct Answer: (3) -1

Solution:

Step 1: Understand Collinearity Condition.

Three points (x_1, y_1) , (x_2, y_2) , and (x_3, y_3) are collinear if the area of the triangle formed by these points is zero. This can be expressed using the determinant condition:

$$\begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix} = 0.$$

Substituting the given points $(-5, 1)$, $(1, p)$, and $(4, -2)$ into the determinant:

$$\begin{vmatrix} -5 & 1 & 1 \\ 1 & p & 1 \\ 4 & -2 & 1 \end{vmatrix} = 0.$$

Step 2: Expand the Determinant.

Expanding along the first row:

$$\begin{vmatrix} -5 & 1 & 1 \\ 1 & p & 1 \\ 4 & -2 & 1 \end{vmatrix} = -5 \begin{vmatrix} p & 1 \\ -2 & 1 \end{vmatrix} - 1 \begin{vmatrix} 1 & 1 \\ 4 & 1 \end{vmatrix} + 1 \begin{vmatrix} 1 & p \\ 4 & -2 \end{vmatrix}.$$

Calculate each minor determinant:

$$\begin{aligned} 1. \quad & \begin{vmatrix} p & 1 \\ -2 & 1 \end{vmatrix} = p(1) - (-2)(1) = p + 2, \\ 2. \quad & \begin{vmatrix} 1 & 1 \\ 4 & 1 \end{vmatrix} = 1(1) - 4(1) = 1 - 4 = -3, \\ 3. \quad & \begin{vmatrix} 1 & p \\ 4 & -2 \end{vmatrix} = 1(-2) - 4(p) = -2 - 4p. \end{aligned}$$

Substitute back into the expanded determinant:

$$-5(p + 2) - 1(-3) + 1(-2 - 4p) = 0.$$

Simplify:

$$-5p - 10 + 3 - 2 - 4p = 0,$$

$$-5p - 4p - 10 + 3 - 2 = 0,$$

$$-9p - 9 = 0.$$

Solve for p :

$$-9p = 9 \implies p = -1.$$

Step 3: Analyze the Options.Option (1): 1 — Incorrect, as $p = -1$.Option (2): -2 — Incorrect, as $p = -1$.

Option (3): -1 — Correct, as this matches the calculated value.

Option (4): 3 — Incorrect, as $p = -1$.**Step 4: Final Answer.**

$$\mathbf{(3) -1}$$

Quick Tip

For three points to be collinear, the area of the triangle formed by them must be zero.
Use the determinant condition to set up an equation and solve for the unknown variable.
Always simplify step-by-step to avoid errors.

3. If $(1 + \cos A)(1 - \cos A) = \frac{3}{4}$, then the value of $\sec A$ is :

(1) 1

(2) 3

(3) 2

(4) 4

Correct Answer: (3) 2

Solution:

Step 1: Simplify the given expression using algebraic identities.

The given equation is $(1 + \cos A)(1 - \cos A) = \frac{3}{4}$.

This expression is in the form of $(a + b)(a - b)$, which simplifies to $a^2 - b^2$.

Here, $a = 1$ and $b = \cos A$.

So, $(1)^2 - (\cos A)^2 = \frac{3}{4}$

$1 - \cos^2 A = \frac{3}{4}$

Step 2: Use the fundamental trigonometric identity.

Recall the Pythagorean identity: $\sin^2 A + \cos^2 A = 1$.

From this identity, we can write $\sin^2 A = 1 - \cos^2 A$.

Substitute this into the simplified equation:

$\sin^2 A = \frac{3}{4}$

Step 3: Find the value of $\sin A$.

Taking the square root of both sides:

$\sin A = \pm \sqrt{\frac{3}{4}} = \pm \frac{\sqrt{3}}{2}$

Step 4: Find the value of $\cos A$.

We have $1 - \cos^2 A = \frac{3}{4}$.

Rearrange the equation to solve for $\cos^2 A$:

$\cos^2 A = 1 - \frac{3}{4}$

$$\cos^2 A = \frac{4-3}{4} = \frac{1}{4}$$

Taking the square root of both sides:

$$\cos A = \pm \sqrt{\frac{1}{4}} = \pm \frac{1}{2}$$

Step 5: Find the value of Sec A.

Recall that $\sec A = \frac{1}{\cos A}$.

Using the value of $\cos A$:

$$\sec A = \frac{1}{\pm \frac{1}{2}} = \pm 2$$

Step 6: Choose the appropriate value from the options.

The options provided are positive integers. Therefore, we consider the positive value of $\sec A$. $\sec A = 2$

(3) 2

Quick Tip

Remember the algebraic identity $(a + b)(a - b) = a^2 - b^2$ and the fundamental trigonometric identity $\sin^2 A + \cos^2 A = 1$. These are crucial for simplifying trigonometric expressions. Also, $\sec A$ is the reciprocal of $\cos A$.

4. If $\tan \theta + \frac{1}{\tan \theta} = 2$, then the value of $\tan^2 \theta + \frac{1}{\tan^2 \theta}$ is:

- (1) 2
- (2) 3
- (3) 4
- (4) 5

Correct Answer: (1) 2

Solution:

Step 1: Identify the given equation and the expression to be found.

Given equation: $\tan \theta + \frac{1}{\tan \theta} = 2$ Expression to find: $\tan^2 \theta + \frac{1}{\tan^2 \theta}$

Step 2: Use an algebraic identity to relate the given and required expressions.

This problem can be solved by squaring the given equation.

Let $x = \tan \theta$. Then the given equation is $x + \frac{1}{x} = 2$.

We need to find $x^2 + \frac{1}{x^2}$.

Recall the algebraic identity: $(a + b)^2 = a^2 + b^2 + 2ab$.

In our case, let $a = x$ and $b = \frac{1}{x}$.

So, $\left(x + \frac{1}{x}\right)^2 = x^2 + \left(\frac{1}{x}\right)^2 + 2(x)\left(\frac{1}{x}\right)$

$$\left(x + \frac{1}{x}\right)^2 = x^2 + \frac{1}{x^2} + 2$$

Step 3: Substitute the given value into the identity.

We know that $x + \frac{1}{x} = 2$.

Substitute this into the squared identity:

$$(2)^2 = x^2 + \frac{1}{x^2} + 2$$

$$4 = x^2 + \frac{1}{x^2} + 2$$

Step 4: Solve for the required expression.

Rearrange the equation to find $x^2 + \frac{1}{x^2}$:

$$x^2 + \frac{1}{x^2} = 4 - 2$$

$$x^2 + \frac{1}{x^2} = 2$$

Since $x = \tan\theta$, we have $\tan^2\theta + \frac{1}{\tan^2\theta} = 2$.

Alternative Method (Directly Solving for $\tan \theta$):

Step 1: Given $\tan\theta + \frac{1}{\tan\theta} = 2$.

Let $y = \tan\theta$.

$$y + \frac{1}{y} = 2$$

Multiply by y to clear the denominator:

$$y^2 + 1 = 2y$$

$$y^2 - 2y + 1 = 0$$

Step 2: Factor the quadratic equation.

This is a perfect square trinomial: $(y - 1)^2 = 0$.

So, $y - 1 = 0 \implies y = 1$.

Therefore, $\tan\theta = 1$.

Step 3: Substitute the value of $\tan\theta$ into the required expression.

$$\tan^2\theta + \frac{1}{\tan^2\theta} = (1)^2 + \frac{1}{(1)^2}$$

$$= 1 + \frac{1}{1}$$

$$= 1 + 1 = 2.$$

Both methods yield the same result.

Step 5: Final Answer.

The value of $\tan^2\theta + \frac{1}{\tan^2\theta}$ is 2.

(1) 2

Quick Tip

This type of problem often uses the algebraic identity

$$(a + b)^2 = a^2 + b^2 + 2ab.$$

Alternatively, for expressions like

$$x + \frac{1}{x} = k,$$

recognize that squaring both sides gives

$$x^2 + \frac{1}{x^2} = k^2 - 2.$$

For the specific case where

$$x + \frac{1}{x} = 2,$$

it implies

$$x = 1$$

(since

$$x^2 - 2x + 1 = 0 \implies (x - 1)^2 = 0).$$

5. $\sin 2A = 2 \sin A$ is true when A is equal to:

- (1) 0°
- (2) 30°
- (3) 45°
- (4) 60°

Correct Answer: (1) 0°

Solution:

Step 1: Use the Double-Angle Identity for Sine.

The double-angle identity for sine states:

$$\sin 2A = 2 \sin A \cos A.$$

Thus, the given equation becomes:

$$2 \sin A \cos A = 2 \sin A.$$

Step 2: Simplify the Equation.

Rearrange the equation:

$$2 \sin A \cos A - 2 \sin A = 0.$$

Factor out $2 \sin A$:

$$2 \sin A (\cos A - 1) = 0.$$

Step 3: Solve for A .

Set each factor equal to zero:

1. $2 \sin A = 0$:

$$\sin A = 0 \implies A = 0^\circ, 180^\circ, 360^\circ, \dots$$

The simplest solution within the standard range is $A = 0^\circ$.

2. $\cos A - 1 = 0$:

$$\cos A = 1 \implies A = 0^\circ, 360^\circ, \dots$$

Again, the simplest solution is $A = 0^\circ$.

Step 4: Analyze the Options.

Option (1): 0° — Correct, as it satisfies the equation.

Option (2): 30° — Incorrect, as substituting $A = 30^\circ$ does not satisfy the equation.

Option (3): 45° — Incorrect, as substituting $A = 45^\circ$ does not satisfy the equation.

Option (4): 60° — Incorrect, as substituting $A = 60^\circ$ does not satisfy the equation.

Step 5: Final Answer.

(1) 0°

Quick Tip

When solving trigonometric equations involving double-angle identities, always simplify using basic trigonometric formulas and consider all possible solutions within the given range. Factorization can help identify key angles that satisfy the equation.

6. If $\sec(7^\circ - 2\alpha) = \csc(5\alpha - 7^\circ)$, then the value of α is:

- (1) 60°
- (2) 50°
- (3) 40°
- (4) 30°

Correct Answer: (4) 30°

Solution:

Step 1: Use the Relationship Between Secant and Cosecant.

Recall that:

$$\sec \theta = \csc(90^\circ - \theta)$$

Thus, the given equation:

$$\sec(7^\circ - 2\alpha) = \csc(5\alpha - 7^\circ)$$

can be rewritten using the relationship above:

$$\csc(90^\circ - (7^\circ - 2\alpha)) = \csc(5\alpha - 7^\circ)$$

Step 2: Simplify the Argument of the Cosecant Function.

Simplify $90^\circ - (7^\circ - 2\alpha)$:

$$90^\circ - (7^\circ - 2\alpha) = 90^\circ - 7^\circ + 2\alpha = 83^\circ + 2\alpha$$

Thus, the equation becomes:

$$\csc(83^\circ + 2\alpha) = \csc(5\alpha - 7^\circ)$$

Step 3: Equate the Arguments.

For the cosecant functions to be equal, their arguments must differ by integer multiples of 360° , or be directly equal. We assume:

$$83^\circ + 2\alpha = 5\alpha - 7^\circ$$

Step 4: Solve for α .

Rearranging the equation:

Start with the equation:

$$83^\circ + 2\alpha = 5\alpha - 7^\circ$$

Move all terms to one side:

$$83^\circ + 2\alpha - 5\alpha + 7^\circ = 0$$

Combine like terms:

$$(83^\circ + 7^\circ) - 3\alpha = 0$$

$$90^\circ = 3\alpha$$

Now solve for α :

$$\alpha = \frac{90^\circ}{3} = 30^\circ$$

Step 5: Analyze the Options.

Option (1): 60° — Incorrect

Option (2): 50° — Incorrect

Option (3): 40° — Incorrect

Option (4): 30° — Correct

Step 6: Final Answer.

(4) 30°

Quick Tip

When dealing with trigonometric equations involving secant and cosecant, use the complementary angle relationships to simplify the problem. Equating the arguments of trigonometric functions often leads to straightforward algebraic solutions.

7. The angle of elevation of a 15 m high tower from a point 15 m away from its foot is:

(1) 30°

(2) 45°

(3) 60°

(4) 90°

Correct Answer: (2) 45°

Solution:

Step 1: Visualize the problem as a right-angled triangle.

Let the tower be represented by the vertical side (opposite side) of a right-angled triangle, and the distance from the foot of the tower to the observation point be the horizontal side (adjacent side). The angle of elevation is the angle between the horizontal line and the line of sight to the top of the tower.

Step 2: Identify the given values.

Height of the tower (Opposite side) = 15 m

Distance from the foot of the tower (Adjacent side) = 15 m

Step 3: Choose the appropriate trigonometric ratio.

We have the opposite side and the adjacent side, so the tangent function is suitable:

$$\tan(\text{angle of elevation}) = \frac{\text{Opposite}}{\text{Adjacent}}$$

Step 4: Substitute the given values and solve for the angle.

Let the angle of elevation be θ .

$$\tan \theta = \frac{15 \text{ m}}{15 \text{ m}}$$

$$\tan \theta = 1$$

We know that $\tan(45^\circ) = 1$.

Therefore, $\theta = 45^\circ$.

Step 5: Final Answer. The angle of elevation of the tower is 45° .

(2) 45°

Quick Tip

When the height of an object and the horizontal distance from its base are equal, the angle of elevation to its top will always be 45° , because $\tan 45^\circ = 1$. This creates an isosceles right-angled triangle.

8. If the angle of elevation of the top of a tower from a point on the ground, which is 30 m away from the foot of the tower is 30° , then the height of the tower is :

- (1) $9\sqrt{3}$ m
- (2) $10\sqrt{3}$ m
- (3) $11\sqrt{3}$ m
- (4) $13\sqrt{3}$ m

Correct Answer: (2) $10\sqrt{3}$ m

Solution:

Step 1: Visualize the problem as a right-angled triangle.

Let the tower be represented by the vertical side (opposite side), and the distance from the foot of the tower to the observation point be the horizontal side (adjacent side). The angle of elevation is given.

Step 2: Identify the given values.

Angle of elevation (θ) = 30°

Distance from the foot of the tower (Adjacent side) = 30 m

Let the height of the tower be h (Opposite side).

Step 3: Choose the appropriate trigonometric ratio.

We have the angle, the adjacent side, and we need to find the opposite side. The tangent function relates these:

$$\tan \theta = \frac{\text{Opposite}}{\text{Adjacent}}$$

Step 4: Substitute the given values and solve for the height.

$$\tan 30^\circ = \frac{h}{30}$$

Recall that $\tan 30^\circ = \frac{1}{\sqrt{3}}$, so:

$$\frac{1}{\sqrt{3}} = \frac{h}{30}$$

Now, solve for h :

$$h = \frac{30}{\sqrt{3}}$$

To rationalize the denominator, multiply numerator and denominator by $\sqrt{3}$:

$$h = \frac{30}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{30\sqrt{3}}{3}$$

$$h = 10\sqrt{3} \text{ m}$$

Step 5: Final Answer.

The height of the tower is $10\sqrt{3}$ m.

$$(2) 10\sqrt{3} \text{ m}$$

Quick Tip

Remember the standard trigonometric values for common angles like 30° , 45° , 60° . For 30° , $\tan 30^\circ = \frac{1}{\sqrt{3}}$. Always rationalize the denominator if your answer is in the form of a fraction with a radical in the denominator.

9. A tangent PQ at a point P of a circle of radius 5 cm meets a line through the centre O at a point Q So that OQ=12 cm, height PQ is :

- (1) 12 cm
- (2) 13 cm
- (3) 8.5 cm
- (4) $\sqrt{119}$ cm

Correct Answer: (4) $\sqrt{119}$ cm

Solution:

Step 1: Visualize the geometry and identify key properties.

We have a circle with center O.

P is a point on the circle, so OP is the radius. The radius of the circle (OP) is given as 5 cm.

PQ is a tangent to the circle at point P.

A line passes through the center O and meets the tangent at point Q. The distance OQ is given as 12 cm.

Step 2: Apply the theorem related to tangents and radii.

A fundamental property of circles is that the tangent at any point of a circle is perpendicular to the radius through the point of contact.

Therefore, the angle $\angle OPQ$ is a right angle (90°).

This means that triangle $\triangle OPQ$ is a right-angled triangle, with OQ as the hypotenuse.

Step 3: Use the Pythagorean theorem to find the length of PQ.

In a right-angled triangle $\triangle OPQ$, according to the Pythagorean theorem:

$$OP^2 + PQ^2 = OQ^2$$

We are given:

$$OP = 5 \text{ cm}$$

$$OQ = 12 \text{ cm}$$

Substitute the known values into the equation:

$$5^2 + PQ^2 = 12^2$$

$$25 + PQ^2 = 144$$

Now, solve for PQ^2 :

$$PQ^2 = 144 - 25$$

$$PQ^2 = 119$$

Finally, find PQ:

$$PQ = \sqrt{119} \text{ cm}$$

Step 4: Compare the result with the given options.

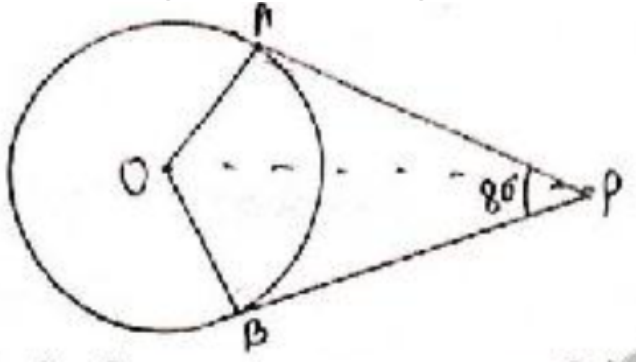
The calculated length of PQ is $\sqrt{119}$ cm, which matches option (4).

(4) $\sqrt{119}$ cm

Quick Tip

Remember that the radius drawn to the point of tangency is always perpendicular to the tangent line. This creates a right-angled triangle, allowing the use of the Pythagorean theorem to solve for unknown lengths.

10. If tangents PA and PB from a point P to a circle with centre O are inclined to each other at angle of 80° in the fig, then $\angle POA$ is equal to :



- (1) 50°
- (2) 60°
- (3) 70°
- (4) 80°

Correct Answer: (1) 50°

Solution:

Step 1: Analyze the given information and properties of tangents to a circle.

PA and PB are tangents from an external point P to a circle with center O.

The angle between the tangents, $\angle APB$, is given as 80° . We need to find $\angle POA$.

Key properties of tangents from an external point:

The lengths of tangents from an external point to a circle are equal ($PA = PB$).

The line segment from the center to the external point (OP) bisects the angle between the tangents ($\angle APB$).

The radius drawn to the point of tangency is perpendicular to the tangent ($OA \perp PA$ and $OB \perp PB$). This means $\angle OAP = \angle OBP = 90^\circ$.

Step 2: Use the property that OP bisects $\angle APB$.

Since OP bisects $\angle APB$, we have:

$$\angle OPA = \frac{1}{2} \angle APB$$

$$\angle OPA = \frac{1}{2} \times 80^\circ$$

$$\angle OPA = 40^\circ$$

Step 3: Consider triangle $\triangle OAP$.

We know that $\triangle OAP$ is a right-angled triangle because $\angle OAP = 90^\circ$ (radius is perpendicular to the tangent at the point of contact).

The sum of angles in a triangle is 180° . So, in $\triangle OAP$: $\angle OAP + \angle OPA + \angle POA = 180^\circ$

Substitute the known angle values:

$$90^\circ + 40^\circ + \angle POA = 180^\circ$$

$$130^\circ + \angle POA = 180^\circ$$

Step 4: Solve for $\angle POA$.

$$\angle POA = 180^\circ - 130^\circ$$

$$\angle POA = 50^\circ$$

Alternatively, consider quadrilateral OAPB:

The sum of angles in a quadrilateral is 360° .

$$\angle OAP + \angle APB + \angle PBO + \angle BOA = 360^\circ$$

$$90^\circ + 80^\circ + 90^\circ + \angle BOA = 360^\circ$$

$$260^\circ + \angle BOA = 360^\circ$$

$$\angle BOA = 360^\circ - 260^\circ = 100^\circ$$

Since $\triangle OAP \cong \triangle OBP$ (RHS congruence criterion, as $OA=OB$ (radii), $OP=OP$ (common), $\angle OAP = \angle OBP = 90^\circ$), OP also bisects $\angle AOB$.

Therefore, $\angle POA = \frac{1}{2}\angle BOA = \frac{1}{2} \times 100^\circ = 50^\circ$.

Step 5: Compare with the given options.

The calculated angle $\angle POA$ is 50° , which matches option (1).

(1) 50°

Quick Tip

When two tangents are drawn from an external point to a circle, the line joining the center to that external point bisects both the angle between the tangents and the angle subtended by the chord of contact at the center. Also, the radius is perpendicular to the tangent at the point of contact.

11. To draw a pair of tangents to a circle which are inclined to each other at an angle of

50° , it is required to draw tangents at end points of those two radii of the circle. What should be the angle between these two radii?

- (1) 150°
- (2) 140°
- (3) 130°
- (4) 120°

Correct Answer: (3) 130°

Solution:

Step 1: Understand the Geometry of Tangents and Radii.

When two tangents are drawn to a circle from an external point, the angle between the tangents is related to the angle between the radii drawn to the points of tangency. The relationship is given by:

$$\text{Angle between tangents} = 180^\circ - \text{Angle between radii}.$$

Step 2: Apply the Relationship.

Given that the angle between the tangents is 50° , we can use the formula:

$$\text{Angle between radii} = 180^\circ - \text{Angle between tangents}.$$

Substitute the given angle:

$$\text{Angle between radii} = 180^\circ - 50^\circ = 130^\circ.$$

Step 3: Analyze the Options.

Option (1): 150° — Incorrect, as this does not match the calculated value.

Option (2): 140° — Incorrect, as this does not match the calculated value.

Option (3): 130° — Correct, as it matches the calculated value.

Option (4): 120° — Incorrect, as this does not match the calculated value.

Step 4: Final Answer.

(3) 130°

Quick Tip

The angle between the tangents drawn to a circle from an external point is supplementary to the angle between the radii drawn to the points of tangency. Use the relationship $\text{Angle between tangents} = 180^\circ - \text{Angle between radii}$ to solve such problems.

12. If the perimeter of a circle is equal to that of a square, then find the ratio of their areas.

(1) 11 : 14

(2) 5 : 6

(3) 14 : 11

(4) 7 : 8

Correct Answer: (3) 14 : 11

Solution:

Step 1: Define Variables and Equations.

Let the radius of the circle be r and the side length of the square be s .

Perimeter of the circle: $2\pi r$.

Perimeter of the square: $4s$.

Given that the perimeters are equal:

$$2\pi r = 4s.$$

Solve for s in terms of r :

$$s = \frac{\pi r}{2}.$$

Step 2: Calculate the Areas.

Area of the circle: πr^2 .

Area of the square:

$$s^2 = \left(\frac{\pi r}{2}\right)^2 = \frac{\pi^2 r^2}{4}.$$

Step 3: Find the Ratio of Areas.

The ratio of the area of the circle to the area of the square is:

$$\text{Ratio} = \frac{\text{Area of circle}}{\text{Area of square}} = \frac{\pi r^2}{\frac{\pi^2 r^2}{4}} = \frac{\pi r^2 \cdot 4}{\pi^2 r^2} = \frac{4}{\pi}.$$

To express this ratio in terms of integers, approximate $\pi \approx \frac{22}{7}$:

$$\frac{4}{\pi} \approx \frac{4}{\frac{22}{7}} = \frac{4 \times 7}{22} = \frac{28}{22} = \frac{14}{11}.$$

Thus, the ratio of the areas is 14 : 11.

Step 4: Analyze the Options.

Option (1): 11 : 14 — Incorrect, as this is the reciprocal of the correct ratio.

Option (2): 5 : 6 — Incorrect, as this does not match the calculated value.

Option (3): 14 : 11 — Correct, as it matches the calculated value.

Option (4): 7 : 8 — Incorrect, as this does not match the calculated value.

Step 5: Final Answer.

(3) 14 : 11

Quick Tip

When comparing the areas of a circle and a square with equal perimeters, use the relationship between their dimensions to derive the ratio of their areas. Approximating π as $\frac{22}{7}$ can help simplify calculations and arrive at the correct integer ratio.

13. The length of an arc of a circle of radius 12 cm is 10π . Find the central angle of this arc.

(1) 160°

(2) 150°

(3) 140°

(4) 130°

Correct Answer: (2) 150°

Solution:

Step 1: Recall the formula for the length of an arc.

The length of an arc (L) is given by the formula:

$$L = \frac{\theta}{360^\circ} \times 2\pi r$$

where θ is the central angle in degrees and r is the radius of the circle.

Step 2: Identify the given values.

Length of the arc (L) = 10π cm

Radius of the circle (r) = 12 cm

Step 3: Substitute the given values into the formula and solve for θ .

$$10\pi = \frac{\theta}{360^\circ} \times 2\pi \times 12$$

$$10\pi = \frac{\theta}{360^\circ} \times 24\pi$$

Divide both sides by π :

$$10 = \frac{\theta}{360^\circ} \times 24$$

Now, isolate θ :

$$10 = \frac{24\theta}{360^\circ}$$

$$10 \times 360^\circ = 24\theta$$

$$3600^\circ = 24\theta$$

$$\theta = \frac{3600^\circ}{24}$$

$$\theta = 150^\circ$$

Step 4: Final Answer.

The central angle of the arc is 150° .

$$(2) \quad 150^\circ$$

Quick Tip

Always remember the formula for arc length. If the angle is given in radians, the formula is $L = r\theta_{\text{radians}}$. If the angle is in degrees, use $L = \frac{\theta_{\text{degrees}}}{360^\circ} \times 2\pi r$. Be careful with units and ensure consistency.

14. If a cone of height h and a sphere have same radii r and same volume, then $r:h$ will be:

- (1) 4:1
- (2) 1:4
- (3) 2:3
- (4) 3:2

Correct Answer: (2) 1:4

Solution:

Step 1: Write down the formulas for the volume of a cone and a sphere.

Volume of a cone (V_{cone}) = $\frac{1}{3}\pi r^2 h$

Volume of a sphere (V_{sphere}) = $\frac{4}{3}\pi r^3$

where r is the radius and h is the height.

Step 2: Use the given condition that their volumes are the same.

Given that $V_{\text{cone}} = V_{\text{sphere}}$:

$$\frac{1}{3}\pi r^2 h = \frac{4}{3}\pi r^3$$

Step 3: Simplify the equation to find the ratio $r : h$.

First, cancel common terms on both sides. Both sides have $\frac{1}{3}$ and π . Also, both sides have r^2 :

$$r^2 h = 4r^3$$

Divide both sides by r^2 (assuming $r \neq 0$):

$$h = 4r$$

Now, find the ratio $r : h$.

Divide both sides by h :

$$1 = 4\frac{r}{h}$$

Divide both sides by 4:

$$\frac{1}{4} = \frac{r}{h}$$

So, the ratio $r : h$ is 1 : 4.

Step 4: Final Answer.

The ratio $r : h$ is $1 : 4$.

(2) $1 : 4$

Quick Tip

This problem is a direct application of volume formulas. Always write down the formulas, set up the equality as per the problem statement, and then simplify carefully. Remember that $r^3 = r^2 \times r$.

15. The empirical relationship among the three measures of central tendency (median, mode, and mean) is:

(1) $2 \cdot \text{Median} = 3 \cdot \text{Mode} + \text{Mean}$

(2) $\text{Median} = \text{Mode} + 2 \cdot \text{Mean}$

(3) $2 \cdot \text{Mode} = 3 \cdot \text{Median} + \text{Mean}$

(4) $2 \cdot \text{Mean} = 3 \cdot \text{Median} + 2 \cdot \text{Mode}$

Correct Answer: (4) $2 \cdot \text{Mean} = 3 \cdot \text{Median} + 2 \cdot \text{Mode}$

Solution:

Step 1: Understand the Empirical Relationship.

In statistics, there is an empirical relationship between the mean, median, and mode for a moderately skewed distribution. This relationship is given by:

$$\text{Mode} \approx 3 \cdot \text{Median} - 2 \cdot \text{Mean}$$

Rearranging this formula gives:

$$2 \cdot \text{Mean} = 3 \cdot \text{Median} + 2 \cdot \text{Mode}$$

Step 2: Analyze Each Option.

Let's evaluate each option based on the empirical relationship:

1. $2 \cdot \text{Median} = 3 \cdot \text{Mode} + \text{Mean}$:

Incorrect, as this does not match the standard empirical relationship.

2. $\text{Median} = \text{Mode} + 2 \cdot \text{Mean}$:

Incorrect, as this does not match the standard empirical relationship.

3. $2 \cdot \text{Mode} = 3 \cdot \text{Median} + \text{Mean}$:

Incorrect, as this does not match the standard empirical relationship.

4. $2 \cdot \text{Mean} = 3 \cdot \text{Median} + 2 \cdot \text{Mode}$:

Correct, as this matches the standard empirical relationship.

Step 3: Final Answer.

$$(4) \ 2 \cdot \text{Mean} = 3 \cdot \text{Median} + 2 \cdot \text{Mode}$$

Quick Tip

The empirical relationship between the mean, median, and mode is useful for understanding the skewness of a distribution. Remember that for a moderately skewed distribution, the formula is $\text{Mode} \approx 3 \cdot \text{Median} - 2 \cdot \text{Mean}$. Rearranging this formula gives the correct answer.

16. If the median of the series exceeds the mean by 3, then the number by which the mode exceeds its mean is:

- (1) 8
- (2) 9
- (3) 10
- (4) 11

Correct Answer: (2) 9

Solution:

Step 1: Use the Empirical Relationship.

From the empirical relationship between the mean, median, and mode:

$$\text{Mode} \approx 3 \cdot \text{Median} - 2 \cdot \text{Mean}$$

Step 2: Given Information.

We are told that the median exceeds the mean by 3:

$$\text{Median} = \text{Mean} + 3$$

Step 3: Substitute into the Empirical Formula.

Substitute $\text{Median} = \text{Mean} + 3$ into the empirical formula:

$$\text{Mode} \approx 3 \cdot (\text{Mean} + 3) - 2 \cdot \text{Mean}$$

Simplify:

$$\text{Mode} \approx 3 \cdot \text{Mean} + 9 - 2 \cdot \text{Mean}$$

$$\text{Mode} \approx \text{Mean} + 9$$

Step 4: Determine How Much the Mode Exceeds the Mean.

From the equation $\text{Mode} \approx \text{Mean} + 9$, we see that the mode exceeds the mean by 9.

Step 5: Analyze the Options.

Option (1): 8 — Incorrect, as the mode exceeds the mean by 9.

Option (2): 9 — Correct, as this matches the calculated value.

Option (3): 10 — Incorrect, as the mode exceeds the mean by 9.

Option (4): 11 — Incorrect, as the mode exceeds the mean by 9.

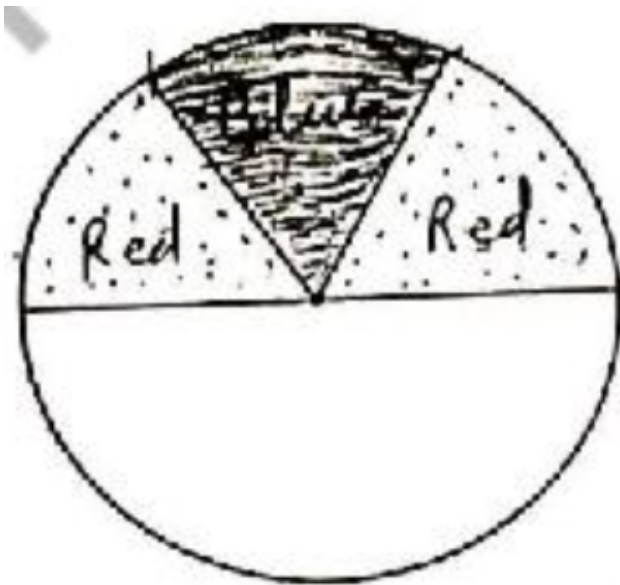
Step 6: Final Answer.

(2) 9

Quick Tip

When solving problems involving the empirical relationship between mean, median, and mode, always start with the formula $\text{Mode} \approx 3 \cdot \text{Median} - 2 \cdot \text{Mean}$. Use the given information to substitute and simplify the expression to find the required value.

17. A student observes the following spinner. What is the probability of obtaining the red colour.



- (1) $\frac{2}{3}$
- (2) $\frac{1}{3}$
- (3) $\frac{5}{3}$
- (4) $\frac{7}{3}$

Correct Answer: (2) $\frac{1}{3}$

Solution:

Step 1: Analyze the spinner's divisions.

The spinner is a circle. Visually inspecting the spinner, we can deduce the proportions of the different colored regions. The circle appears to be divided in such a way that the top semi-circle is split into three approximately equal parts, and the bottom semi-circle is one large part.

Let the total area of the spinner be 1 unit.

The top half represents $\frac{1}{2}$ of the total area.

The bottom half represents $\frac{1}{2}$ of the total area.

In the top half:

One section is labeled "Blue".

Two sections are labeled "Red".

If these three sections in the top half are equal, then each of them occupies $\frac{1}{3}$ of the top half's area.

Step 2: Calculate the area occupied by the red color.

Area of one small section in the top half = $\frac{1}{3} \times \frac{1}{2} = \frac{1}{6}$ of the total spinner area.

Since there are two "Red" sections in the top half:

Total area of Red sections = $2 \times \frac{1}{6} = \frac{2}{6} = \frac{1}{3}$ of the total spinner area.

Step 3: Calculate the probability of obtaining the red color.

The probability of obtaining the red color is the ratio of the area occupied by red to the total area of the spinner:

$$P(\text{Red}) = \frac{\text{Area of Red sections}}{\text{Total Area of Spinner}} = \frac{1}{3}$$

Step 4: Final Answer.

The probability of obtaining the red color is $\frac{1}{3}$.

$$(2) \quad \frac{1}{3}$$

Quick Tip

For spinner problems, the probability of landing on a specific color is the ratio of the angular measure (or area) of that color's sector(s) to the total angle (360°) or total area of the spinner. Carefully interpret the visual divisions.

18. Which of the following cannot be the probability of an event?

- (1) $\frac{2}{3}$
- (2) -1.5
- (3) 20%
- (4) 0.7

Correct Answer: (2) -1.5

Solution:

Step 1: Recall the fundamental properties of probability.

The probability of any event, denoted as $P(E)$, must always satisfy two key conditions:

1. **Non-negativity:** The probability of an event cannot be negative. It must be greater than or equal to 0. So, $P(E) \geq 0$.
2. **Upper bound:** The probability of an event cannot be greater than 1. It must be less than or equal to 1. So, $P(E) \leq 1$.

Combining these, the probability of any event E must lie in the range $[0, 1]$, i.e.,
 $0 \leq P(E) \leq 1$.

Step 2: Evaluate each given option against these properties.

- **(1) $\frac{2}{3}$:** This is a fraction. As a decimal, $\frac{2}{3} \approx 0.666\dots$. This value is clearly between 0 and 1. Therefore, $\frac{2}{3}$ can be the probability of an event.
- **(2) -1.5:** This is a negative number. According to the non-negativity property of probability, a probability value cannot be less than 0. Therefore, -1.5 cannot be the probability of an event.
- **(3) 20%:** Percentages can be converted to decimal form by dividing by 100.
 $20\% = \frac{20}{100} = 0.2$. This value is between 0 and 1. Therefore, 20% can be the probability of an event.
- **(4) 0.7:** This is a decimal number. This value is between 0 and 1. Therefore, 0.7 can be the probability of an event.

Step 3: Identify the value that cannot be a probability.

Based on the evaluation, -1.5 is the only option that violates the fundamental rules of probability.

(2) -1.5

Quick Tip

Remember the golden rule of probability: The probability of any event must be a number between 0 and 1, inclusive. Any value outside this range (i.e., negative or greater than 1) is not a valid probability.

19. One card is drawn from a well-shuffled deck of 52 cards. The probability of getting a face card is:

- (1) $\frac{1}{26}$
- (2) $\frac{3}{13}$
- (3) $\frac{3}{26}$

(4) $\frac{1}{52}$

Correct Answer: (2) $\frac{3}{13}$

Solution:

Step 1: Understand the Deck Composition.

A standard deck of 52 cards consists of:

4 suits (hearts, diamonds, clubs, spades).

Each suit has 13 cards: 2 through 10, Jack, Queen, King, and Ace.

The "face cards" are the Jack, Queen, and King of each suit.

Therefore, there are:

$$3 \text{ face cards per suit} \times 4 \text{ suits} = 12 \text{ face cards in total.}$$

Step 2: Calculate the Probability.

The probability of drawing a face card is given by:

$$P(\text{Face Card}) = \frac{\text{Number of Face Cards}}{\text{Total Number of Cards}} = \frac{12}{52}.$$

Simplify the fraction:

$$P(\text{Face Card}) = \frac{12}{52} = \frac{3}{13}.$$

Step 3: Analyze the Options.

Option (1): $\frac{1}{26}$ — Incorrect, as this does not match the calculated value.

Option (2): $\frac{3}{13}$ — Correct, as it matches the calculated value.

Option (3): $\frac{3}{26}$ — Incorrect, as this does not match the calculated value.

Option (4): $\frac{1}{52}$ — Incorrect, as this does not match the calculated value.

Step 4: Final Answer.

(2) $\frac{3}{13}$

Quick Tip

To calculate probabilities involving a deck of cards, identify the number of favorable outcomes and divide by the total number of possible outcomes. Simplify fractions to match the given options.

20. A dice is thrown twice. The probability that 5 will not come up either time is:

- (1) $\frac{11}{36}$
- (2) $\frac{25}{36}$
- (3) $\frac{13}{36}$
- (4) $\frac{17}{36}$

Correct Answer: (2) $\frac{25}{36}$

Solution:

Step 1: Understand the Problem.

When a die is thrown, there are 6 possible outcomes: {1, 2, 3, 4, 5, 6}.

The probability of rolling a 5 on a single throw is:

$$P(5) = \frac{1}{6}.$$

The probability of not rolling a 5 on a single throw is:

$$P(\text{Not } 5) = 1 - P(5) = 1 - \frac{1}{6} = \frac{5}{6}.$$

Step 2: Calculate the Probability for Two Throws.

Since the throws are independent events, the probability that 5 does not come up on either throw is:

$$P(\text{Not } 5 \text{ on both throws}) = \left(\frac{5}{6}\right) \times \left(\frac{5}{6}\right) = \frac{25}{36}.$$

Step 3: Analyze the Options.

Option (1): $\frac{11}{36}$ — Incorrect, as this does not match the calculated value.

Option (2): $\frac{25}{36}$ — Correct, as it matches the calculated value.

Option (3): $\frac{13}{36}$ — Incorrect, as this does not match the calculated value.

Option (4): $\frac{17}{36}$ — Incorrect, as this does not match the calculated value.

Step 4: Final Answer.

$$(2) \quad \frac{25}{36}$$

Quick Tip

For independent events, the probability of multiple events occurring together is the product of their individual probabilities. When calculating the probability of an event not happening, use the complement rule: $P(\text{Not Event}) = 1 - P(\text{Event})$.

21. An irrational number between 2 and 2.5 is:

- (1) $\sqrt{11}$
- (2) $\sqrt{5}$
- (3) $\sqrt{22.5}$
- (4) $\sqrt{12.5}$

Correct Answer: (2) $\sqrt{5}$

Solution:

Step 1: Understand what an irrational number is and the target range.

An irrational number is a real number that cannot be expressed as a simple fraction of two integers (i.e., $\frac{p}{q}$ where p, q are integers and $q \neq 0$). Its decimal representation is non-terminating and non-repeating. Examples include $\sqrt{2}$, π .

We need to find an irrational number that lies strictly between 2 and 2.5.

To check if a number is between 2 and 2.5, it's often easiest to square the boundary values:

$$2^2 = 4$$

$$(2.5)^2 = 6.25$$

So, we are looking for a number x such that \sqrt{x} is irrational and $4 < x < 6.25$.

Step 2: Evaluate each option to find its approximate value and check if it's irrational.

- **(1) $\sqrt{11}$:** Since $3^2 = 9$ and $4^2 = 16$, $\sqrt{11}$ lies between 3 and 4. $\sqrt{11} \approx 3.317$. This value is not between 2 and 2.5. (11 is not a perfect square, so $\sqrt{11}$ is irrational).
- **(2) $\sqrt{5}$:** Since $2^2 = 4$ and $3^2 = 9$, $\sqrt{5}$ lies between 2 and 3. More precisely, $\sqrt{5} \approx 2.236$. This value is indeed between 2 and 2.5 ($2 < 2.236 < 2.5$). Also, 5 is not a perfect square, so $\sqrt{5}$ is an irrational number.
- **(3) $\sqrt{22.5}$:** Since $4^2 = 16$ and $5^2 = 25$, $\sqrt{22.5}$ lies between 4 and 5. $\sqrt{22.5} \approx 4.743$. This value is not between 2 and 2.5.
- **(4) $\sqrt{12.5}$:** Since $3^2 = 9$ and $4^2 = 16$, $\sqrt{12.5}$ lies between 3 and 4. $\sqrt{12.5} \approx 3.535$. This value is not between 2 and 2.5.

Step 3: Conclude the correct option.

From the evaluation, $\sqrt{5}$ is the only irrational number that falls within the specified range of 2 and 2.5.

$$(2) \quad \sqrt{5}$$

Quick Tip

To quickly check if \sqrt{x} is between two numbers A and B , square A , B , and x . Then verify if $A^2 < x < B^2$. Remember that an irrational number cannot be written as a simple fraction, and square roots of non-perfect squares are common examples.

22. The value of m for which $\left[\left\{\left(\frac{1}{7^2}\right)^{-2}\right\}^{-\frac{1}{3}}\right]^{\frac{1}{4}} = 7^m$ is:

(1) $-\frac{1}{3}$

(2) $\frac{1}{4}$

(3) -3

(4) 2

Correct Answer: (1) $-\frac{1}{3}$

Solution:

Step 1: Simplify the innermost expression using exponent rules.

$$\left(\frac{1}{7^2}\right)^{-2 \times (-\frac{1}{3}) \times \frac{1}{4}} = 7^m$$

Let's start with the innermost part: $\left(\frac{1}{7^2}\right)^{-2}$. Recall the exponent rule: $\left(\frac{1}{a^b}\right)^{-c} = (a^{-b})^{-c} = a^{bc}$.

Here, $a = 7$, $b = 2$, $c = 2$.

So, $\left(\frac{1}{7^2}\right)^{-2} = (7^{-2})^{-2} = 7^{(-2) \times (-2)} = 7^4$.

Step 2: Substitute the simplified expression back and simplify the next layer.

Now the equation becomes: $\left[\{7^4\}^{-\frac{1}{3}}\right]^{\frac{1}{4}} = 7^m$.

Next, simplify $(7^4)^{-\frac{1}{3}}$.

Recall the exponent rule: $(a^b)^c = a^{bc}$.

Here, $a = 7$, $b = 4$, $c = -\frac{1}{3}$.

So, $(7^4)^{-\frac{1}{3}} = 7^{4 \times (-\frac{1}{3})} = 7^{-\frac{4}{3}}$.

Step 3: Substitute this simplified expression back and simplify the outermost layer.

The equation is now: $\left[7^{-\frac{4}{3}}\right]^{\frac{1}{4}} = 7^m$.

Finally, simplify $\left(7^{-\frac{4}{3}}\right)^{\frac{1}{4}}$.

Using the same rule $(a^b)^c = a^{bc}$:

Here, $a = 7$, $b = -\frac{4}{3}$, $c = \frac{1}{4}$.

So, $\left(7^{-\frac{4}{3}}\right)^{\frac{1}{4}} = 7^{(-\frac{4}{3}) \times (\frac{1}{4})} = 7^{-\frac{4 \times 1}{3 \times 4}} = 7^{-\frac{4}{12}} = 7^{-\frac{1}{3}}$.

Step 4: Equate the exponents.

We have simplified the left side of the equation to $7^{-\frac{1}{3}}$. The original equation is $7^{-\frac{1}{3}} = 7^m$.

Since the bases are equal (both are 7), the exponents must also be equal. Therefore, $m = -\frac{1}{3}$.

(1) $-\frac{1}{3}$

Quick Tip

When dealing with multiple nested exponents, work from the inside out. Always remember the fundamental rules of exponents: $(a^m)^n = a^{mn}$, $a^{-m} = \frac{1}{a^m}$, and $(a/b)^m = a^m/b^m$. Consistent application of these rules simplifies complex expressions.

23. If $\sqrt{13 - a\sqrt{10}} = \sqrt{8} + \sqrt{5}$ then a =

(1) -5

(2) -6

(3) -4

(4) -2

Correct Answer: (3) -4

Solution:

Step 1: Simplify the right-hand side (RHS) or prepare to square both sides.

The given equation is $\sqrt{13 - a\sqrt{10}} = \sqrt{8} + \sqrt{5}$.

To eliminate the outermost square root on the left side, we will square both sides of the equation.

Step 2: Square both sides of the equation.

$$(\sqrt{13 - a\sqrt{10}})^2 = (\sqrt{8} + \sqrt{5})^2$$

The left side simplifies to:

$$13 - a\sqrt{10}$$

The right side uses the identity $(x + y)^2 = x^2 + y^2 + 2xy$, with $x = \sqrt{8}$ and $y = \sqrt{5}$:

$$(\sqrt{8})^2 + (\sqrt{5})^2 + 2\sqrt{8}\sqrt{5} = 8 + 5 + 2\sqrt{40}$$

Step 3: Simplify the radical term on the RHS.

$$2\sqrt{40} = 2\sqrt{4 \cdot 10} = 2 \cdot 2\sqrt{10} = 4\sqrt{10}$$

Now the RHS becomes:

$$13 + 4\sqrt{10}$$

Step 4: Equate the simplified left and right sides of the equation.

$$13 - a\sqrt{10} = 13 + 4\sqrt{10}$$

Step 5: Solve for a by comparing coefficients.

Subtract 13 from both sides:

$$-a\sqrt{10} = 4\sqrt{10}$$

Divide both sides by $\sqrt{10}$:

$$-a = 4$$

Multiply by -1:

$$a = -4$$

Step 6: Final Answer.

$$\mathbf{(3) \quad -4}$$

Quick Tip

When dealing with equations involving surds (square roots), especially nested ones or sums/differences of surds, squaring both sides is a very common and effective first step. Remember the perfect square factors when simplifying radicals (e.g., $\sqrt{AB} = \sqrt{A}\sqrt{B}$). Comparing the rational and irrational parts on both sides after squaring is crucial for solving.

24. If $\frac{a}{b} + \frac{b}{a} = 1$, then $a^3 + b^3 =$

(1) 1

(2) -1

(3) $\frac{1}{2}$

(4) 0

Correct Answer: (4) 0

Solution:

Step 1: Analyze the Given Equation.

We are given:

$$\frac{a}{b} + \frac{b}{a} = 1$$

Rewrite this using a common denominator:

$$\frac{a^2 + b^2}{ab} = 1$$

Multiply both sides by ab (assuming $a, b \neq 0$):

$$a^2 + b^2 = ab$$

Step 2: Use the Identity for $a^3 + b^3$.

The identity is:

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

From earlier, we know:

$$a^2 + b^2 = ab$$

Now substitute into the expression $a^2 - ab + b^2$:

$$a^2 - ab + b^2 = (a^2 + b^2) - ab = ab - ab = 0$$

Thus:

$$a^3 + b^3 = (a + b)(0) = 0$$

Step 3: Analyze the Options.

Option (1): 1 — Incorrect

Option (2): -1 — Incorrect

Option (3): $\frac{1}{2}$ — Incorrect

Option (4): 0 — Correct

Step 4: Final Answer.

(4) 0

Quick Tip

When solving problems involving algebraic identities, use known formulas like the sum of cubes and simplify step-by-step. Substituting relationships derived from the given equations can help reduce complexity.

25. The value of $\frac{(2.3)^3 - 0.027}{(2.3)^2 + 0.69 + 0.09}$ is:

(1) 2

(2) 3

(3) 2.327

(4) 2.273

Correct Answer: (1) 2

Solution:

Step 1: Simplify the Numerator.

The numerator is:

$$(2.3)^3 - 0.027$$

Notice that $0.027 = (0.3)^3$. So the numerator becomes:

$$(2.3)^3 - (0.3)^3$$

Use the identity:

$$x^3 - y^3 = (x - y)(x^2 + xy + y^2)$$

Here, $x = 2.3$ and $y = 0.3$. So:

$$(2.3)^3 - (0.3)^3 = (2.3 - 0.3)((2.3)^2 + (2.3)(0.3) + (0.3)^2)$$

Now simplify each term:

$$2.3 - 0.3 = 2$$

$$(2.3)^2 + (2.3)(0.3) + (0.3)^2 = 5.29 + 0.69 + 0.09 = 6$$

So the numerator is:

$$2 \times 6 = 12$$

Step 2: Simplify the Denominator.

The denominator is:

$$(2.3)^2 + 0.69 + 0.09 = 5.29 + 0.78 = 6$$

Step 3: Compute the Fraction.

Now evaluate:

$$\frac{(2.3)^3 - 0.027}{(2.3)^2 + 0.69 + 0.09} = \frac{12}{6} = 2$$

Step 4: Analyze the Options.

Option (1): 2 — Correct

Option (2): 3 — Incorrect

Option (3): 2.327 — Incorrect

Option (4): 2.273 — Incorrect

Step 5: Final Answer.

(1) 2

Quick Tip

When simplifying expressions involving powers and sums, look for patterns or formulas like the difference of cubes. Breaking down terms and simplifying step-by-step ensures accuracy.

26. If $(x^{140} + 2x^{151} + K)$ is divisible by $(x + 1)$ then the value of K is :

(1) 1

(2) -3

(3) 2

(4) -2

Correct Answer: (1) 1

Solution:

Step 1: Understand the Remainder Theorem.

The Remainder Theorem states that if a polynomial $P(x)$ is divided by $(x - a)$, then the remainder is $P(a)$.

In this problem, the polynomial is $P(x) = x^{140} + 2x^{151} + K$.

It is given that $P(x)$ is divisible by $(x + 1)$. This means that when $P(x)$ is divided by $(x + 1)$, the remainder is 0.

According to the Remainder Theorem, if $P(x)$ is divisible by $(x + 1)$, then $P(-1) = 0$. (Here, $x - a = x + 1$, so $a = -1$).

Step 2: Substitute $x = -1$ into the polynomial.

Substitute $x = -1$ into the expression for $P(x)$:

$$P(-1) = (-1)^{140} + 2(-1)^{151} + K$$

Step 3: Evaluate the powers of -1.

Recall that $(-1)^{\text{even number}} = 1$ and $(-1)^{\text{odd number}} = -1$.

Here, 140 is an even number, so $(-1)^{140} = 1$.

And 151 is an odd number, so $(-1)^{151} = -1$.

Step 4: Substitute the evaluated powers back into the expression for $P(-1)$.

$$P(-1) = 1 + 2(-1) + K$$

$$P(-1) = 1 - 2 + K$$

$$P(-1) = -1 + K$$

Step 5: Set $P(-1)$ to 0 and solve for K.

Since $P(x)$ is divisible by $(x + 1)$, we know that $P(-1) = 0$. So, set the expression for $P(-1)$ equal to 0:

$$-1 + K = 0$$

Add 1 to both sides:

$$K = 1$$

Step 6: Final Answer.

The value of K is 1.

(1) 1

Quick Tip

The Remainder Theorem is crucial for problems involving divisibility of polynomials. If a polynomial $P(x)$ is divisible by $(x - a)$, then $P(a)$ must be 0. Remember to correctly handle the signs when substituting negative values into powers.

27. If the graph of the equation $4x + 3y = 12$ cuts the coordinate axes at A and B , then the hypotenuse of right triangle $\triangle AOB$ is of length:

- (1) 4 units
- (2) 3 units
- (3) 5 units
- (4) None of these

Correct Answer: (3) 5 units

Solution:

Step 1: Find the Points of Intersection with the Coordinate Axes.

The given equation is:

$$4x + 3y = 12.$$

Intersection with the x-axis ($y = 0$):

Substitute $y = 0$ into the equation:

$$4x + 3(0) = 12 \implies 4x = 12 \implies x = 3.$$

So, the point of intersection with the x-axis is $A(3, 0)$.

Intersection with the y-axis ($x = 0$):

Substitute $x = 0$ into the equation:

$$4(0) + 3y = 12 \implies 3y = 12 \implies y = 4.$$

So, the point of intersection with the y-axis is $B(0, 4)$.

Step 2: Determine the Lengths of the Legs of the Right Triangle.

The points $A(3, 0)$ and $B(0, 4)$ form a right triangle $\triangle AOB$ with the origin $O(0, 0)$. The lengths of the legs of the triangle are:

Distance from O to A (along the x-axis):

$$OA = 3 \text{ units.}$$

Distance from O to B (along the y-axis):

$$OB = 4 \text{ units.}$$

Step 3: Calculate the Hypotenuse.

The hypotenuse AB is the distance between points $A(3, 0)$ and $B(0, 4)$. Using the distance formula:

$$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}.$$

Substitute $A(3, 0)$ and $B(0, 4)$:

$$AB = \sqrt{(0 - 3)^2 + (4 - 0)^2} = \sqrt{(-3)^2 + 4^2} = \sqrt{9 + 16} = \sqrt{25} = 5.$$

Step 4: Analyze the Options.

Option (1): 4 units — Incorrect, as the hypotenuse is 5 units.

Option (2): 3 units — Incorrect, as the hypotenuse is 5 units.

Option (3): 5 units — Correct, as it matches the calculated value.

Option (4): None of these — Incorrect, as 5 units is a valid option.

Step 5: Final Answer.

(3) 5 units

Quick Tip

To find the hypotenuse of a right triangle formed by the intercepts of a linear equation, first determine the intercepts, then use the Pythagorean theorem or the distance formula to calculate the hypotenuse.

28. Two points having the same abscissae but different ordinates lie on:

- (1) x-axis
- (2) y-axis
- (3) a line parallel to the y-axis
- (4) a line parallel to the x-axis

Correct Answer: (3) a line parallel to the y-axis

Solution:

Step 1: Understand the Problem.

The abscissa of a point refers to its x-coordinate, and the ordinate refers to its y-coordinate.

If two points have the same abscissa but different ordinates, their x-coordinates are identical, while their y-coordinates differ.

Step 2: Analyze Each Option.

Let the two points be $P(x_1, y_1)$ and $Q(x_1, y_2)$, where x_1 is the same for both points, but $y_1 \neq y_2$.

1. x-axis:

Points on the x-axis have $y = 0$. Since the ordinates are different, these points cannot lie on the x-axis.

2. y-axis:

Points on the y-axis have $x = 0$. Since the abscissae are the same but not necessarily zero, these points do not necessarily lie on the y-axis.

3. a line parallel to the y-axis:

A line parallel to the y-axis has a constant x-coordinate. Since both points have the same x-coordinate, they lie on a vertical line parallel to the y-axis.

4. a line parallel to the x-axis:

A line parallel to the x-axis has a constant y-coordinate. Since the ordinates are different, these points do not lie on a horizontal line.

Step 3: Analyze the Options.

Option (1): x-axis — Incorrect, as the ordinates are different.

Option (2): y-axis — Incorrect, as the abscissae are not necessarily zero.

Option (3): a line parallel to the y-axis — Correct, as points with the same abscissa lie on a vertical line.

Option (4): a line parallel to the x-axis — Incorrect, as the ordinates are different.

Step 4: Final Answer.

(3) a line parallel to the y-axis

Quick Tip

Points with the same abscissa (x-coordinate) but different ordinates (y-coordinates) lie on a vertical line parallel to the y-axis. This is because their x-coordinates remain constant, while their y-coordinates vary.

29. Two complementary angles are such that two times the measure of one is equal to three times the measure of the other. The measure of the smaller angle is :

- (1) 45°
- (2) 30°
- (3) 36°
- (4) None of these

Correct Answer: (3) 36°

Solution:

Step 1: Define complementary angles and set up equations.

Complementary angles are two angles whose sum is 90° .

Let the two angles be x and y .

From the definition of complementary angles:

$$x + y = 90^\circ \text{ (Equation 1)}$$

From the problem statement, "two times the measure of one is equal to three times the measure of the other":

$$2x = 3y \text{ (Equation 2)}$$

Step 2: Solve the system of equations.

From Equation 2, express one variable in terms of the other.

$$x = \frac{3}{2}y$$

Substitute this expression for x into Equation 1:

$$\frac{3}{2}y + y = 90^\circ$$

Multiply by 2 to eliminate the fraction:

$$3y + 2y = 180^\circ$$

$$5y = 180^\circ$$

$$y = \frac{180^\circ}{5}$$

$$y = 36^\circ$$

Now, find x using Equation 1:

$$x + 36^\circ = 90^\circ$$

$$x = 90^\circ - 36^\circ$$

$$x = 54^\circ$$

Step 3: Identify the smaller angle.

The two angles are 54° and 36° .

The smaller angle is 36° .

Step 4: Compare with the given options.

The calculated smaller angle is 36° , which matches option (3).

(3) 36°

Quick Tip

Remember that "complementary" means angles sum to 90° , while "supplementary" means angles sum to 180° . Always set up two equations from the given information to solve for two unknown angles.

30. If one angle of a parallelogram is 24° less than twice the smallest angle, then the measure of the largest angle of the parallelogram is :

(1) 176°

(2) 68°

(3) 112°

(4) 102°

Correct Answer: (3) 112°

Solution: Step 1: Recall properties of a parallelogram.

In a parallelogram, consecutive angles are supplementary (sum to 180°), and opposite angles are equal.

Let the two distinct angles of the parallelogram be α and β . We know that $\alpha + \beta = 180^\circ$.

Step 2: Set up equations based on the problem statement.

Let the smallest angle be S .

Let the other angle be L .

From the problem statement, "one angle of a parallelogram is 24° less than twice the smallest angle".

$$\text{So, } L = 2S - 24^\circ.$$

Also, we know that the sum of adjacent angles in a parallelogram is 180° :

$$S + L = 180^\circ$$

Step 3: Solve the system of equations for S and L .

Substitute the expression for L into the sum equation:

$$S + (2S - 24^\circ) = 180^\circ$$

$$3S - 24^\circ = 180^\circ$$

$$3S = 180^\circ + 24^\circ$$

$$3S = 204^\circ$$

$$S = \frac{204^\circ}{3}$$

$$S = 68^\circ$$

Now, find L :

$$L = 2S - 24^\circ$$

$$L = 2(68^\circ) - 24^\circ$$

$$L = 136^\circ - 24^\circ$$

$$L = 112^\circ$$

Step 4: Identify the largest angle.

The two angles are $S = 68^\circ$ and $L = 112^\circ$.

The largest angle of the parallelogram is 112° .

(Check: $68^\circ + 112^\circ = 180^\circ$, which is correct for adjacent angles of a parallelogram).

Step 5: Compare with the given options.

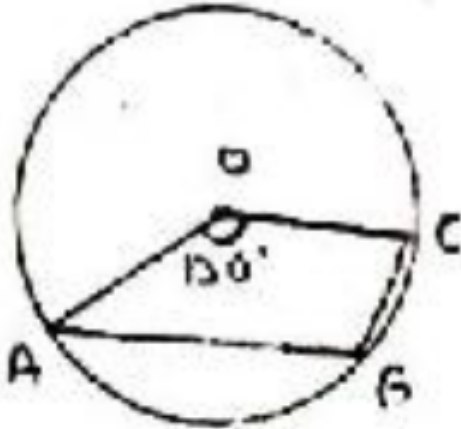
The calculated largest angle is 112° , which matches option (3).

(3) 112°

Quick Tip

Always remember the fundamental properties of parallelograms: consecutive angles are supplementary, and opposite angles are equal. This allows you to set up equations to solve for unknown angles.

31. In figure, O is the centre of the circle such that $\angle AOC = 130^\circ$, then $\angle ABC = \dots\dots$



- (1) 130°
- (2) 115°
- (3) 65°
- (4) 165°

Correct Answer: (2) 115°

Solution:

Step 1: Understand the relationship between the angle at the center and the angle at the circumference.

The angle subtended by an arc at the center of a circle is double the angle subtended by it at any point on the remaining part of the circle.

Step 2: Calculate the reflex angle $\angle AOC$.

The given $\angle AOC$ is 130° . This is the angle subtended by the minor arc AC at the center.

The reflex angle $\angle AOC$ (the angle formed by the major arc AC at the center) is

$$360^\circ - 130^\circ = 230^\circ.$$

Step 3: Apply the theorem for the angle subtended by the major arc.

The angle subtended by the major arc AC at the center is the reflex $\angle AOC = 230^\circ$.

The angle subtended by the major arc AC at point B on the circumference is $\angle ABC$.

According to the theorem, reflex $\angle AOC = 2 \times \angle ABC$.

Step 4: Solve for $\angle ABC$.

$$230^\circ = 2 \times \angle ABC$$

$$\angle ABC = \frac{230^\circ}{2}$$

$$\angle ABC = 115^\circ$$

Step 5: Compare the result with the given options.

The calculated angle $\angle ABC$ is 115° , which matches option (2).

(2) 115°

Quick Tip

Always be careful to distinguish between the angle subtended by the minor arc and the major (reflex) arc at the center when applying the theorem. The angle at the circumference corresponds to the arc it subtends.

32. The sum of the length, breadth and depth of a cuboid is 19 cm and its diagonal is $5\sqrt{5}$ cm. Its surface area is :

(1) 361 cm^2

(2) 125 cm^2

(3) 236 cm^2

(4) 486 cm^2

Correct Answer: (3) 236 cm^2

Solution:

Step 1: Define variables and write down the given information.

Let the length, breadth, and depth (height) of the cuboid be l , b , and h respectively.

Given:

1. Sum of length, breadth, and depth: $l + b + h = 19 \text{ cm}$

2. Length of the diagonal: $D = 5\sqrt{5} \text{ cm}$

Step 2: Recall the formulas for the diagonal and surface area of a cuboid.

The formula for the diagonal of a cuboid is $D = \sqrt{l^2 + b^2 + h^2}$.

The formula for the total surface area of a cuboid is $SA = 2(lb + bh + hl)$.

Step 3: Use the diagonal information.

We are given $D = 5\sqrt{5} \text{ cm}$.

So, $\sqrt{l^2 + b^2 + h^2} = 5\sqrt{5}$.

Squaring both sides:

$$l^2 + b^2 + h^2 = (5\sqrt{5})^2$$

$$l^2 + b^2 + h^2 = 25 \times 5$$

$$l^2 + b^2 + h^2 = 125$$

Step 4: Use the sum of sides information to find the surface area.

We know the algebraic identity:

$$(l + b + h)^2 = l^2 + b^2 + h^2 + 2(lb + bh + hl)$$

We have:

$$l + b + h = 19$$

$$l^2 + b^2 + h^2 = 125$$

Substitute these values into the identity:

$$(19)^2 = 125 + 2(lb + bh + hl)$$

$$361 = 125 + 2(lb + bh + hl)$$

We recognize $2(lb + bh + hl)$ as the surface area (SA) of the cuboid. $361 = 125 + SA$

Step 5: Solve for the surface area.

$$SA = 361 - 125$$

$$SA = 236 \text{ cm}^2$$

Step 6: Compare with the given options.

The calculated surface area is 236 cm^2 , which matches option (3).

(3) 236 cm^2

Quick Tip

This problem cleverly uses the algebraic identity $(a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$ to connect the sum of dimensions, the diagonal, and the surface area of a cuboid.

Recognizing this identity is key to a straightforward solution.

33. Vertical cross-section of a right circular cylinder is always a :

- (1) Square
- (2) Rectangle
- (3) Rhombus

(4) Trapezium

Correct Answer: (2) Rectangle

Solution:

Step 1: Understand what a right circular cylinder is.

A right circular cylinder is a 3D geometric shape with two parallel circular bases of the same radius and a curved surface connecting them. The axis connecting the centers of the circular bases is perpendicular to the bases.

Step 2: Understand what a vertical cross-section means.

A vertical cross-section is obtained by cutting the cylinder with a plane that passes through its axis or is parallel to its axis.

Step 3: Visualize the cross-section.

Imagine cutting a cylinder straight down from top to bottom. If you cut a right circular cylinder vertically, the resulting 2D shape will have two sides that are part of the curved surface (which appear as straight lines when cut vertically) and two sides that are parts of the circular bases.

Let the radius of the cylinder be r and its height be h .

When you make a vertical cut:

If the cut passes through the center of the circular bases (i.e., along the diameter), the width of the cross-section will be $2r$ (the diameter), and the height will be h .

If the cut is parallel to the axis but not through the center, the width of the cross-section will be less than $2r$, but the height will still be h .

In both cases, the opposite sides will be parallel, and all angles will be right angles (90 degrees) because the vertical cut is perpendicular to the circular bases.

Step 4: Determine the shape.

A quadrilateral with all angles equal to 90 degrees is a rectangle.

While a square is a special type of rectangle (where all sides are equal), a vertical cross-section of a cylinder is not *always* a square. It would only be a square if the diameter of the cylinder ($2r$) happened to be equal to its height (h), which is not a general property.

Therefore, the most general and always true description for a vertical cross-section of a right circular cylinder is a rectangle.

Step 5: Compare with the given options.

The calculated shape is a rectangle, which matches option (2).

(2) Rectangle

Quick Tip

To visualize cross-sections, imagine slicing through the 3D object with a flat knife. A 'vertical' cross-section usually implies a slice parallel to the height or axis of the object. For a right circular cylinder, such a slice will always produce a rectangle.

34. The ratio between the volume of a sphere and volume of a circumscribing right circular cylinder is :

- (1) 2 : 1
- (2) 1 : 1
- (3) 2 : 3
- (4) 1 : 2

Correct Answer: (3) 2 : 3

Solution:

Step 1: Understand the term 'circumscribing right circular cylinder'.

A circumscribing right circular cylinder for a sphere means that the cylinder just encloses the sphere such that the sphere touches the top, bottom, and curved surface of the cylinder.

For this to happen:

The radius of the cylinder (R_{cyl}) must be equal to the radius of the sphere (R_{sph}). So,

$$R_{cyl} = R_{sph} = R.$$

The height of the cylinder (H_{cyl}) must be equal to the diameter of the sphere. So,

$$H_{cyl} = 2R_{sph} = 2R.$$

Step 2: Write down the formulas for the volume of a sphere and a cylinder.

$$\text{Volume of a sphere } (V_{sph}) = \frac{4}{3}\pi R_{sph}^3$$

$$\text{Volume of a cylinder } (V_{cyl}) = \pi R_{cyl}^2 H_{cyl}$$

Step 3: Substitute the relationships from Step 1 into the volume formulas.

For the sphere, let its radius be R . So, $V_{sph} = \frac{4}{3}\pi R^3$.

For the circumscribing cylinder:

$$R_{cyl} = R$$

$$H_{cyl} = 2R$$

$$\text{So, } V_{cyl} = \pi(R)^2(2R) = 2\pi R^3.$$

Step 4: Calculate the ratio of the volume of the sphere to the volume of the circumscribing cylinder.

$$\text{Ratio} = \frac{V_{sph}}{V_{cyl}} = \frac{\frac{4}{3}\pi R^3}{2\pi R^3}$$

Cancel out πR^3 from the numerator and denominator:

$$\text{Ratio} = \frac{\frac{4}{3}}{2} = \frac{4}{3 \times 2} = \frac{4}{6} = \frac{2}{3}$$

So, the ratio is 2 : 3.

Step 5: Compare with the given options.

The calculated ratio is 2 : 3, which matches option (3).

(3) 2 : 3

Quick Tip

This problem is a classic geometry question that highlights the relationship between a sphere and its circumscribing cylinder. The key is to correctly identify the dimensions of the cylinder in terms of the sphere's radius.

35. If the ratio of mode and median of a certain data is 6 : 5, then find the ratio of its mean and median :

- (1) 3 : 5
- (2) 3 : 10
- (3) 9 : 10
- (4) 10 : 9

Correct Answer: (3) 9 : 10

Solution:

Step 1: Recall the empirical relationship between Mean, Median, and Mode.

For a moderately skewed distribution, there is an empirical relationship (often called the Empirical Mean-Median-Mode Formula or Karl Pearson's empirical relation):

$$\text{Mode} = 3 \text{ Median} - 2 \text{ Mean}$$

Step 2: Write down the given ratio.

Given: Ratio of Mode to Median = 6 : 5

This means $\frac{\text{Mode}}{\text{Median}} = \frac{6}{5}$.

So, Mode = $\frac{6}{5}$ Median.

Step 3: Substitute the given ratio into the empirical formula.

Substitute Mode = $\frac{6}{5}$ Median into the formula:

$$\frac{6}{5} \text{ Median} = 3 \text{ Median} - 2 \text{ Mean}$$

Step 4: Rearrange the equation to find the relationship between Mean and Median.

Move the terms involving Median to one side and Mean to the other side:

$$2 \text{ Mean} = 3 \text{ Median} - \frac{6}{5} \text{ Median}$$

$$2 \text{ Mean} = \left(\frac{15}{5} - \frac{6}{5}\right) \text{ Median}$$

$$2 \text{ Mean} = \frac{9}{5} \text{ Median}$$

Step 5: Find the ratio of Mean and Median.

We need to find $\frac{\text{Mean}}{\text{Median}}$.

From the equation $2 \text{ Mean} = \frac{9}{5} \text{ Median}$, divide both sides by 2 and by Median:

$$\frac{\text{Mean}}{\text{Median}} = \frac{9}{5 \times 2}$$

$$\frac{\text{Mean}}{\text{Median}} = \frac{9}{10}$$

So, the ratio of mean and median is 9 : 10.

Step 6: Compare with the given options.

The calculated ratio is 9 : 10, which matches option (3).

(3) 9 : 10

Quick Tip

This problem relies on knowing the empirical relationship between the measures of central tendency: Mode = 3 Median - 2 Mean. This formula is approximate but widely used in statistics for moderately skewed distributions.

36. If $\sqrt{2^n} = 1024$ then $3^{2(\frac{n}{4}-1)} = \dots\dots\dots$

(1) 3

(2) 9

(3) 27

(4) 81

Correct Answer: (4) 81

Solution:

Step 1: Solve for 'n' from the first equation.

The given equation is $\sqrt{2^n} = 1024$.

We can rewrite $\sqrt{2^n}$ as $2^{n/2}$.

So, $2^{n/2} = 1024$.

Express 1024 as a power of 2: $1024 = 2^{10}$.

Equating the exponents:

$$n/2 = 10$$

$$n = 2 \times 10$$

$$n = 20$$

Step 2: Substitute the value of 'n' into the expression to be evaluated.

The expression to evaluate is $3^{2(\frac{n}{4}-1)}$.

Substitute $n = 20$:

$$3^{2(\frac{20}{4}-1)}$$

Step 3: Simplify the exponent.

First, simplify the term inside the parenthesis: $\frac{20}{4} = 5$. So, the exponent becomes $2(5 - 1)$.

$$2(5 - 1) = 2(4) = 8.$$

Step 4: Calculate the final value (and address potential typo).

The expression is 3^8 .

$$3^8 = 3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3 = 6561.$$

However, 6561 is not among the given options (3, 9, 27, 81).

Given the options, it is highly probable there is a typo in the question and the exponent should have been $(\frac{n}{4} - 1)$ instead of $2(\frac{n}{4} - 1)$. Let's proceed with this assumption to match one of the options.

Recalculation based on assumed typo ($3^{(\frac{n}{4}-1)}$):

Substitute $n = 20$ into the modified expression:

$$3^{(\frac{20}{4}-1)}$$

Simplify the exponent:

$$3^{(5-1)} = 3^4$$

Calculate the final value:

$$3^4 = 3 \times 3 \times 3 \times 3 = 81.$$

Step 5: Compare the result with the given options.

The calculated value 81 matches option (4).

(4) 81

Quick Tip

When solving exponential equations, try to express both sides with the same base. If the powers are equal, then their exponents must also be equal. In multiple-choice questions, if your literal calculation doesn't match any option, re-examine the question for common typos, especially in exponents or coefficients, that might lead to one of the given answers.

37. If $3x = a + b + c$, then the value of

$$[(x - a)^3 + (x - b)^3 + (x - c)^3 - 3(x - a)(x - b)(x - c)] \text{ is :}$$

(1) $a + b + c$

(2) $(a - b)(b - c)(c - a)$

(3) 0

(4) None of these

Correct Answer: (3) 0

Solution:

Step 1: Recall the algebraic identity for sum of cubes.

A key algebraic identity states: If $A + B + C = 0$, then $A^3 + B^3 + C^3 = 3ABC$.

This can be rearranged as: $A^3 + B^3 + C^3 - 3ABC = 0$.

Step 2: Define A, B, and C in terms of the given expression.

Let's assign the terms inside the cubes to variables:

Let $A = (x - a)$

Let $B = (x - b)$

Let $C = (x - c)$

The expression we need to evaluate is exactly in the form $[A^3 + B^3 + C^3 - 3ABC]$.

Step 3: Check if the condition $A + B + C = 0$ is met.

Calculate the sum of A, B, and C:

$$A + B + C = (x - a) + (x - b) + (x - c)$$

$$A + B + C = x - a + x - b + x - c$$

$$A + B + C = 3x - (a + b + c)$$

Step 4: Use the given information to simplify $A + B + C$.

The problem states that $3x = a + b + c$.

Substitute this into the sum $A + B + C$:

$$A + B + C = (a + b + c) - (a + b + c)$$

$$A + B + C = 0$$

Step 5: Apply the algebraic identity.

Since $A + B + C = 0$, according to the identity mentioned in Step 1:

$$A^3 + B^3 + C^3 - 3ABC = 0$$

Therefore, the value of the given expression is 0.

Step 6: Compare the result with the given options.

The calculated value is 0, which matches option (3).

(3) 0

Quick Tip

This problem is a direct application of a common algebraic identity. Recognizing expressions like $A^3 + B^3 + C^3 - 3ABC$ should prompt you to check if the sum $A + B + C$ equals zero, as this simplifies the expression considerably.

38. The percentage increase in the area of a triangle if its each side is doubled will be:

- (1) 200%
- (2) 300%
- (3) 400%
- (4) None of these

Correct Answer: (3) 400%

Solution:

Step 1: Relationship Between Side Length and Area.

If each side of a triangle is doubled, then the new area is:

$$\text{New Area} = (2)^2 \times \text{Original Area} = 4 \times \text{Original Area}.$$

Step 2: Calculate Percentage Increase.

Percentage increase is:

$$\frac{\text{New Area} - \text{Original Area}}{\text{Original Area}} \times 100\% = \frac{4\text{Original Area} - \text{Original Area}}{\text{Original Area}} \times 100\% = 3 \times 100\% = 300\%.$$

Step 3: Analyze the Options.

Option (1): 200% — Incorrect.

Option (2): 300% — Correct.

Option (3): 400% — Incorrect (this is total area, not increase).

Option (4): None of these — Incorrect.

Step 4: Final Answer.

300%

Quick Tip

When each side of a triangle is doubled, the area increases by a factor of 4 because the area is proportional to the square of the side length. This corresponds to a 400% increase in the area.

39. If ℓ is the length of a diagonal of a cube of volume V , then:

(1) $3V = \ell^3$

(2) $\sqrt{3}V = \ell^3$

(3) $3\sqrt{3}V = 2\ell^3$

(4) $3\sqrt{3}V = \ell^3$

Correct Answer: (4) $3\sqrt{3}V = \ell^3$

Solution:

Step 1: Relate the Diagonal of the Cube to Its Side Length.

Let the side length of the cube be a . The volume of the cube is:

$$V = a^3.$$

The length of the space diagonal of the cube is given by:

$$\ell = a\sqrt{3}.$$

Step 2: Express ℓ in Terms of V .

From $V = a^3$, we have:

$$a = \sqrt[3]{V}.$$

Substitute $a = \sqrt[3]{V}$ into the expression for ℓ :

$$\ell = \sqrt[3]{V} \cdot \sqrt{3}.$$

Cube both sides to eliminate the cube root:

$$\ell^3 = \left(\sqrt[3]{V} \cdot \sqrt{3}\right)^3 = \left(\sqrt[3]{V}\right)^3 \cdot (\sqrt{3})^3 = V \cdot 3\sqrt{3}.$$

Thus:

$$3\sqrt{3}V = \ell^3.$$

Step 3: Analyze the Options.

Option (1): $3V = \ell^3$ — Incorrect, as it does not match the derived equation.

Option (2): $\sqrt{3}V = \ell^3$ — Incorrect, as it does not match the derived equation.

Option (3): $3\sqrt{3}V = 2\ell^3$ — Incorrect, as it does not match the derived equation.

Option (4): $3\sqrt{3}V = \ell^3$ — Correct, as it matches the derived equation.

Step 4: Final Answer.

$$(4) \ 3\sqrt{3}V = \ell^3$$

Quick Tip

The diagonal of a cube relates to its side length by $\ell = a\sqrt{3}$. Using the relationship between the side length and volume ($a = \sqrt[3]{V}$), you can derive the equation $3\sqrt{3}V = \ell^3$.

40. The algebraic sum of the deviations of a set of 'n' values from their mean is :

- (1) 0
- (2) n-1
- (3) n
- (4) n+1

Correct Answer: (1) 0

Solution:

Step 1: Define the terms.

Let a set of 'n' values be x_1, x_2, \dots, x_n . The mean of these values, denoted by \bar{x} , is given by:

$$\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$$

The deviation of a value x_i from the mean \bar{x} is $(x_i - \bar{x})$.

Step 2: Calculate the algebraic sum of the deviations.

The algebraic sum of the deviations is $\sum_{i=1}^n (x_i - \bar{x})$.

Expand the sum: $\sum_{i=1}^n (x_i - \bar{x}) = (x_1 - \bar{x}) + (x_2 - \bar{x}) + \dots + (x_n - \bar{x})$

Rearrange the terms: $= (x_1 + x_2 + \dots + x_n) - (\bar{x} + \bar{x} + \dots + \bar{x} \text{ (n times)}) = \sum_{i=1}^n x_i - n\bar{x}$

Step 3: Substitute the definition of the mean into the expression.

We know that $\sum_{i=1}^n x_i = n\bar{x}$ from the definition of the mean. Substitute this into the sum of deviations: $\sum_{i=1}^n x_i - n\bar{x} = n\bar{x} - n\bar{x} = 0$

Step 4: Conclude the result.

The algebraic sum of the deviations of a set of 'n' values from their mean is always 0.

Step 5: Compare with the given options.

The result is 0, which matches option (1).

(1) 0

Quick Tip

This is a fundamental property of the arithmetic mean. The mean is the balancing point of the data; thus, the sum of positive deviations from the mean exactly balances the sum of negative deviations, resulting in a net sum of zero.

41. H.C.F. of 85 and 119 can be expressed in the form of $85x - 153$. Value of x is :

(1) 1

(2) 2

(3) 3

(4) 4

Correct Answer: (2) 2

Solution:

Step 1: Find the H.C.F. (Highest Common Factor) of 85 and 119 using the Euclidean Algorithm or prime factorization.

Method 1: Euclidean Algorithm

Divide 119 by 85: $119 = 85 \times 1 + 34$

Divide 85 by the remainder 34: $85 = 34 \times 2 + 17$

Divide 34 by the remainder 17: $34 = 17 \times 2 + 0$

The last non-zero remainder is 17. So, H.C.F. (85, 119) = 17.

Method 2: Prime Factorization

Prime factors of 85: 5×17

Prime factors of 119: 7×17

The common factor is 17.

So, H.C.F. (85, 119) = 17.

Step 2: Set up the given equation.

We are given that the H.C.F. can be expressed in the form $85x - 153$.

From Step 1, H.C.F. = 17.

So, we have the equation:

$$85x - 153 = 17$$

Step 3: Solve the equation for x .

Add 153 to both sides of the equation:

$$85x = 17 + 153$$

$$85x = 170$$

Divide both sides by 85:

$$x = \frac{170}{85}$$

$$x = 2$$

Step 4: Verify the answer (optional).

Substitute $x = 2$ back into the expression $85x - 153$:

$$85(2) - 153 = 170 - 153 = 17.$$

This matches the H.C.F., so the value of x is correct.

Step 5: Compare with the given options.

The calculated value of x is 2, which matches option (2).

(2) 2

Quick Tip

This problem combines finding the H.C.F. of two numbers with solving a linear equation. The Euclidean Algorithm is an efficient method for finding the H.C.F. of larger numbers.

42. If α and β are the zeros of the polynomial, such that $\alpha + \beta = 6$ and $\alpha\beta = 4$, then the quadratic polynomial is:

(1) $x^2 - x - 6$

(2) $x^2 + x - 6$

(3) $x^2 - 6x + 4$

(4) $x^2 - 6x + 4$

Correct Answer: (3) $x^2 - 6x + 4$

Solution:

Step 1: Use Vieta's Formulas.

For a quadratic polynomial:

$$P(x) = x^2 - (\text{sum of roots})x + (\text{product of roots}),$$

where the sum of the roots is $\alpha + \beta = 6$ and the product is $\alpha\beta = 4$.

Step 2: Substitute the values.

$$P(x) = x^2 - 6x + 4.$$

Step 3: Analyze the options.

Option (1): $x^2 - x - 6$ — Incorrect.

Option (2): $x^2 + x - 6$ — Incorrect.

Option (3): $x^2 - 6x + 4$ — Correct.

Option (4): $x^2 - 6x + 4$ — Correct.

Step 4: Final Answer.

$$x^2 - 6x + 4$$

Quick Tip

To construct a quadratic polynomial given the sum and product of its roots, use Vieta's formulas: $P(x) = x^2 - (\text{sum of roots})x + (\text{product of roots})$. This ensures the polynomial accurately reflects the given conditions.

43. The value of k for which the equations $6x - 2y = 3$ and $kx - y = 2$ have infinitely many solutions is:

- (1) -3
- (2) 3
- (3) No value
- (4) $\frac{3}{2}$

Correct Answer: (3) No value

Solution:

For a system of linear equations to have infinitely many solutions, the equations must represent the same line. This occurs when the ratios of their coefficients are equal:

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

Given the equations:

$$\begin{cases} 6x - 2y = 3 & (1) \\ kx - y = 2 & (2) \end{cases}$$

Compute the ratios:

$$\frac{6}{k} = \frac{-2}{-1} = \frac{3}{2}$$

Simplify the second ratio:

$$\frac{-2}{-1} = 2$$

Now, set the first ratio equal to 2:

$$\frac{6}{k} = 2 \implies k = \frac{6}{2} = 3$$

Check the third ratio:

$$\frac{3}{2} \neq 2$$

Since the ratios are not equal, there is **no value of** k that satisfies the condition for infinitely many solutions.

Final Answer

No value

Quick Tip

For two linear equations to have infinitely many solutions, their coefficients must be proportional. Ensure all ratios of corresponding coefficients are equal to confirm dependency.

44. If $x^2 - 5x + 1 = 0$, then $(x + \frac{1}{x})$ will be equal to :

- (1) 10
- (2) 8
- (3) 6
- (4) 5

Correct Answer: (4) 5

Solution:

Step 1: Start with the given equation.

We are given the equation: $x^2 - 5x + 1 = 0$

Step 2: Manipulate the equation to get terms involving $x + \frac{1}{x}$.

Since we are looking for $x + \frac{1}{x}$, we should try to divide the entire equation by x .

First, check that $x \neq 0$. If $x = 0$, then $0^2 - 5(0) + 1 = 0$, which simplifies to $1 = 0$, which is false. Therefore, $x \neq 0$, and we can safely divide by x .

Divide every term in the equation by x :

$$\frac{x^2}{x} - \frac{5x}{x} + \frac{1}{x} = \frac{0}{x}$$

$$x - 5 + \frac{1}{x} = 0$$

Step 3: Isolate the term $(x + \frac{1}{x})$.

Add 5 to both sides of the equation:

$$x + \frac{1}{x} = 5$$

Step 4: Conclude the result.

The value of $(x + \frac{1}{x})$ is 5.

Step 5: Compare with the given options.

The calculated value is 5, which matches option (4).

(4) 5

Quick Tip

This type of problem frequently appears in algebra. The key technique is to divide the quadratic equation by 'x' (assuming $x \neq 0$) to transform it into an expression involving

$$x + \frac{1}{x} \text{ or } x - \frac{1}{x}.$$

45. The sum of first 5 multiples of 3 is :

(1) 45

(2) 55

(3) 65

(4) 75

Correct Answer: (1) 45

Solution:

Step 1: Identify the first 5 multiples of 3.

The multiples of 3 are numbers that can be obtained by multiplying 3 by an integer.

The first 5 multiples of 3 are:

$$3 \times 1 = 3$$

$$3 \times 2 = 6$$

$$3 \times 3 = 9$$

$$3 \times 4 = 12$$

$$3 \times 5 = 15$$

So, the multiples are 3, 6, 9, 12, 15.

Step 2: Calculate the sum of these multiples.

$$\text{Sum} = 3 + 6 + 9 + 12 + 15$$

Method 1: Direct Summation

$$\text{Sum} = 3 + 6 + 9 + 12 + 15 = 45$$

Method 2: Using Arithmetic Progression (AP) formula

The multiples of 3 form an arithmetic progression with:

$$\text{First term } (a) = 3$$

$$\text{Common difference } (d) = 3$$

$$\text{Number of terms } (n) = 5$$

The sum of an arithmetic progression is given by the formula:

$$S_n = \frac{n}{2}(2a + (n - 1)d)$$

or

$$S_n = \frac{n}{2}(a + l), \text{ where } l \text{ is the last term.}$$

Using the first formula:

$$S_5 = \frac{5}{2}(2 \times 3 + (5 - 1) \times 3)$$

$$S_5 = \frac{5}{2}(6 + 4 \times 3)$$

$$S_5 = \frac{5}{2}(6 + 12)$$

$$S_5 = \frac{5}{2}(18)$$

$$S_5 = 5 \times 9$$

$$S_5 = 45$$

Using the second formula (where $l = 15$):

$$S_5 = \frac{5}{2}(3 + 15)$$

$$S_5 = \frac{5}{2}(18)$$

$$S_5 = 5 \times 9$$

$$S_5 = 45$$

Step 3: Conclude the result.

The sum of the first 5 multiples of 3 is 45.

Step 4: Compare with the given options.

The calculated sum is 45, which matches option (1).

(1) 45

Quick Tip

This problem can be solved by direct summation for a small number of terms. For a larger number of terms, it's more efficient to recognize that multiples of a number form an arithmetic progression and use the sum formula for an AP.

46. If $2k$, $3k-1$, 8 are in A.P. Then the value of k is :

- (1) $\frac{3}{2}$
- (2) $\frac{5}{2}$
- (3) $\frac{1}{2}$
- (4) $\frac{7}{2}$

Correct Answer: (2) $\frac{5}{2}$

Solution:

Step 1: Understand the property of an Arithmetic Progression (A.P.).

In an Arithmetic Progression, the difference between consecutive terms is constant. This constant difference is called the common difference. If a , b , and c are in A.P., then

$b - a = c - b$. This can be rearranged to $2b = a + c$.

Step 2: Apply the A.P. property to the given terms.

The given terms are $2k$, $3k - 1$, and 8 .

Let $a = 2k$

Let $b = 3k - 1$

Let $c = 8$

Using the property $2b = a + c$:

$$2(3k - 1) = 2k + 8$$

Step 3: Solve the equation for k .

Distribute the 2 on the left side:

$$6k - 2 = 2k + 8$$

Subtract $2k$ from both sides:

$$6k - 2k - 2 = 8$$

$$4k - 2 = 8$$

Add 2 to both sides:

$$4k = 8 + 2$$

$$4k = 10$$

Divide by 4:

$$k = \frac{10}{4}$$

$$k = \frac{5}{2}$$

Step 4: Verify the result.

If $k = 5/2$:

The terms are:

$$2k = 2(5/2) = 5$$

$$3k - 1 = 3(5/2) - 1 = 15/2 - 2/2 = 13/2 = 6.5$$

8

The sequence is 5, 6.5, 8.

The common difference is $6.5 - 5 = 1.5$ and $8 - 6.5 = 1.5$.

Since the common difference is constant, the terms are in A.P.

Step 5: Compare the result with the given options.

The calculated value of k is $\frac{5}{2}$, which matches option (2).

$$(2) \quad \frac{5}{2}$$

Quick Tip

For three terms a, b, c to be in Arithmetic Progression (A.P.), the middle term must be the average of the other two, i.e., $2b = a + c$, or equivalently, the common difference between consecutive terms must be equal: $b - a = c - b$.

47. What is the sum of first n natural numbers ?

$$(1) \quad \frac{n(n+3)}{2}$$

$$(2) \quad \frac{n(n+1)}{2}$$

$$(3) \quad \frac{n^2(n+1)}{2}$$

$$(4) \quad \frac{n(n^2+1)}{2}$$

Correct Answer: (2) $\frac{n(n+1)}{2}$

Solution:**Step 1: Understand what "natural numbers" mean.**

Natural numbers are positive integers starting from 1: $1, 2, 3, \dots$. The sum of the first n natural numbers means the sum $1 + 2 + 3 + \dots + n$.

Step 2: Recall the formula for the sum of an arithmetic series.

The sum of an arithmetic series can be found using the formula:

$$S_n = \frac{n}{2}(a_1 + a_n)$$

where:

S_n is the sum of the first n terms

n is the number of terms

a_1 is the first term

a_n is the last term

Step 3: Apply the formula to the sum of natural numbers.

In the case of the sum of the first n natural numbers:

$a_1 = 1$ (the first natural number)

$a_n = n$ (the n -th natural number)

$n = n$ (there are n terms)

Substitute these values into the formula:

$$S_n = \frac{n}{2}(1 + n)$$

$$S_n = \frac{n(n+1)}{2}$$

Step 4: Compare the result with the given options.

The derived formula is $\frac{n(n+1)}{2}$, which matches option (2).

(2) $\frac{n(n+1)}{2}$

Quick Tip

The formula for the sum of the first n natural numbers, $S_n = \frac{n(n+1)}{2}$, is a very common and useful result, often attributed to Carl Friedrich Gauss. It is derived from the properties of arithmetic progressions.

48. In a right triangle, the square of the hypotenuse is equal to the of the

square of the other two sides.

- (1) Product
- (2) Sum
- (3) Difference
- (4) Ratio

Correct Answer: (2) Sum

Solution:

Step 1: Understand the Pythagorean Theorem.

The Pythagorean theorem states that in a right triangle, the square of the length of the hypotenuse (c) is equal to the sum of the squares of the lengths of the other two sides (a and b). Mathematically, this is expressed as:

$$c^2 = a^2 + b^2.$$

Step 2: Analyze Each Option.

Let's evaluate each option based on the Pythagorean theorem:

1. Product:

Incorrect, as the theorem does not involve multiplying the squares of the sides.

2. Sum:

Correct, as the theorem explicitly states that the square of the hypotenuse is the sum of the squares of the other two sides.

3. Difference:

Incorrect, as the theorem does not involve subtracting the squares of the sides.

4. Ratio:

Incorrect, as the theorem does not involve dividing the squares of the sides.

Step 3: Final Answer.

(2) Sum

Quick Tip

The Pythagorean theorem is a fundamental property of right triangles. It states that the square of the hypotenuse is equal to the sum of the squares of the other two sides. This relationship is crucial for solving problems involving right triangles.

49. A ladder is placed against a wall such that its foot is at a distance of 2.5 m from the wall and its top reaches 6 m above the ground. Then the length of the ladder is:

- (1) 3.5 m
- (2) 4.5 m
- (3) 8.5 m
- (4) 6.5 m

Correct Answer: (4) 6.5 m

Solution:

Step 1: Visualize the Problem.

The ladder forms a right triangle with the wall and the ground. The distance from the foot of the ladder to the wall is 2.5 m, and the height reached by the ladder is 6 m. The length of the ladder is the hypotenuse.

Step 2: Apply the Pythagorean Theorem.

$$\text{Length}^2 = (2.5)^2 + 6^2 = 6.25 + 36 = 42.25.$$

Taking the square root:

$$\text{Length} = \sqrt{42.25} = 6.5 \text{ m.}$$

Step 3: Analyze the Options.

Option (1): 3.5 m — Incorrect.

Option (2): 4.5 m — Incorrect.

Option (3): 8.5 m — Incorrect.

Option (4): 6.5 m — Correct.

Step 4: Final Answer.

6.5 m

Quick Tip

When solving problems involving ladders leaning against walls, visualize the situation as a right triangle and apply the Pythagorean theorem. Ensure all measurements are correctly substituted into the formula to avoid errors.

50. If a line segment joining the points P and Q $(3, -4)$ is bisected at origin, then the coordinates of P are :

- (1) $(4, -3)$
- (2) $(2, 4)$
- (3) $(-3, 4)$
- (4) $(4, 3)$

Correct Answer: (3) $(-3, 4)$

Solution:

Step 1: Understand the given information and define coordinates.

Let the coordinates of point P be (x_1, y_1) .

Let the coordinates of point Q be $(x_2, y_2) = (3, -4)$.

The line segment PQ is bisected at the origin. This means the origin $(0, 0)$ is the midpoint of the line segment PQ.

Step 2: Recall the midpoint formula.

The midpoint M of a line segment joining two points (x_1, y_1) and (x_2, y_2) is given by the formula:

$$M = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Step 3: Apply the midpoint formula with the given information.

Here, the midpoint M is the origin $(0, 0)$.

So, we have:

$$(0, 0) = \left(\frac{x_1 + 3}{2}, \frac{y_1 + (-4)}{2} \right)$$

Step 4: Equate the x-coordinates and y-coordinates to find x_1 and y_1 .

For the x-coordinate:

$$\frac{x_1 + 3}{2} = 0$$

$$x_1 + 3 = 0 \times 2$$

$$x_1 + 3 = 0$$

$$x_1 = -3$$

For the y-coordinate:

$$\frac{y_1 - 4}{2} = 0$$

$$y_1 - 4 = 0 \times 2$$

$$y_1 - 4 = 0$$

$$y_1 = 4$$

Step 5: State the coordinates of P.

The coordinates of point P are $(-3, 4)$.

Step 6: Compare with the given options.

The calculated coordinates are $(-3, 4)$, which matches option (3).

(3) $(-3, 4)$

Quick Tip

When a line segment is bisected at a point, that point is the midpoint of the segment. The origin $(0, 0)$ acts as the midpoint here. Understanding the midpoint formula is crucial for solving this problem.

PHYSICS

51. Electric current produces :

- (1) Heating effect
- (2) Magnetic effect
- (3) Both 1 & 2
- (4) None of the above

Correct Answer: (3) Both 1 & 2

Solution:

Step 1: Analyze the effects of electric current.

Electric current is the flow of electric charge. When current flows through a conductor, it produces several effects.

Effect 1: Heating Effect of Electric Current (Joule Heating)

When electric current flows through a conductor, the moving electrons collide with the atoms or ions of the conductor. These collisions transfer kinetic energy to the atoms, causing them to vibrate more rapidly and leading to an increase in the temperature of the conductor. This phenomenon is known as the heating effect of electric current or Joule heating. Examples include electric heaters, incandescent light bulbs, and electric kettles.

Effect 2: Magnetic Effect of Electric Current

Danish physicist Hans Christian Ørsted discovered in 1820 that an electric current produces a magnetic field around the conductor. This means that a current-carrying wire behaves like a magnet and can deflect a compass needle. This effect is the basis for electromagnets, electric motors, generators, and many other electrical devices.

Step 3: Evaluate the options.

- (1) Heating effect: This is a well-known effect of electric current (Joule heating).
- (2) Magnetic effect: This is also a well-known effect of electric current (Ørsted's discovery).
- (3) Both 1 & 2: Since electric current produces both heating and magnetic effects, this option is correct.
- (4) None of the above: This is incorrect because both effects are produced.

Step 4: Conclude the answer.

Electric current produces both heating and magnetic effects.

(3) Both 1 & 2

Quick Tip

Electric current has several important effects. The heating effect (Joule heating) is due to the resistance of the conductor, while the magnetic effect (Ørsted's discovery) is fundamental to electromagnetism and the operation of motors and generators.

52. Which one is not true for magnetic field lines ?

- (1) They do not intersect each other.
- (2) Outside the magnet, they are from North pole to South pole.
- (3) Outside the magnet, they are from South pole to North pole.
- (4) They form closed loop.

Correct Answer: (3) Outside the magnet, they are from South pole to North pole.

Solution:

Step 1: Analyze property (1) - "They do not intersect each other."

Magnetic field lines never intersect each other. If they did, it would mean that at the point of intersection, the magnetic field would have two directions, which is impossible. So, statement (1) is true.

Step 2: Analyze property (2) - "Outside the magnet, they are from North pole to South pole."

Conventionally, the direction of magnetic field lines outside a magnet is taken from the North pole to the South pole. So, statement (2) is true.

Step 3: Analyze property (3) - "Outside the magnet, they are from South pole to North pole."

As established in Step 2, outside the magnet, the direction of magnetic field lines is from North pole to South pole. Therefore, the statement that they are from South pole to North pole outside the magnet is false. This statement is the one that is NOT true.

Step 4: Analyze property (4) - "They form closed loop."

Magnetic field lines form continuous closed loops. They emerge from the North pole and merge at the South pole outside the magnet, and inside the magnet, their direction is from the South pole to the North pole, thus forming closed loops. So, statement (4) is true.

Step 5: Identify the statement that is not true.

Based on the analysis, statement (3) is the one that is not true.

(3) Outside the magnet, they are from South pole to North pole.

Quick Tip

Remember the key properties of magnetic field lines: they never intersect, they originate from the North pole and terminate at the South pole outside the magnet, and they form continuous closed loops, extending from the South pole to the North pole inside the magnet.

53. At the time of short circuit, the current in the circuit is :

- (1) Reduces
- (2) Remains constant
- (3) Increases heavily
- (4) Vary continuously

Correct Answer: (3) Increases heavily

Solution:

Step 1: Understand what a short circuit is.

A short circuit occurs when there is a low-resistance connection between two conductors supplying electrical power to a circuit. This bypasses the normal load of the circuit.

Step 2: Apply Ohm's Law.

Ohm's Law states that current (I) is directly proportional to voltage (V) and inversely proportional to resistance (R), i.e., $I = V/R$.

Step 3: Analyze the effect of a short circuit on resistance.

In a short circuit, the resistance (R) of the path becomes very low, ideally close to zero.

Step 4: Determine the effect on current.

According to Ohm's Law, if the resistance (R) decreases significantly (approaches zero), and the voltage (V) remains relatively constant (from the power source), then the current (I) must increase heavily. A very low resistance leads to a very high current.

Step 5: Compare the conclusion with the given options.

When a short circuit occurs, the current in the circuit increases heavily. This matches option (3).

(3) Increases heavily

Quick Tip

A short circuit creates a path of very low resistance, leading to a sudden and very large increase in current flow. This surge in current can generate excessive heat, potentially causing damage to the circuit components, power supply, or even fires.

54. The device used for producing electric current is called:

- (1) Generator
- (2) Galvanometer
- (3) Ammeter
- (4) Motor

Correct Answer: (1) Generator

Solution:

Step 1: Understand Each Device.

Let's analyze each option to determine which device is used for producing electric current:

1. Generator:

A generator converts mechanical energy into electrical energy by rotating a coil in a magnetic field or moving a conductor through a magnetic field. This is the primary function of a generator.

2. Galvanometer:

A galvanometer is an instrument used to detect and measure small electric currents. It does not produce electric current but measures it.

3. Ammeter:

An ammeter is a device used to measure electric current. Like the galvanometer, it does not produce electric current but measures it.

4. Motor:

A motor converts electrical energy into mechanical energy. It consumes electric current rather than producing it.

Step 2: Analyze the Options.

Option (1): Generator — Correct, as generators are specifically designed to produce electric current.

Option (2): Galvanometer — Incorrect, as it measures current, not produces it.

Option (3): Ammeter — Incorrect, as it measures current, not produces it.

Option (4): Motor — Incorrect, as motors consume current, not produce it.

Step 3: Final Answer.

(1) Generator

Quick Tip

A generator is the device used to produce electric current by converting other forms of energy (such as mechanical or chemical energy) into electrical energy. Always remember that devices like galvanometers and ammeters measure current, while motors consume current.

55. The north and south poles of a magnet:

- (1) are of different strength
- (2) are of equal strength
- (3) can be separated by cutting the magnet
- (4) None of the above

Correct Answer: (2) are of equal strength

Solution:

Step 1: Understand Magnetic Poles.

In a bar magnet, there are two poles: the north pole and the south pole. These poles have the following properties:

1. Strength of Poles:

The north and south poles of a magnet are always of equal strength. This is a fundamental property of magnets, as they are dipolar in nature, meaning the total magnetic flux emerging from one pole must equal the flux entering the other pole.

2. Separation of Poles:

When a magnet is cut into pieces, each piece becomes a new magnet with its own north and south poles. The original poles cannot be separated; instead, new poles form at the cut surfaces.

Step 2: Analyze Each Option.

Option (1): are of different strength — Incorrect, as the poles are always of equal strength.

Option (2): are of equal strength — Correct, as this matches the fundamental property of magnets.

Option (3): can be separated by cutting the magnet — Incorrect, as cutting a magnet creates new poles rather than separating the original poles.

Option (4): None of the above — Incorrect, as Option (2) is correct.

Step 3: Final Answer.

(2) are of equal strength

Quick Tip

Magnetic poles always come in pairs (north and south), and their strengths are always equal. Cutting a magnet does not separate the original poles but creates new poles at the cut surfaces. Understanding these basic properties helps in solving problems related to magnets and their behavior.

56. Strength of magnetic field produced by a current carrying solenoid depends upon :

- (1) Number of turns
- (2) Current
- (3) Nature of core
- (4) All the above

Correct Answer: (4) All the above

Solution:

Step 1: Understand what a solenoid is and how it produces a magnetic field.

A solenoid is a long coil containing a large number of close turns of insulated copper wire. When an electric current flows through a solenoid, it produces a magnetic field similar to that of a bar magnet. The magnetic field lines inside a long straight solenoid are nearly uniform and parallel to the axis of the solenoid.

Step 2: Recall the factors affecting the strength of the magnetic field of a solenoid.

The strength of the magnetic field (B) inside a solenoid is given by the formula:

$$B = \mu n I$$

where:

B is the magnetic field strength.

μ is the magnetic permeability of the core material inside the solenoid.

n is the number of turns per unit length of the solenoid (i.e., $n = N/L$, where N is the total number of turns and L is the length of the solenoid).

I is the current flowing through the solenoid.

Let's analyze each factor mentioned in the options:

Factor 1: Number of turns (specifically, number of turns per unit length)

From the formula $B = \mu n I$, it is clear that B is directly proportional to n (number of turns per unit length). A higher number of turns (for a given length) means a stronger magnetic field. So, 'Number of turns' (implicitly, number of turns per unit length) affects the strength.

Factor 2: Current

From the formula $B = \mu n I$, it is clear that B is directly proportional to I (current). A larger current produces a stronger magnetic field. So, 'Current' affects the strength.

Factor 3: Nature of core

The term μ in the formula represents the magnetic permeability of the core material inserted inside the solenoid.

For a solenoid with an air core or vacuum, $\mu = \mu_0$ (permeability of free space).

If a soft iron core (a ferromagnetic material) is placed inside the solenoid, the magnetic permeability (μ) of the core material is much greater than μ_0 . This significantly increases the strength of the magnetic field produced. So, the 'Nature of core' affects the strength.

Step 3: Conclude based on the analysis.

Since the strength of the magnetic field produced by a current-carrying solenoid depends on the number of turns (per unit length), the current flowing through it, and the nature of the core material, all the listed factors influence the magnetic field strength.

Step 4: Compare with the given options.

Option (4) "All the above" correctly summarizes that the strength depends on all three factors.

(4) All the above

Quick Tip

The magnetic field of a solenoid is described by $B = \mu n I$. This formula directly shows that the strength of the magnetic field is dependent on the permeability of the core material (μ), the number of turns per unit length (n), and the current (I).

57. An electromagnet is :

- (1) A permanent magnet
- (2) A temporary magnet
- (3) Both 1 & 2
- (4) None of the above

Correct Answer: (2) A temporary magnet

Solution:

Step 1: Define what an electromagnet is.

An electromagnet is a type of magnet in which the magnetic field is produced by an electric current. It typically consists of a coil of wire wrapped around a core of ferromagnetic material (like soft iron).

Step 2: Understand the characteristics of an electromagnet.

The key characteristic of an electromagnet is that its magnetism is temporary and can be controlled.

It acts as a magnet only when current flows through its coil.

When the current is switched off, the core material loses most or all of its magnetism (depending on the core material and its retentivity).

The strength and polarity of an electromagnet can be varied by changing the current, the number of turns in the coil, or by reversing the direction of the current.

Step 3: Differentiate between permanent and temporary magnets.

- **Permanent magnets** are materials that retain their magnetic properties even after the external magnetizing field is removed. Examples include magnets made from steel or alloys like Alnico.
- **Temporary magnets** are materials that behave as magnets only when they are under the influence of an external magnetic field (like an electromagnet) or when an electric current is flowing through them. They lose their magnetism once the external influence is removed.

Step 4: Conclude based on the characteristics.

Since an electromagnet's magnetic field can be turned on or off by controlling the current, it fits the definition of a temporary magnet. It does not retain its magnetism permanently.

Step 5: Compare with the given options.

Option (2) "A temporary magnet" is the correct classification for an electromagnet.

(2) A temporary magnet

Quick Tip

The defining feature of an electromagnet is its controllable magnetism. It can be turned 'on' and 'off', and its strength can be adjusted. This makes it a temporary magnet, unlike permanent magnets which retain their magnetism.

58. A mirror forms a virtual and diminished image. It is a :

- (1) Convex mirror
- (2) Plane mirror
- (3) Concave mirror
- (4) None of the above

Correct Answer: (1) Convex mirror

Solution:

Step 1: Analyze image formation by a Plane Mirror.

A plane mirror always forms a virtual, erect (upright), and same-sized image as the object. It does not form a diminished image.

Step 2: Analyze image formation by a Concave Mirror.

A concave mirror can form both real and virtual images, and these can be magnified, diminished, or same-sized depending on the object's position. However, when it forms a virtual image, that image is always erect and magnified, not diminished.

Step 3: Analyze image formation by a Convex Mirror.

A convex mirror always forms a virtual, erect (upright), and diminished image, regardless of the object's position. This is a characteristic property of convex mirrors.

Step 4: Compare with the given properties.

The problem states that the mirror forms a virtual and diminished image. Based on the analysis, only a convex mirror consistently forms a virtual and diminished image.

(1) Convex mirror

Quick Tip

Remember the key image properties for different types of mirrors:

- **Plane Mirror:** Virtual, erect, same size.
- **Concave Mirror:** Can be real/virtual, inverted/erect, magnified/diminished/same size. Virtual image is always magnified.
- **Convex Mirror:** Always forms virtual, erect, and diminished image.

59. Focal length of a plane mirror is :

- (1) Infinite
- (2) Zero
- (3) 1 m
- (4) 5 cm

Correct Answer: (1) Infinite

Solution:

Step 1: Understand the concept of focal length.

The focal length of a mirror is the distance from the mirror's pole to its principal focus. For spherical mirrors, it is half of the radius of curvature ($f = R/2$).

Step 2: Consider the curvature of a plane mirror.

A plane mirror can be considered as a part of a spherical mirror with an infinitely large radius of curvature. In other words, its reflecting surface is flat, which implies it has no curvature, or equivalently, an infinite radius of curvature.

Step 3: Determine the focal length based on curvature.

Since a plane mirror has an infinite radius of curvature ($R = \infty$), its focal length ($f = R/2$) will also be infinite ($f = \infty/2 = \infty$).

Parallel rays of light incident on a plane mirror continue to be parallel after reflection, or appear to diverge from a point at infinity behind the mirror, hence the infinite focal length.

Step 4: Compare the conclusion with the given options.

The focal length of a plane mirror is infinite. This matches option (1).

(1) Infinite

Quick Tip

A plane mirror can be thought of as a spherical mirror with an infinitely large radius of curvature. Consequently, its focal length, which is half of the radius of curvature, is also infinite. This is why parallel light rays reflecting off a plane mirror remain parallel.

60. A convex lens forms the image of sun at :

- (1) Focus
- (2) Centre of curvature
- (3) Between focus and centre of curvature
- (4) No image is formed

Correct Answer: (1) Focus

Solution:

Step 1: Understand the nature of light rays from the Sun.

The Sun is an extremely distant object. For practical purposes in optics, light rays coming from a very distant object are considered to be parallel to the principal axis when they reach a lens or mirror.

Step 2: Recall the properties of a convex lens for parallel rays.

A convex lens is a converging lens. When parallel rays of light (like those from the Sun) incident on a convex lens, after refraction through the lens, they converge at a single point on the principal axis. This point is known as the principal focus (or focal point) of the lens.

Step 3: Determine the image location.

Since the parallel rays from the Sun converge at the principal focus after passing through the convex lens, the image of the Sun is formed at the focus. This image is real, inverted, and highly diminished (a point-like image).

Step 4: Compare the conclusion with the given options.

The image of the Sun formed by a convex lens is at its focus. This matches option (1).

(1) Focus

Quick Tip

For any lens or mirror, light rays coming from an object at infinity (like the Sun) are considered parallel. These parallel rays, after refraction/reflection, converge at the focal point of the lens/mirror.

61. Speed of light in vacuum is:

- (1) 8×10^3 m/s
- (2) 8×10^6 m/s
- (3) 3×10^6 m/s
- (4) 3×10^8 m/s

Correct Answer: (4) 3×10^8 m/s

Solution:

Step 1: Understand the Speed of Light in Vacuum.

The speed of light in vacuum is denoted by c and is approximately:

$$c = 3 \times 10^8 \text{ m/s.}$$

Step 2: Analyze Each Option.

Option 1: 8×10^3 m/s — Incorrect, much smaller than c .

Option 2: 8×10^6 m/s — Incorrect, still smaller than c .

Option 3: 3×10^6 m/s — Incorrect, too small by two orders of magnitude.

Option 4: 3×10^8 m/s — Correct, matches the speed of light.

Step 3: Final Answer.

$3 \times 10^8 \text{ m/s}$

Quick Tip

The speed of light in a vacuum is a fundamental constant in physics, denoted by c , and its value is approximately 3×10^8 m/s. This value is crucial in many areas of physics, including optics, relativity, and electromagnetism.

62. The cause of twinkling of stars is:

- (1) Dispersion
- (2) Scattering
- (3) Atmospheric refraction
- (4) Reflection

Correct Answer: (3) Atmospheric refraction

Solution:

Step 1: Understand Twinkling of Stars.

Twinkling, or scintillation, is the apparent fluctuation in the brightness and position of stars when viewed from Earth. This phenomenon occurs due to the bending of light as it passes through Earth's atmosphere. The key factors involved are:

1. Dispersion:

Dispersion refers to the splitting of light into its component colors due to differences in refractive indices. While dispersion affects the color of light, it is not the primary cause of twinkling.

2. Scattering: - Scattering occurs when light interacts with particles in the atmosphere, causing it to spread out in different directions. While scattering can affect the overall brightness of stars, it is not the main cause of twinkling.

3. Atmospheric Refraction:

Atmospheric refraction is the bending of light as it passes through Earth's atmosphere. The density of the atmosphere varies with altitude, causing light from stars to bend as it travels through different layers. This bending causes the starlight to appear to "twinkle" because the path of light changes slightly due to turbulence in the atmosphere.

4. Reflection:

Reflection involves light bouncing off surfaces. While reflection can occur in certain

atmospheric conditions, it is not the primary cause of twinkling.

Step 2: Analyze Each Option.

Option (1): Dispersion — Incorrect, as dispersion does not directly cause twinkling.

Option (2): Scattering — Incorrect, as scattering is not the primary cause of twinkling.

Option (3): Atmospheric refraction — Correct, as this is the primary cause of twinkling.

Option (4): Reflection — Incorrect, as reflection is not the primary cause of twinkling.

Step 3: Final Answer.

(3) Atmospheric refraction

Quick Tip

Twinkling of stars is primarily caused by atmospheric refraction, which bends light as it passes through Earth's atmosphere. The varying density of the atmosphere causes the light path to change, leading to fluctuations in the star's apparent brightness and position.

63. Blue colour of sky is due to :

- (1) Reflection
- (2) Scattering
- (3) Dispersion
- (4) Refraction

Correct Answer: (2) Scattering

Solution:

Step 1: Understand the phenomenon of light interaction with the atmosphere.

The Earth's atmosphere consists of various gases (like nitrogen, oxygen) and tiny suspended particles. Sunlight, which is white light, is composed of different colours (wavelengths) of electromagnetic radiation.

Step 2: Analyze the given options in the context of light interaction.

- **Reflection:** This is the bouncing back of light when it strikes a surface. While reflection occurs, it doesn't primarily explain the blue color of the sky.
- **Scattering:** This is the phenomenon where light rays are deflected in various directions

as they pass through a medium containing small particles or inhomogeneities. Rayleigh scattering is particularly relevant here.

- **Dispersion:** This is the splitting of white light into its constituent colours when it passes through a medium (like a prism) due to different wavelengths having different speeds. This is responsible for rainbows, not the general blue color of the sky.
- **Refraction:** This is the bending of light as it passes from one medium to another (e.g., from air to water). While refraction occurs in the atmosphere, it's not the primary reason for the sky's blue color.

Step 3: Explain why scattering leads to the blue sky.

The blue color of the sky is primarily due to the scattering of sunlight by the gases and tiny particles in Earth's atmosphere. This phenomenon is known as Rayleigh scattering.

Rayleigh scattering states that the amount of scattering of light is inversely proportional to the fourth power of its wavelength ($\text{Scattering} \propto \frac{1}{\lambda^4}$).

Blue light has a shorter wavelength compared to red light (and other colours at the red end of the spectrum).

Because blue light has a shorter wavelength, it is scattered much more effectively by the small particles in the atmosphere than longer wavelengths like red or yellow light.

When sunlight enters the atmosphere, the blue light is scattered in all directions. This scattered blue light reaches our eyes from all parts of the sky, making the sky appear blue.

At sunrise and sunset, when the sun is low on the horizon, the sunlight has to travel a greater distance through the atmosphere. Most of the blue light is scattered away, allowing the longer wavelength red and orange light to reach our eyes, which is why the sky appears reddish or orange.

Step 4: Conclude the correct option.

The blue colour of the sky is due to scattering.

(2) Scattering

Quick Tip

The blue color of the sky is a classic example of Rayleigh scattering, where shorter wavelengths (like blue) are scattered more efficiently by atmospheric particles than longer wavelengths (like red).

64. Myopia is corrected by using :

- (1) Concave lens
- (2) Convex lens
- (3) Cylindrical lens
- (4) Any lens

Correct Answer: (1) Concave lens

Solution:

Step 1: Understand what Myopia is.

Myopia, also known as nearsightedness, is a common vision condition where a person can see close objects clearly, but objects farther away appear blurry.

In a myopic eye, the eyeball is either too long, or the cornea is too steeply curved. This causes light rays from distant objects to focus in front of the retina, instead of directly on the retina.

Step 2: Determine the type of lens needed to correct Myopia.

To correct myopia, the light rays from distant objects need to be diverged slightly before they enter the eye, so that they can then focus directly on the retina.

A diverging lens is required for this purpose.

Step 3: Identify which type of lens is a diverging lens.

- **Concave lens:** A concave lens is a diverging lens. It is thinner in the middle and thicker at the edges. It causes parallel rays of light to diverge (spread out) after passing through it.
- **Convex lens:** A convex lens is a converging lens. It is thicker in the middle and thinner at the edges. It causes parallel rays of light to converge (come together) after passing through it. Convex lenses are used to correct hypermetropia (farsightedness).

- **Cylindrical lens:** A cylindrical lens is used to correct astigmatism, a condition where the eye's cornea or lens has an irregular curvature.
- **Any lens:** This is incorrect, as the specific type of vision defect requires a specific type of corrective lens.

Step 4: Conclude the correct corrective lens.

Since a concave lens is a diverging lens and is used to spread out light rays before they enter the myopic eye, it is used to correct myopia.

Step 5: Compare with the given options.

The correct option is (1) Concave lens.

(1) Concave lens

Quick Tip

Myopia (nearsightedness) causes light to focus in front of the retina. To push the focal point back onto the retina, a diverging lens is needed. Concave lenses are diverging lenses, making them the correct choice for myopia correction.

65. For which colour of light, the angle of deviation by a prism is maximum ?

- (1) Red
- (2) Yellow
- (3) Blue
- (4) Violet

Correct Answer: (4) Violet

Solution:

Step 1: Understand the phenomenon of dispersion of light by a prism.

When white light passes through a prism, it splits into its constituent colours (VIBGYOR - Violet, Indigo, Blue, Green, Yellow, Orange, Red). This phenomenon is called dispersion. The extent to which a colour of light bends (deviates) depends on its wavelength and the refractive index of the prism material for that specific wavelength.

Step 2: Relate angle of deviation to wavelength and refractive index.

The angle of deviation is inversely proportional to the wavelength of light. Colours with

shorter wavelengths deviate more. The refractive index of a material is generally higher for shorter wavelengths.

Step 3: Compare wavelengths of different colours.

In the visible spectrum (VIBGYOR), violet light has the shortest wavelength, and red light has the longest wavelength.

Step 4: Determine which colour deviates the most.

Since violet light has the shortest wavelength among the visible colours, it experiences the maximum deviation when passing through a prism. Conversely, red light, having the longest wavelength, deviates the least.

Step 5: Compare the conclusion with the given options.

Among the given options, Violet light will have the maximum angle of deviation.

(4) Violet

Quick Tip

Remember the acronym VIBGYOR for the order of colours in the visible spectrum. Violet has the shortest wavelength and deviates the most, while Red has the longest wavelength and deviates the least when passing through a prism.

66. What does the odometer of vehicle measure?

- (1) Speed
- (2) Distance
- (3) Acceleration
- (4) Velocity

Correct Answer: (2) Distance

Solution:

Step 1: Understand the function of an odometer.

An odometer is an instrument used to measure the distance traveled by a vehicle. It typically records the total cumulative distance from the time the vehicle was manufactured or reset.

Step 2: Differentiate from other measurements.

- **Speed** is measured by a speedometer, which indicates how fast the vehicle is moving at a particular instant.
- **Acceleration** is the rate of change of velocity, which is not directly measured by a standard odometer.
- **Velocity** is speed in a given direction, also not directly measured by an odometer.

Step 3: Conclude the primary measurement of an odometer.

The primary and sole function of an odometer is to measure the total distance covered by the vehicle.

Step 4: Compare the conclusion with the given options.

The odometer of a vehicle measures distance.

(2) Distance

Quick Tip

An odometer measures the total distance covered, while a speedometer measures instantaneous speed. Don't confuse the two!

67. An object travels 25 m in 5 s and then travels 25 m in 3 s. What is the average speed of the object?

- (1) 4.25 m/s^{-1}
- (2) 5.25 m/s^{-1}
- (3) 6.25 m/s^{-1}
- (4) 5.33 m/s^{-1}

Correct Answer: (3) 6.25 m/s^{-1}

Solution: Average speed is calculated as the **total distance traveled** divided by the **total time taken**.

Given:

$$\text{Distance}_1 = 25 \text{ m}, \quad \text{Time}_1 = 5 \text{ s}$$

$$\text{Distance}_2 = 25 \text{ m}, \quad \text{Time}_2 = 3 \text{ s}$$

1. Total Distance:

$$25 \text{ m} + 25 \text{ m} = 50 \text{ m}$$

2. Total Time:

$$5 \text{ s} + 3 \text{ s} = 8 \text{ s}$$

3. Average Speed:

$$\text{Average Speed} = \frac{\text{Total Distance}}{\text{Total Time}} = \frac{50 \text{ m}}{8 \text{ s}} = 6.25 \text{ m/s}$$

Final Answer

$$\boxed{6.25 \text{ m/s}}$$

Quick Tip

To find the average speed, always divide the total distance by the total time. Keep in mind that the total time and distance are independent of how the object moves during each part of the journey.

68. A train is moving at a constant speed of 54 km/h. What is the speed of the train in m/s?

- (1) 5 m/s^{-1}
- (2) 15 m/s^{-1}
- (3) 25 m/s^{-1}
- (4) 35 m/s^{-1}

Correct Answer: (2) 15 m/s^{-1}

Solution:

To convert the speed from km/h to m/s, we use the following relation:

$$1 \text{ km/h} = \frac{1000 \text{ m}}{3600 \text{ s}} = \frac{5}{18} \text{ m/s}.$$

Convert 54 km/h to m/s.

Now, to convert the speed of the train from kilometers per hour to meters per second, we multiply the speed in km/h by $\frac{5}{18}$:

$$\text{Speed in m/s} = 54 \text{ km/h} \times \frac{5}{18}.$$

$$\text{Speed in m/s} = \frac{54 \times 5}{18} = 15 \text{ m/s}.$$

Thus, the speed of the train in m/s is 15 m/s.

Quick Tip

To convert from km/h to m/s, multiply by $\frac{5}{18}$. This will give you the equivalent speed in meters per second.

69. What is the 'SI' unit of acceleration ?

- (1) KMSec^{-1}
- (2) KM/Sec^{-1}
- (3) MS^{-1}
- (4) MS^{-2}

Correct Answer: (4) MS^{-2}

Solution:

Step 1: Define acceleration.

Acceleration is the rate of change of velocity with respect to time. Velocity is a vector quantity representing the rate of change of position, and it has units of length per unit time.

Step 2: Determine the SI units of length and time.

In the International System of Units (SI), the base unit for length is the meter (m), and the base unit for time is the second (s).

Step 3: Determine the SI unit of velocity.

Velocity is displacement divided by time. So, the SI unit of velocity is meters per second (m/s), or MS^{-1} .

Step 4: Determine the SI unit of acceleration.

Acceleration is change in velocity divided by time. Therefore, the SI unit of acceleration is the unit of velocity divided by the unit of time:

$$\frac{\text{m/s}}{\text{s}} = \frac{\text{m}}{\text{s}^2}$$

This can also be written as MS^{-2} .

Step 5: Compare with the given options.

(1) KMSec^{-1} : Kilometers per second, which is a unit of speed or velocity, not acceleration.

(2) KM/Sec^{-1} : Kilometers per second, same as (1).

(3) MS^{-1} : Meters per second, which is the unit of speed or velocity.

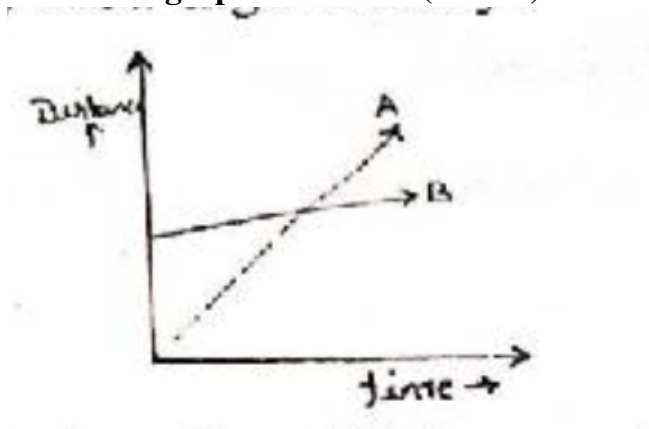
(4) MS^{-2} : Meters per second squared, which is the correct SI unit for acceleration.

(4) MS^{-2}

Quick Tip

Remember the definitions: Speed is distance/time, velocity is displacement/time, and acceleration is change in velocity/time. This helps in deriving their respective units.

70. In this graph which line (A or B) show high velocity :



(1) A line

(2) B-line

(3) Both are same

(4) None of these

Correct Answer: (1) A line

Solution:

Step 1: Understand a Distance-Time graph.

A distance-time graph plots the distance traveled by an object against time. The slope (gradient) of a distance-time graph represents the speed or velocity of the object.

Step 2: Relate slope to velocity.

A steeper slope indicates a greater change in distance over a given time interval, which means a higher speed or velocity. A less steep slope indicates a lower speed or velocity.

Step 3: Analyze the slopes of line A and line B from the provided graph.

Visually inspecting the graph, line A is steeper than line B. This means that for the same amount of time, line A covers more distance than line B.

Step 4: Compare the velocities of line A and line B.

Since line A has a steeper slope than line B, line A represents a higher velocity compared to line B.

Step 5: Conclude the result.

Line A shows high velocity.

Step 6: Compare with the given options.

The result matches option (1).

(1) A line

Quick Tip

On a distance-time graph, the steeper the line, the faster the object is moving. If the line is flat (zero slope), the object is stationary.

71. An object mass is 'M' and Velocity is 'V'. What is the momentum of the object :

- (1) $2 MV$
- (2) MV
- (3) MV^2
- (4) $\frac{1}{2}MV^2$

Correct Answer: (2) MV

Solution:

Step 1: Define momentum.

Momentum is a fundamental concept in physics that describes the quantity of motion an

object has. It is a vector quantity, meaning it has both magnitude and direction.

Step 2: State the formula for momentum.

The momentum (p) of an object is defined as the product of its mass (m) and its velocity (v).

The formula is: $p = m \times v$.

Step 3: Apply the given variables to the formula.

In this problem, the mass of the object is given as 'M' and its velocity is 'V'.

Substituting these into the momentum formula:

$$\text{Momentum} = M \times V$$

$$\text{Momentum} = MV$$

Step 4: Compare the result with the given options.

The calculated momentum is MV, which matches option (2).

(2) MV

Quick Tip

Remember the definition of momentum as the product of mass and velocity ($p = mv$). This is a core concept in classical mechanics, often used in conservation laws.

72. When we beat a carpet by stick the dust particles come out. Which law of motion works here ?

- (1) First law of Motion
- (2) Second law of Motion
- (3) Third law of Motion
- (4) None of these

Correct Answer: (1) First law of Motion

Solution:

Step 1: Understand Newton's First Law of Motion.

Newton's First Law of Motion, also known as the Law of Inertia, states that an object at rest will stay at rest, and an object in motion will stay in motion with the same speed and in the same direction unless acted upon by an unbalanced force.

Step 2: Analyze the scenario of beating a carpet.

Initially, both the carpet and the dust particles on it are at rest. When the carpet is beaten with a stick, a force is applied to the carpet, causing it to move suddenly.

However, the dust particles, due to their inertia (tendency to resist changes in their state of motion), tend to remain at rest.

Step 3: Relate the scenario to the Law of Inertia.

Because the carpet moves away quickly while the dust particles try to maintain their state of rest, the dust particles detach from the carpet and fall out. This phenomenon is a direct demonstration of inertia, which is explained by Newton's First Law of Motion.

Step 4: Consider other laws of motion (briefly).

- **Newton's Second Law of Motion** relates force, mass, and acceleration ($F = ma$). While force and acceleration are involved, the primary reason for the dust falling out is the inertia of the dust.
- **Newton's Third Law of Motion** states that for every action, there is an equal and opposite reaction. While there are action-reaction pairs when the stick hits the carpet, this law doesn't directly explain why the dust detaches due to the carpet's movement.

Step 5: Conclude the relevant law.

The phenomenon of dust particles coming out when a carpet is beaten is best explained by Newton's First Law of Motion (Law of Inertia).

(1) First law of Motion**Quick Tip**

Newton's First Law of Motion explains why passengers lurch forward when a car suddenly stops (their bodies tend to continue moving) and why dust falls off a carpet when it's shaken (the dust tends to remain at rest while the carpet moves).

73. An object has a mass of 120 kg on Earth. What is the mass of the object on the Moon?

(1) 60 kg

(2) 120 kg

(3) 20 kg

(4) 10 kg

Correct Answer: (2) 120 kg

Solution:

Step 1: Understand Mass and Weight.

Mass is a measure of the amount of matter in an object and remains constant regardless of location.

Weight is the force exerted on an object due to gravity and depends on the gravitational acceleration at the location.

The mass of an object does not change when it is moved from one location to another, such as from Earth to the Moon. Therefore, the mass of the object on the Moon is the same as its mass on Earth.

Step 2: Analyze the Options.

Option (1): 60 kg — Incorrect, as mass does not change with location.

Option (2): 120 kg — Correct, as the mass remains the same.

Option (3): 20 kg — Incorrect, as mass does not change with location.

Option (4): 10 kg — Incorrect, as mass does not change with location.

Step 3: Final Answer.

(2) 120 kg

Quick Tip

Mass is an intrinsic property of an object and does not change with location. Weight, however, depends on the gravitational acceleration at the location. Always remember that mass is constant, while weight varies with gravity.

74. If we apply 10 N of force on an object, then the acceleration produced is 2.5 m/s^2 .

What is the mass of the object?

(1) 4 kg

(2) 8 kg

(3) 12 kg

(4) 16 kg

Correct Answer: (2) 4 kg

Solution:

Step 1: Recall Newton's Second Law of Motion.

Newton's second law states:

$$F = ma$$

where: F is the net force applied on the object (in newtons),

m is the mass of the object (in kilograms),

a is the acceleration produced (in m/s^2).

Step 2: Rearranging the equation to find mass.

$$m = \frac{F}{a}$$

Step 3: Substitute the given values.

$$F = 10 \text{ N}, \quad a = 2.5 \text{ m/s}^2$$

$$m = \frac{10}{2.5} = 4 \text{ kg}$$

Final Answer: The mass of the object is 4 kg.

Quick Tip

Always use Newton's second law, $F = ma$, to relate force, mass, and acceleration. Ensure you substitute the given values correctly before solving for the unknown variable.

75. If we walk on Ice its not easy for us why?

(1) Low friction

(2) High friction

(3) Zero friction

(4) None of these

Correct Answer: (1) Low friction

Solution:

Step 1: Understand the concept of friction in walking.

When we walk, we push backwards on the ground, and the ground, in turn, pushes us forwards with an equal and opposite force (Newton's Third Law of Motion). This forward push from the ground is due to friction between our shoes and the walking surface. Friction is essential for us to gain a grip and propel ourselves forward.

Step 2: Consider walking on ice.

Ice is known for being a very slippery surface. This slipperiness is a direct result of low friction between our shoes and the ice.

Step 3: Evaluate the given options.

- **(1) Low friction:** When the friction between our shoes and the ice is low, there isn't enough opposing force for us to push against. This makes it difficult to get a grip, resulting in slipping and making it hard to walk. This aligns with the understanding of friction and walking.
- **(2) High friction:** High friction would make it easier to walk, as it would provide a strong grip. This contradicts the experience of walking on ice.
- **(3) Zero friction:** While friction on ice is very low, it's generally not exactly zero. Even a tiny amount of friction exists. However, "low friction" is the more accurate and practical explanation for the difficulty. If it were truly zero, it would be impossible to initiate or stop motion.
- **(4) None of these:** Since "Low friction" is a direct and accurate explanation, this option is incorrect.

Step 4: Conclude the reason for difficulty in walking on ice.

Walking on ice is difficult because of the low friction between our shoes and the ice surface.

(1) Low friction

Quick Tip

Friction is a force that opposes motion. It's necessary for walking because it provides the grip needed to push off the ground. On slippery surfaces like ice, friction is very low, making it difficult to walk without slipping.

76. A naughty boy hit a mango tree by stone then a mango fall down. Why the mango fall down :

- (1) Due to gravetional force of earth
- (2) Due to friction
- (3) Due to acceleration
- (4) None of these

Correct Answer: (1) Due to gravitational force of earth

Solution:

Step 1: Analyze the event described.

A boy hits a mango tree with a stone, and a mango falls down. We need to identify the fundamental force or principle responsible for the mango's downward motion.

Step 2: Evaluate the given options.

- **(1) Due to gravitational force of earth:** The Earth exerts a gravitational force on all objects with mass, pulling them towards its center. This force is commonly referred to as gravity. When an object is no longer supported (like a mango detached from a tree), gravity is the force that causes it to fall downwards.
- **(2) Due to friction:** Friction is a force that opposes motion between surfaces in contact. While air resistance (a type of friction) might affect the mango's fall by slowing it down, it is not the cause of the fall itself.
- **(3) Due to acceleration:** Acceleration is the rate of change of velocity. The mango *accelerates* downwards due to gravity, but acceleration is an effect of the force, not the cause of the fall itself. The cause of the acceleration is the gravitational force.
- **(4) None of these:** This option would be correct only if none of the other options explained the phenomenon.

Step 3: Conclude the primary reason for the mango falling.

The primary reason the mango falls down once it's dislodged from the tree is the Earth's gravitational pull.

Step 4: Compare with the given options.

The phenomenon is explained by the gravitational force of the Earth.

(1) Due to gravitational force of earth

Quick Tip

Any object released near the Earth's surface falls downwards due to the Earth's gravitational force. This is a fundamental concept in physics.

77. Universal Law of gravitation is :

(1) $F = G \frac{Mm}{d^2}$

(2) $F = G \frac{m_1 m_2}{d^2}$

(3) $F = mg$

(4) 1 and 2 both

Correct Answer: (4) 1 and 2 both

Solution: Step 1: Recall Newton's Universal Law of Gravitation.

Newton's Universal Law of Gravitation states that every particle attracts every other particle in the universe with a force that is directly proportional to the product of their masses and inversely proportional to the square of the distance between their centers.

Step 2: Express the law mathematically.

The mathematical formula for this law is typically written as: $F = G \frac{m_1 m_2}{r^2}$ or $F = G \frac{m_1 m_2}{d^2}$ where:

- F is the gravitational force between the two objects.
- G is the gravitational constant.
- m_1 and m_2 are the masses of the two objects.
- r or d is the distance between the centers of the two objects.

Step 3: Analyze the given options.

- Option (1) is $F = G \frac{Mm}{d^2}$. This formula uses M and m to represent the two masses, which is a common notation. So, this is a valid representation of the Universal Law of Gravitation.
- Option (2) is $F = G \frac{m_1 m_2}{d^2}$. This formula uses m_1 and m_2 to represent the two masses,

which is also a common notation. So, this is a valid representation of the Universal Law of Gravitation.

- Option (3) is $F = mg$. This formula represents the weight of an object (the force of gravity on an object near a planet's surface), where g is the acceleration due to gravity. This is a specific case derived from the Universal Law of Gravitation, but it is not the Universal Law itself.

Step 4: Conclude which options are correct.

Both options (1) and (2) correctly represent the Universal Law of Gravitation, just using different variable names for the masses. Therefore, the correct answer is that both 1 and 2 are true.

(4) 1 and 2 both

Quick Tip

Newton's Universal Law of Gravitation describes the attractive force between any two masses. The key is the product of the two masses and the inverse square of the distance between them, multiplied by the gravitational constant G . Different symbols for mass (e.g., M , m or m_1 , m_2) are equally valid.

78. 1 KWh is equal to :

- (1) 3.6×10^6 J
- (2) 3.6×10^9 J
- (3) 3.6×10^{12} J
- (4) 3.6×10^7 J

Correct Answer: (1) 3.6×10^6 J

Solution: Step 1: Understand the units involved.

- **KWh (Kilowatt-hour)** is a unit of energy. It is commonly used to measure electrical energy consumption.
- **J (Joule)** is the standard international (SI) unit of energy.

Step 2: Break down KWh into fundamental units. 1 KWh means 1 kilowatt operating for 1 hour.

- 1 kilowatt (KW) = 1000 watts (W)
- 1 hour (h) = 60 minutes \times 60 seconds = 3600 seconds (s)

The relationship between power, energy, and time is: Energy = Power \times Time. So, 1 KWh = 1 KW \times 1 h.

Step 3: Convert KWh to Joules.

Substitute the values from Step 2:

$$1 \text{ KWh} = 1000 \text{ W} \times 3600 \text{ s}$$

Recall that 1 Watt (W) = 1 Joule per second (J/s).

$$\text{So, } 1 \text{ KWh} = 1000 \text{ (J/s)} \times 3600 \text{ s}$$

$$1 \text{ KWh} = 3,600,000 \text{ J}$$

Step 4: Express the result in scientific notation.

3,600,000 J can be written as $3.6 \times 10^6 \text{ J}$.

Step 5: Compare the result with the given options.

The calculated value $3.6 \times 10^6 \text{ J}$ matches option (1).

$$(1) \quad 3.6 \times 10^6 \text{ J}$$

Quick Tip

Remember that 1 kilowatt-hour (KWh) is a unit of energy, and it represents the energy consumed by a device with a power of 1 kilowatt operating for one hour. The conversion to Joules involves multiplying kilowatts by 1000 (to get watts) and hours by 3600 (to get seconds), since 1 Watt = 1 Joule/second.

79. Sound can move in:

- (1) Solid
- (2) Liquid
- (3) Vacuum
- (4) 1 and 2 both

Correct Answer: (4) 1 and 2 both

Solution:

Step 1: Understand the Nature of Sound Waves.

Sound is a mechanical wave that requires a medium to propagate. It can travel through:

1. Solids:

Sound travels fastest in solids due to their high density and strong intermolecular forces.

2. Liquids:

Sound travels slower in liquids compared to solids but faster than in gases due to the intermediate density and molecular interactions.

3. Vacuum:

Sound cannot travel through a vacuum because there are no particles to transmit the wave. A vacuum lacks the medium necessary for sound propagation.

Step 2: Analyze Each Option.

Option (1): Solid — Incorrect, as sound can also travel through liquids.

Option (2): Liquid — Incorrect, as sound can also travel through solids.

Option (3): Vacuum — Incorrect, as sound cannot travel through a vacuum.

Option (4): 1 and 2 both — Correct, as sound can travel through both solids and liquids.

Step 3: Final Answer.

(4) 1 and 2 both

Quick Tip

Sound waves require a medium to propagate. They can travel through solids and liquids but not through a vacuum. The speed of sound depends on the properties of the medium, such as density and elasticity.

80. What is the relation between sound velocity (V), frequency (γ), and wavelength (λ)?

(1) $V = \gamma\lambda$

(2) $\gamma = \frac{V}{\lambda}$

(3) $\lambda = \frac{V}{\gamma}$

(4) All of these

Correct Answer: (4) All of these

Solution:

Step 1: Recall the Relationship Between Velocity, Frequency, and Wavelength.

The relationship between the velocity (V), frequency (γ), and wavelength (λ) of a wave is given by:

$$V = \gamma\lambda.$$

This equation can be rearranged to express frequency or wavelength in terms of the other variables:

$$\gamma = \frac{V}{\lambda}, \quad \lambda = \frac{V}{\gamma}.$$

Step 2: Analyze Each Option.

Option (1): $V = \gamma\lambda$ — Correct, as this is the standard wave equation.

Option (2): $\gamma = \frac{V}{\lambda}$ — Correct, as this is a valid rearrangement of the wave equation.

Option (3): $\lambda = \frac{V}{\gamma}$ — Correct, as this is another valid rearrangement of the wave equation.

Option (4): All of these — Correct, as all three equations are valid relationships derived from the wave equation.

Step 3: Final Answer.

(4) All of these

Quick Tip

The relationship between velocity, frequency, and wavelength is fundamental in wave mechanics. Always remember the basic wave equation $V = \gamma\lambda$ and its rearrangements $\gamma = \frac{V}{\lambda}$ and $\lambda = \frac{V}{\gamma}$. These equations apply to all types of waves, including sound waves.

81. The number of electrons constituting one coulomb of charge :

(1) 6.25×10^{18}

(2) 1.6×10^{-19}

(3) 7.25×10^{23}

(4) 6.23×10^{-23}

Correct Answer: (1) 6.25×10^{18}

Solution:

Step 1: Recall the charge of a single electron.

The charge of a single electron (e) is approximately 1.602×10^{-19} Coulombs (C).

Step 2: Understand the relationship between total charge, number of electrons, and charge per electron.

The total charge (Q) is equal to the number of electrons (n) multiplied by the charge of a single electron (e). So, $Q = n \times e$.

Step 3: Rearrange the formula to find the number of electrons.

To find the number of electrons (n), we can rearrange the formula as: $n = \frac{Q}{e}$

Step 4: Substitute the given values into the formula.

We are given that $Q = 1$ Coulomb (C) and $e = 1.602 \times 10^{-19}$ C. $n = \frac{1 \text{ C}}{1.602 \times 10^{-19} \text{ C}}$

Step 5: Calculate the number of electrons.

$n \approx 6.242 \times 10^{18}$ Rounding to two decimal places, this is approximately 6.25×10^{18} .

Step 6: Compare with the given options.

- (1) 6.25×10^{18} : This matches our calculated value.
- (2) 1.6×10^{-19} : This is the magnitude of the charge of a single electron, not the number of electrons in one coulomb.
- (3) 7.25×10^{23} : This value is incorrect.
- (4) 6.23×10^{-23} : This value is incorrect.
- (1)** 6.25×10^{18}

Quick Tip

The fundamental charge of an electron is 1.6×10^{-19} C. To find the number of electrons in a given charge, divide the total charge by the charge of one electron.

82. The resistance of an ideal Voltmeter is :

- (1) 100Ω
- (2) Infinite
- (3) Low
- (4) Zero

Correct Answer: (2) Infinite

Solution:

Step 1: Understand the function of a voltmeter.

A voltmeter is an instrument used to measure the potential difference (voltage) between two points in an electrical circuit. To measure voltage, a voltmeter must be connected in parallel across the component whose voltage is to be measured.

Step 2: Consider how a voltmeter should ideally interact with a circuit.

For a voltmeter to accurately measure the voltage across a component without altering the current distribution or voltage drop in the rest of the circuit, it should draw negligible current from the circuit.

Step 3: Relate current drawn to resistance (Ohm's Law).

According to Ohm's Law, $V = IR$, where V is voltage, I is current, and R is resistance. If the voltmeter draws negligible current ($I \approx 0$) for a given voltage (V), its resistance ($R = V/I$) must be very high.

Step 4: Define "ideal" voltmeter resistance.

In an ideal scenario, a voltmeter draws no current at all to ensure perfect measurement accuracy. For I to be zero while V is non-zero, the resistance (R) must be infinitely large.

Step 5: Evaluate the given options in the context of an ideal voltmeter.

- **(1) 100 Ω :** This is a finite, relatively low resistance, which would draw significant current and affect the circuit being measured.
- **(2) Infinite:** An infinite resistance ensures that no current flows through the voltmeter, thus not disturbing the circuit it is measuring. This is the characteristic of an ideal voltmeter.
- **(3) Low:** A low resistance would cause the voltmeter to act like a short circuit, diverting current and significantly altering the voltage being measured.
- **(4) Zero:** Zero resistance would mean the voltmeter acts as a perfect short circuit, drawing maximum current and effectively shorting out the component it's meant to measure the voltage across.

Step 6: Conclude the correct resistance for an ideal voltmeter.

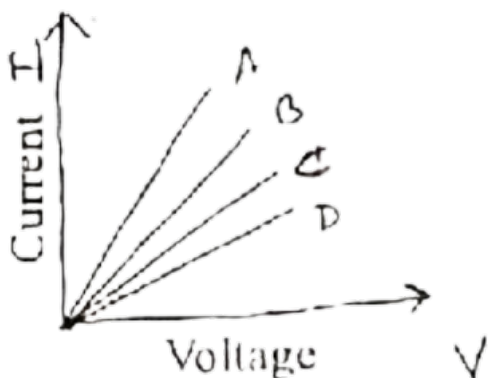
The resistance of an ideal voltmeter is infinite.

(2) Infinite

Quick Tip

An ideal voltmeter should not alter the circuit it is measuring. To achieve this, it must draw no current, which implies it has infinite resistance when connected in parallel.

83. V-I graph for four materials A, B, C & D are shown in fig. The best material to make live wire of domestic wiring is :



- (1) A
- (2) B
- (3) C
- (4) D

Correct Answer: (1) A

Solution: Step 1: Understand the V-I graph and Ohm's Law.

The V-I graph plots voltage (V) on the x-axis and current (I) on the y-axis. Ohm's Law states that $V = IR$, which means $R = V/I$. Therefore, the resistance (R) of a conductor is the reciprocal of the slope of the I-V graph (Current vs. Voltage graph). A steeper slope on an I-V graph means lower resistance and higher conductance.

Step 2: Determine the ideal property for a live wire in domestic wiring.

For domestic wiring, a material with very low resistance is needed for the live wire. High resistance leads to significant energy loss as heat ($P = I^2R$) and a drop in voltage, which is undesirable for efficient electrical transmission.

Step 3: Analyze the slopes of the V-I graphs for materials A, B, C, and D.

Looking at the provided graph:

- Material A has the steepest slope, indicating the largest I/V ratio.
- Material B has a less steep slope than A.
- Material C has a less steep slope than B.
- Material D has the least steep slope, indicating the smallest I/V ratio.

Step 4: Relate the slope to resistance.

A steeper slope on an I - V graph means a higher current for a given voltage, which implies lower resistance ($R = V/I$). Therefore, material A has the lowest resistance, and material D has the highest resistance.

Step 5: Select the best material.

Since the best material for domestic wiring (live wire) should have the lowest resistance to minimize energy loss and voltage drop, material A is the most suitable choice.

(1) A

Quick Tip

For an I - V graph (Current on y -axis, Voltage on x -axis), the slope represents the conductance ($1/R$). A steeper slope indicates lower resistance and thus a better conductor. For domestic wiring, a material with very low resistance is desired to efficiently transmit electricity.

84. The resistivity of a conductor depends upon :

- (1) Area of cross-section of conductor
- (2) Length of conductor
- (3) 1 and 2 both
- (4) None of the above

Correct Answer: (4) None of the above

Solution: Step 1: Define resistivity.

Resistivity (ρ) is an intrinsic property of a material that quantifies how strongly it resists electric current. It is a fundamental characteristic of the material itself, unlike resistance, which depends on the dimensions of the conductor.

Step 2: Recall the formula for resistance and its relation to resistivity.

The resistance (R) of a conductor is given by the formula: $R = \rho \frac{L}{A}$ where:

- R is the resistance
- ρ (rho) is the resistivity of the material
- L is the length of the conductor
- A is the area of the cross-section of the conductor

Step 3: Analyze the dependence of resistivity. Resistivity (ρ) depends only on:

- **Nature of the material:** Different materials (e.g., copper, aluminum, silver) have different resistivities.
- **Temperature:** The resistivity of most materials changes with temperature. For metals, resistivity generally increases with temperature.

Resistivity does not depend on the geometric dimensions of the conductor, such as its length (L) or area of cross-section (A). These dimensions affect the resistance of the conductor, but not its intrinsic resistivity.

Step 4: Evaluate the given options.

- (1) Area of cross-section of conductor: Resistivity does not depend on the area of cross-section.
- (2) Length of conductor: Resistivity does not depend on the length of the conductor.
- (3) 1 and 2 both: Since neither (1) nor (2) affects resistivity, this option is incorrect.
- (4) None of the above: This aligns with the understanding that resistivity is an inherent property of the material and its temperature, not its dimensions.

(4) None of the above

Quick Tip

Resistivity is an inherent property of the material itself and its temperature, indicating how well it resists current flow. It is independent of the conductor's length or cross-sectional area. These dimensions affect the overall resistance, but not the material's fundamental resistivity.

85. If the diameter of a wire of $1\ \Omega$ is tripled, then its resistance will become:

- (1) $9\ \Omega$
- (2) $\frac{1}{9}\ \Omega$
- (3) $\frac{1}{3}\ \Omega$
- (4) $3\ \Omega$

Correct Answer: (2) $\frac{1}{9}\ \Omega$

Solution:

Step 1: Understand Resistance Formula.

The resistance (R) of a wire is given by:

$$R = \rho \frac{L}{A},$$

where:

ρ is the resistivity of the material,

L is the length of the wire,

A is the cross-sectional area of the wire.

The cross-sectional area (A) of a wire is related to its diameter (d) by:

$$A = \pi \left(\frac{d}{2} \right)^2 = \frac{\pi d^2}{4}.$$

Step 2: Analyze the Effect of Tripling the Diameter.

If the diameter is tripled, new diameter $= 3d$. Then,

$$A_{\text{new}} = \pi \left(\frac{3d}{2} \right)^2 = \frac{\pi(3d)^2}{4} = \frac{9\pi d^2}{4} = 9A.$$

Since resistance is inversely proportional to cross-sectional area:

$$R \propto \frac{1}{A}.$$

So if A becomes 9 times, then:

$$R_{\text{new}} = \frac{R_{\text{original}}}{9}.$$

Given $R_{\text{original}} = 1\ \Omega$, we have:

$$R_{\text{new}} = \frac{1}{9}\ \Omega.$$

Step 3: Analyze the Options.

Option (1): $9\ \Omega$ — Incorrect

Option (2): $\frac{1}{9}\ \Omega$ — Correct

Option (3): $\frac{1}{3}\ \Omega$ — Incorrect

Option (4): $3\ \Omega$ — Incorrect

Step 4: Final Answer.

$(2) \quad \frac{1}{9}\ \Omega$

Quick Tip

When the diameter of a wire is changed, the resistance changes inversely with the square of the diameter because the cross-sectional area depends on the square of the diameter. Always use the formula $R \propto \frac{1}{A}$ to analyze such problems.

86. On increasing the temperature, the resistance of conductors:

(1) Increases

(2) Decreases

(3) Becomes zero

(4) None of the above

Correct Answer: (1) Increases

Solution:

Step 1: Understand Temperature Dependence of Resistance.

For most conductors, the resistance increases with an increase in temperature. This is due to increased lattice vibrations in the material, which hinder the flow of electrons. The relationship between resistance (R) and temperature (T) is often expressed as:

$$R(T) = R_0 [1 + \alpha(T - T_0)],$$

where:

R_0 is the resistance at a reference temperature T_0 ,

α is the temperature coefficient of resistivity.

For metals, $\alpha > 0$, meaning resistance increases with temperature.

Step 2: Analyze Each Option. Option (1): Increases — Correct, as resistance generally increases with temperature for conductors.

Option (2): Decreases — Incorrect, as resistance typically increases with temperature.

Option (3): Becomes zero — Incorrect, as resistance does not become zero unless the material becomes superconducting, which is not implied here.

Option (4): None of the above — Incorrect, as option (1) is correct.

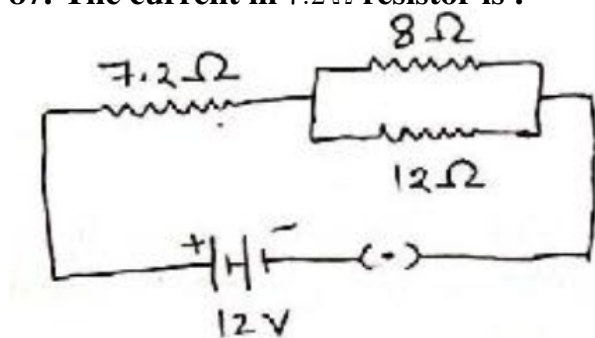
Step 3: Final Answer.

(1) Increases

Quick Tip

For most conductors, resistance increases with temperature due to increased lattice vibrations that impede electron flow. This behavior is described by the temperature dependence formula $R(T) = R_0 [1 + \alpha(T - T_0)]$.

87. The current in $7.2\ \Omega$ resistor is :



(1) 1.5 A

(2) 2 A

(3) 1 A

(4) 0.5 A

Correct Answer: (3) 1 A

Solution:

Step 1: Identify the components and configuration in the circuit.

The circuit consists of a 12V battery, a $7.2\ \Omega$ resistor in series with a parallel combination of an $8\ \Omega$ resistor and a $12\ \Omega$ resistor. The current in the $7.2\ \Omega$ resistor is the total current flowing out of the battery, as it is in the main series path.

Step 2: Calculate the equivalent resistance of the parallel combination.

For two resistors in parallel, the equivalent resistance ($R_{eq,parallel}$) is given by:

$$\frac{1}{R_{eq,parallel}} = \frac{1}{R_1} + \frac{1}{R_2}$$

Here, $R_1 = 8\ \Omega$ and $R_2 = 12\ \Omega$.

$$\frac{1}{R_{eq,parallel}} = \frac{1}{8} + \frac{1}{12} = \frac{3+2}{24} = \frac{5}{24}$$

$$R_{eq,parallel} = \frac{24}{5} = 4.8\ \Omega$$

Step 3: Calculate the total equivalent resistance of the circuit.

The $7.2\ \Omega$ resistor is in series with the parallel combination ($4.8\ \Omega$).

For resistors in series, the total equivalent resistance (R_{total}) is the sum of individual resistances:

$$R_{total} = R_{series} + R_{eq,parallel}$$

$$R_{total} = 7.2\ \Omega + 4.8\ \Omega = 12\ \Omega$$

Step 4: Calculate the total current flowing through the circuit (and thus through the $7.2\ \Omega$ resistor).

Using Ohm's Law, $V = IR$, where V is the total voltage, I is the total current, and R is the total equivalent resistance.

$$I = \frac{V}{R_{total}}$$

Given $V = 12\ \text{V}$ and $R_{total} = 12\ \Omega$.

$$I = \frac{12\ \text{V}}{12\ \Omega} = 1\ \text{A}$$

Step 5: Conclude the current in the $7.2\ \Omega$ resistor.

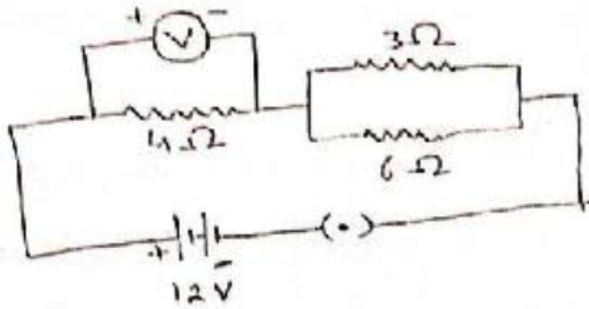
Since the $7.2\ \Omega$ resistor is in the main series path, the current flowing through it is the total current of the circuit, which is 1 A.

(3) 1 A

Quick Tip

In series circuits, the current is the same through all components. In parallel circuits, the voltage across each branch is the same. Always simplify parallel combinations first, then add series resistances to find total resistance.

88. The reading of the voltmeter is :



- (1) 4 V
- (2) 3 V
- (3) 8 V
- (4) 6 V

Correct Answer: (3) 8 V

Solution:

Step 1: Identify the components and configuration in the circuit.

The circuit has a 12V battery. There's a 4Ω resistor in series with a parallel combination of a 3Ω resistor and a 6Ω resistor. The voltmeter is connected across the 4Ω resistor. We need to find the voltage across the 4Ω resistor.

Step 2: Calculate the equivalent resistance of the parallel combination.

For two resistors in parallel, the equivalent resistance ($R_{eq,parallel}$) is given by:

$$\frac{1}{R_{eq,parallel}} = \frac{1}{R_1} + \frac{1}{R_2}$$

Here, $R_1 = 3\Omega$ and $R_2 = 6\Omega$.

$$\frac{1}{R_{eq,parallel}} = \frac{1}{3} + \frac{1}{6} = \frac{2+1}{6} = \frac{3}{6} = \frac{1}{2}$$

$$R_{eq,parallel} = 2\Omega$$

Step 3: Calculate the total equivalent resistance of the circuit.

The 4Ω resistor is in series with the parallel combination (2Ω).

For resistors in series, the total equivalent resistance (R_{total}) is the sum of individual resistances:

$$R_{total} = R_{series} + R_{eq,parallel}$$

$$R_{total} = 4\Omega + 2\Omega = 6\Omega$$

Step 4: Calculate the total current flowing through the circuit.

Using Ohm's Law, $V = IR$, where V is the total voltage, I is the total current, and R is the total equivalent resistance.

$$I_{total} = \frac{V_{total}}{R_{total}}$$

$$\text{Given } V_{total} = 12\text{ V and } R_{total} = 6\Omega. I_{total} = \frac{12\text{V}}{6\Omega} = 2\text{ A}$$

Step 5: Calculate the voltage across the 4Ω resistor.

Since the 4Ω resistor is in the main series path, the total current ($I_{total} = 2\text{ A}$) flows through it. Using Ohm's Law for the 4Ω resistor: $V_{4\Omega} = I_{total} \times R_{4\Omega}$ $V_{4\Omega} = 2\text{ A} \times 4\Omega = 8\text{ V}$

Step 6: Conclude the reading of the voltmeter.

The voltmeter is connected across the 4Ω resistor, so its reading will be 8 V.

(3) 8 V

Quick Tip

To find the voltage across a specific resistor in a series circuit, first find the total current flowing through the circuit, then apply Ohm's law ($V = IR$) to that specific resistor.

89. Which of the following does not represent electric power in the circuit ?

(1) I^2R

(2) IR^2

(3) VI

(4) $\frac{V^2}{R}$

Correct Answer: (2) IR^2

Solution: Step 1: Recall the standard formulas for electric power.

Electric power (P) in a circuit can be expressed in several ways, derived from Ohm's Law ($V = IR$). The primary formula is:

- $P = VI$ (Power equals Voltage times Current)

Step 2: Derive other power formulas using Ohm's Law.

- Substitute $V = IR$ into $P = VI$: $P = (IR)I = I^2R$
- Substitute $I = V/R$ into $P = VI$: $P = V(\frac{V}{R}) = \frac{V^2}{R}$

Step 3: Evaluate each given option based on the derived formulas.

- (1) I^2R : This is a correct formula for electric power.
- (2) IR^2 : This is NOT a standard formula for electric power. The current is multiplied by the square of the resistance, which is incorrect.
- (3) VI : This is a correct and fundamental formula for electric power.
- (4) $\frac{V^2}{R}$: This is a correct formula for electric power.

Step 4: Identify the option that does not represent electric power. Based on the analysis, IR^2 does not represent electric power.

(2) IR^2

Quick Tip

The three common formulas for electric power are $P = VI$, $P = I^2R$, and $P = V^2/R$. These are all derived from the fundamental definition of power and Ohm's Law. Any other combination, like IR^2 , is generally incorrect.

90. Two identical resistance wires are first connected in series and then in parallel in an electric circuit. The ratio of heat produced in the two cases will be :

- (1) 1:2
- (2) 2:1
- (3) 1:4
- (4) 4:1

Correct Answer: (3) 1:4

Solution: Step 1: Define the resistances and heat produced.

Let the resistance of each identical wire be R .

The heat produced (H) in an electric circuit is given by Joule's Law of Heating: $H = I^2 R t$, where I is current, R is resistance, and t is time. Alternatively, $H = \frac{V^2}{R} t$ if voltage is constant, or $H = V I t$. We will assume the same voltage source V is applied in both cases, which is typical for such problems.

Step 2: Calculate equivalent resistance and heat produced in series connection.

When two identical resistors (R) are connected in series, the equivalent resistance (R_S) is:

$$R_S = R + R = 2R$$

The heat produced in the series circuit (H_S) when connected to a voltage source V for time t will be:

$$H_S = \frac{V^2}{R_S} t = \frac{V^2}{2R} t$$

Step 3: Calculate equivalent resistance and heat produced in parallel connection.

When two identical resistors (R) are connected in parallel, the equivalent resistance (R_P) is:

$$\frac{1}{R_P} = \frac{1}{R} + \frac{1}{R} = \frac{2}{R} \quad R_P = \frac{R}{2}$$

The heat produced in the parallel circuit (H_P) when connected to the same voltage source V for time t will be:

$$H_P = \frac{V^2}{R_P} t = \frac{V^2}{(R/2)} t = \frac{2V^2}{R} t$$

Step 4: Determine the ratio of heat produced (series to parallel).

Now, find the ratio $H_S : H_P$:

$$\frac{H_S}{H_P} = \frac{\frac{V^2}{2R} t}{\frac{2V^2}{R} t}$$

Cancel out common terms (V^2 , R , t):

$$\frac{H_S}{H_P} = \frac{1/2}{2 \times 2} = \frac{1}{4}$$

So, the ratio of heat produced in the two cases (series to parallel) is 1:4.

(3) 1:4

Quick Tip

When dealing with heat produced and comparing series vs. parallel connections, it's often easiest to use the $H = V^2/R \cdot t$ formula if the voltage source is assumed to be constant across the combinations. This avoids calculating currents for each case. Remember that series connection increases total resistance, while parallel connection decreases it.

CHEMISTRY

91. Rancidity is due to oxidation of:

- (1) Oil
- (2) Fats
- (3) Oil and Fats
- (4) None of these

Correct Answer: (3) Oil and Fats

Solution:

Step 1: Understand Rancidity.

Rancidity is the process of degradation of fats and oils due to oxidation. This occurs when unsaturated fatty acids in oils and fats react with oxygen in the presence of heat, light, or catalysts, leading to the formation of unpleasant odors and flavors.

Step 2: Analyze Each Option.

Option (1): Oil — Incorrect, as rancidity affects both oils and fats, not just oils.

Option (2): Fats — Incorrect, as rancidity affects both oils and fats, not just fats.

Option (3): Oil and Fats — Correct, as rancidity is caused by the oxidation of both oils and fats.

Option (4): None of these — Incorrect, as options (1) and (2) are partially correct, but the most accurate answer includes both oils and fats.

Step 3: Final Answer.

(3) Oil and Fats

Quick Tip

Rancidity is a chemical reaction that primarily affects unsaturated fats and oils. It is a form of oxidation that leads to the breakdown of these lipids, resulting in undesirable changes in flavor, odor, and texture. Both oils and fats are susceptible to this process.

92. The reaction $\text{CuSO}_4 + \text{Zn} \rightarrow \text{ZnSO}_4 + \text{Cu}$ is an example of a:

- (1) Combination reaction

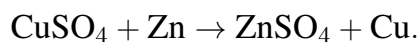
- (2) Double displacement reaction
- (3) Decomposition reaction
- (4) Displacement reaction

Correct Answer: (4) Displacement reaction

Solution:

Step 1: Analyze the Reaction.

The given reaction is:



In this reaction:

Zinc (Zn) displaces copper (Cu) from copper sulfate (CuSO_4).

The products are zinc sulfate (ZnSO_4) and elemental copper (Cu).

Step 2: Identify the Type of Reaction.

This is a displacement reaction, where one element replaces another in a compound.

Specifically, it is a **single displacement** reaction.

Step 3: Analyze Each Option.

Option (1): Combination reaction — Incorrect

Option (2): Double displacement reaction — Incorrect

Option (3): Decomposition reaction — Incorrect

Option (4): Displacement reaction — Correct

Step 4: Final Answer.

(4) Displacement reaction

Quick Tip

Displacement reactions occur when one element replaces another in a compound. They are characterized by the direct replacement of one element by another, often involving metals reacting with metal salts. In this case, zinc displaces copper from copper sulfate.

93. FeSO_4 decomposes on heating into :

- (1) ' Fe_2O_3 '

- (2) ' Fe_2O_3 ' & ' SO_2 '
(3) ' Fe_2O_3 ' & ' SO_3 '
(4) ' Fe_2O_3 ', ' SO_2 ' and ' SO_3 '

Correct Answer: (4) ' Fe_2O_3 ', ' SO_2 ' and ' SO_3 '

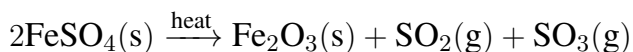
Solution:

Step 1: Understand the decomposition of ferrous sulfate (FeSO_4).

Ferrous sulfate (FeSO_4) is a green crystalline solid that decomposes upon strong heating. This is a common thermal decomposition reaction in chemistry.

Step 2: Write the balanced chemical equation for the decomposition.

When ferrous sulfate heptahydrate ($\text{FeSO}_4 \cdot 7\text{H}_2\text{O}$) is heated, it first loses its water of crystallization to form anhydrous ferrous sulfate. Upon further strong heating, anhydrous ferrous sulfate decomposes into ferric oxide, sulfur dioxide, and sulfur trioxide. The balanced chemical equation for the thermal decomposition of anhydrous ferrous sulfate is:



Step 3: Identify the products of the decomposition.

From the balanced equation, the products are ferric oxide (Fe_2O_3), sulfur dioxide (SO_2), and sulfur trioxide (SO_3).

Step 4: Compare the products with the given options.

- (1) ' Fe_2O_3 ': This is only one of the products.
(2) ' Fe_2O_3 ' & ' SO_2 ': This is missing SO_3 .
(3) ' Fe_2O_3 ' & ' SO_3 ': This is missing SO_2 .
(4) ' Fe_2O_3 ', ' SO_2 ' and ' SO_3 ': This option correctly lists all the products.
(4) ' Fe_2O_3 ', ' SO_2 ' and ' SO_3 '

Quick Tip

Thermal decomposition reactions often produce simpler compounds, sometimes involving changes in oxidation states. For sulfates of transition metals like iron, the products commonly include the metal oxide and oxides of sulfur.

94. Propane, with the molecular formula C_3H_8 has :

- (1) '6' Covalent bonds
- (2) '7' Covalent bonds
- (3) '10' Covalent bonds
- (4) '8' Covalent bonds

Correct Answer: (3) '10' Covalent bonds

Solution:

Step 1: Draw the structural formula of Propane (C_3H_8).

Propane is an alkane with three carbon atoms. The carbon atoms are bonded in a straight chain, and hydrogen atoms are attached to the carbon atoms.

The skeletal structure is C-C-C.

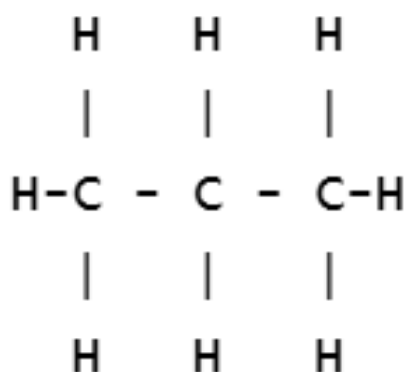
Each carbon atom forms a total of four bonds.

The first carbon (terminal) is bonded to one other carbon and needs three hydrogen atoms.

The second carbon (middle) is bonded to two other carbons and needs two hydrogen atoms.

The third carbon (terminal) is bonded to one other carbon and needs three hydrogen atoms.

The structure looks like this:



Step 2: Count the Carbon-Carbon (C-C) covalent bonds.

There are two C-C single bonds in the propane molecule.

Step 3: Count the Carbon-Hydrogen (C-H) covalent bonds.

The first carbon has 3 C-H bonds.

The second carbon has 2 C-H bonds.

The third carbon has 3 C-H bonds.

Total C-H bonds = $3 + 2 + 3 = 8$ C-H bonds.

Step 4: Calculate the total number of covalent bonds.

Total covalent bonds = (Number of C-C bonds) + (Number of C-H bonds)
Total covalent bonds = $2 + 8 = 10$.

Step 5: Compare with the given options.

- (1) '6' Covalent bonds: Incorrect.
- (2) '7' Covalent bonds: Incorrect.
- (3) '10' Covalent bonds: This matches our calculated value.
- (4) '8' Covalent bonds: Incorrect (this is just the number of C-H bonds).

(3) '10' Covalent bonds**Quick Tip**

For alkanes with molecular formula C_nH_{2n+2} , the total number of covalent bonds (C-C and C-H) is $3n + 1$. For propane (C_3H_8), $n = 3$, so total bonds = $3(3) + 1 = 9 + 1 = 10$.

95. Two successive compounds, having same functional group. They have a difference of :

- (1) $-CH_2$ Unit
- (2) $-CH_3$ Unit
- (3) $-C_2H_2$ Unit
- (4) $-CH_4$ Unit

Correct Answer: (1) $-CH_2$ Unit

Solution: Step 1: Understand the concept of homologous series.

In organic chemistry, a homologous series is a series of compounds with the same general formula, usually varying by a single parameter such as the length of a carbon chain. All compounds in a homologous series have the same functional group and similar chemical properties, with a gradual change in physical properties as the series progresses.

Step 2: Identify the difference between successive members of a homologous series.

Successive compounds in a homologous series differ by a $-CH_2$ (methylene) unit. For example, in the alkane series:

- Methane (CH_4)

- Ethane (C_2H_6) - differs from methane by one $-\text{CH}_2$ group ($\text{CH}_4 + \text{CH}_2 = \text{C}_2\text{H}_6$)
- Propane (C_3H_8) - differs from ethane by one $-\text{CH}_2$ group ($\text{C}_2\text{H}_6 + \text{CH}_2 = \text{C}_3\text{H}_8$)

This pattern holds true for other homologous series as well (e.g., alcohols, carboxylic acids, etc.), as long as they have the same functional group.

Step 3: Compare the conclusion with the given options.

The difference between two successive compounds having the same functional group is a $-\text{CH}_2$ unit. This corresponds to option (1).

(1) $-\text{CH}_2$ Unit

Quick Tip

Remember that a homologous series is characterized by compounds having the same functional group and differing by a $-\text{CH}_2$ unit. This difference leads to a predictable change in molecular mass (14 amu) and a gradual change in physical properties.

96. Formula of Carboxylic group is :

- (1) $-\text{CHO}$
- (2) $-\text{COOH}$
- (3) $-\text{COCH}_3$
- (4) $-\text{OH}$

Correct Answer: (2) $-\text{COOH}$

Solution: Step 1: Understand the definition of a functional group.

A functional group is a specific group of atoms within a molecule that is responsible for the characteristic chemical reactions of that molecule.

Step 2: Recall the common functional groups and their formulas.

- **Aldehyde group:** $-\text{CHO}$ (or $-\text{CH}=\text{O}$)
- **Carboxylic acid group:** $-\text{COOH}$ (or $-\text{C}(=\text{O})\text{OH}$)
- **Ketone group:** $-\text{C}(=\text{O})-$ (often shown within a molecule like $-\text{COCH}_3$ for a methyl ketone, but the group itself is just the carbonyl carbon bonded to two other carbons)

- **Hydroxyl group (Alcohol):** -OH

Step 3: Identify the formula for the Carboxylic group.

Based on the recall, the carboxylic group is characterized by a carbon atom double-bonded to an oxygen atom and single-bonded to a hydroxyl (-OH) group. Its formula is -COOH.

Step 4: Compare the conclusion with the given options.

Option (2) -COOH correctly represents the carboxylic group.

(2) -COOH

Quick Tip

It's essential to recognize common functional groups and their formulas, as they dictate the chemical behavior of organic compounds. Pay close attention to the arrangement of atoms, especially the double-bonded oxygen in carbonyl-containing groups.

97. Triads rule was given by:

- (1) Rutherford
- (2) Dobereiner
- (3) New Lands
- (4) Rutherford and New Land

Correct Answer: (2) Dobereiner

Solution:

Step 1: Understand the Triads Rule. The Triads Rule is a concept in chemistry that was proposed by Johann Wolfgang Döbereiner in the early 19th century. Döbereiner observed that certain elements could be grouped into triads of three elements with similar properties, where the atomic mass of the middle element in each triad was approximately the average of the atomic masses of the other two elements.

Step 2: Analyze Each Option.

Option (1): Rutherford — Incorrect, as Rutherford is known for his work on atomic structure, not the Triads Rule.

Option (2): Dobereiner — Correct, as Döbereiner is credited with proposing the Triads Rule.

Option (3): New Lands — Incorrect, as this is not a recognized name associated with the Triads Rule.

Option (4): Rutherford and New Land — Incorrect, as neither Rutherford nor "New Land" is associated with the Triads Rule.

Step 3: Final Answer.

(2) Dobereiner

Quick Tip

The Triads Rule was an early attempt to classify elements based on their properties and atomic masses. It was proposed by Johann Wolfgang Döbereiner, who grouped elements into triads with similar chemical properties. This laid the groundwork for later periodic classification systems.

98. Which element has '2, 8, 1' Electronic configuration?

- (1) K
- (2) Mg
- (3) Al
- (4) Na

Correct Answer: (4) Na

Solution:

Step 1: Analyze the Electronic Configuration.

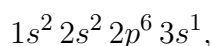
The electronic configuration '2, 8, 1' indicates that the element has:

2 electrons in the first shell (K-shell),

8 electrons in the second shell (L-shell),

1 electron in the third shell (M-shell).

This configuration corresponds to the element sodium (Na), which has an atomic number of 11. The full electronic configuration of sodium is:



which simplifies to '2, 8, 1'.

Step 2: Analyze Each Option.

Option (1): K — Incorrect, as potassium (K) has an electronic configuration of '2, 8, 8, 1'.

Option (2): Mg — Incorrect, as magnesium (Mg) has an electronic configuration of '2, 8, 2'.

Option (3): Al — Incorrect, as aluminum (Al) has an electronic configuration of '2, 8, 3'.

Option (4): Na — Correct, as sodium (Na) has the electronic configuration '2, 8, 1'.

Step 3: Final Answer.

(4) Na

Quick Tip

To determine the element corresponding to a given electronic configuration, count the total number of electrons in each shell. For '2, 8, 1', the total number of electrons is $2 + 8 + 1 = 11$, which corresponds to sodium (Na). Always remember that the electronic configuration reflects the distribution of electrons across different energy levels.

99. Mendeleev's Modern periodic law is based on :

(1) Atomic mass

(2) Atomic Number

(3) No. of Neutrons

(4) Atomic mass and atomic Number

Correct Answer: (1) Atomic mass

Solution:

Step 1: Understand Mendeleev's original Periodic Law.

Dmitri Mendeleev formulated the periodic law stating that the properties of elements are a periodic function of their atomic masses. He arranged elements in his periodic table primarily based on increasing atomic mass.

Step 2: Differentiate between Mendeleev's and the Modern Periodic Law.

The question specifically asks about "Mendeleev's Modern periodic law". This phrasing is slightly ambiguous. The "Modern Periodic Law" (as established later by Moseley) is based on atomic number. However, if it refers to "Mendeleev's" law, it is based on atomic mass. Given the options, it's highly likely it refers to Mendeleev's original formulation.

Step 3: Evaluate the given options.

- **(1) Atomic mass:** This is the basis of Mendeleev's original periodic law.
- **(2) Atomic Number:** This is the basis of the Modern Periodic Law (developed after Mendeleev's work).
- **(3) No. of Nutron's (Neutrons):** The number of neutrons (and thus mass number) is related to atomic mass, but Mendeleev didn't explicitly use neutron count as the basis.
- **(4) Atomic mass and atomic Number:** While both are important properties, Mendeleev's law was specifically based on atomic mass.

Step 4: Conclude the correct basis for Mendeleev's periodic law.

Mendeleev's periodic law is based on atomic mass.

(1) Atomic mass

Quick Tip

Remember the key distinction: Mendeleev's original periodic law is based on atomic mass, while the Modern Periodic Law is based on atomic number.

100. SI unit of density is :

- (1) Kg/cm^3
- (2) Kg/m^3
- (3) g/m^3
- (4) g/cm^3

Correct Answer: (2) Kg/m^3

Solution:

Step 1: Define density.

Density is defined as mass per unit volume.

Step 2: Recall the SI units for mass and volume.

In the International System of Units (SI):

- The SI unit of mass is the kilogram (kg).
- The SI unit of length is the meter (m).

- The SI unit of volume, derived from length, is cubic meter (m^3).

Step 3: Determine the SI unit of density.

Since density = mass / volume, the SI unit of density will be the SI unit of mass divided by the SI unit of volume.

SI unit of density = kilogram/cubic meter = kg/m^3 .

Step 4: Evaluate the given options.

- (1) Kg/cm^3 : This uses kilograms for mass, but cubic centimeters for volume, which is not the SI unit of volume.
- (2) Kg/m^3 : This uses kilograms for mass and cubic meters for volume, which are both SI units. This is the correct SI unit for density.
- (3) g/m^3 : This uses grams for mass, which is a common unit for mass but not the base SI unit (kilogram is).
- (4) g/cm^3 : This uses grams for mass and cubic centimeters for volume. Both are common units but not the primary SI units for density.

(2) Kg/m^3

Quick Tip

Always refer to the base SI units for fundamental quantities (like mass in kg, length in m, time in s) to derive the SI units for derived quantities (like density, speed, force, etc.).

101. "Tyndall effect" will be shown by which of the following ?

- (1) Distilled water
- (2) Sugar solution
- (3) Ethanol
- (4) Starch solution

Correct Answer: (4) Starch solution

Solution: Step 1: Understand the Tyndall effect.

The Tyndall effect is the phenomenon where light is scattered by particles in a colloid or a fine suspension, making the path of the light visible. This effect is observed when the dispersed particles are large enough to scatter light, but small enough that they do not settle

out of the dispersion. True solutions (like distilled water, sugar solution, and ethanol) have particles that are too small to scatter light effectively, so they do not show the Tyndall effect.

Step 2: Classify the given options based on particle size.

- **Distilled water:** A pure substance, essentially a true solution, with particles too small to scatter light.
- **Sugar solution:** A true solution where sugar molecules are dissolved in water; their size is too small to cause significant scattering.
- **Ethanol:** A pure substance, or if considered in solution with water, forms a true solution. Particles are too small.
- **Starch solution:** Starch in water forms a colloidal dispersion (or a fine suspension, depending on concentration and preparation). The starch particles are large enough to scatter light.

Step 3: Determine which solution will exhibit the Tyndall effect. Based on the principle that only colloids and fine suspensions exhibit the Tyndall effect, starch solution is the correct answer because it forms a colloidal dispersion.

(4) Starch solution

Quick Tip

The Tyndall effect is a key characteristic distinguishing colloids and fine suspensions from true solutions. If you can see the light beam passing through a transparent liquid, it's likely a colloid.

102. The formula of Calcium Carbonate is :

- (1) MgCO_3
- (2) Na_2CO_3
- (3) CuCO_3
- (4) CaCO_3

Correct Answer: (4) CaCO_3

Solution: Step 1: Identify the ions involved in Calcium Carbonate.

- **Calcium** is a Group 2 element and forms a cation with a +2 charge: Ca^{2+} .
- **Carbonate** is a polyatomic anion with a -2 charge: CO_3^{2-} .

Step 2: Determine the chemical formula by balancing charges.

To form a neutral compound, the total positive charge must balance the total negative charge. Since calcium has a +2 charge (Ca^{2+}) and carbonate has a -2 charge (CO_3^{2-}), one Ca^{2+} ion combines with one CO_3^{2-} ion. The formula is therefore CaCO_3 .

Step 3: Evaluate the given options.

- (1) MgCO_3 : This is Magnesium Carbonate.
- (2) Na_2CO_3 : This is Sodium Carbonate.
- (3) CuCO_3 : This is Copper(II) Carbonate.
- (4) CaCO_3 : This is Calcium Carbonate.

Step 4: Conclude the correct formula.

The correct formula for Calcium Carbonate is CaCO_3 .

(4) CaCO_3

Quick Tip

When writing chemical formulas for ionic compounds, always remember the charges of the individual ions (cations and anions) and combine them in a ratio that results in a net neutral charge for the compound.

103. Choose the correct relationship: molar mass - common name - chemical formula from the following options.

- (1) 22.5-Ethyne- C_2H_2
- (2) 292.5-Sulphur molecule- S_8
- (3) 36.5-Hydrochloric acid-HCl
- (4) 65.5-Nitric acid- HNO_3

Correct Answer: (3) 36.5-Hydrochloric acid-HCl

Solution:

Step 1: Analyze Each Option.

Let's evaluate each option by calculating or verifying the molar mass, common name, and chemical formula:

1. Option (1): 22.5 — Ethyne — C_2H_2

Ethyne (acetylene) has the chemical formula C_2H_2 .

Molar mass:

$$(2 \times 12.01) + (2 \times 1.01) = 24.02 + 2.02 = 26.04 \text{ g/mol}$$

Given: 22.5, which is incorrect.

2. Option (2): 292.5 — Sulphur molecule — S_8

Molar mass:

$$8 \times 32.07 = 256.56 \text{ g/mol}$$

Given: 292.5, which is incorrect.

3. Option (3): 36.5 — Hydrochloric acid — HCl

Molar mass:

$$1.01 + 35.45 = 36.46 \text{ g/mol}$$

Given: 36.5, which is correct.

4. Option (4): 65.5 — Nitric acid — HNO_3

Molar mass:

$$1.01 + 14.01 + (3 \times 16.00) = 1.01 + 14.01 + 48.00 = 63.02 \text{ g/mol}$$

Given: 65.5, which is incorrect.

Step 2: Final Answer.

(3) 36.5-Hydrochloric acid-HCl

Quick Tip

To solve such problems, calculate the molar mass of the chemical formula provided and compare it with the given molar mass. Ensure that the common name and chemical formula correspond correctly.

104. What is the mass of 0.5 mole of oxygen atoms?

- (1) 10 g
- (2) 12 g
- (3) 14 g
- (4) 8 g

Correct Answer: (4) 8 g

Solution:

Step 1: Understand the Problem.

The atomic mass of oxygen (O) is approximately 16.00 g/mol. To find the mass of 0.5 moles of oxygen atoms, use the formula:

$$\text{Mass} = \text{Number of moles} \times \text{Molar mass.}$$

Step 2: Calculate the Mass.

Substitute the given values:

$$\text{Mass} = 0.5 \text{ mol} \times 16.00 \text{ g/mol} = 8.00 \text{ g.}$$

Step 3: Analyze the Options.

Option (1): 10 g — Incorrect, as the calculated mass is 8.00 g.

Option (2): 12 g — Incorrect, as the calculated mass is 8.00 g.

Option (3): 14 g — Incorrect, as the calculated mass is 8.00 g.

Option (4): 8 g — Correct, as it matches the calculated value.

Step 4: Final Answer.

(4) 8 g

Quick Tip

To find the mass of a given number of moles of an element, multiply the number of moles by the molar mass of the element. Always ensure you use the correct atomic mass from the periodic table.

105. The Avogadro constant $6.022140857 \times 10^{23}$ is defined as the number of atoms present in exactly 12 g of

- (1) Carbon-12
- (2) Oxygen-16
- (3) Nitrogen-14
- (4) Carbon-14

Correct Answer: (1) Carbon-12

Solution:

Step 1: Understand the definition of Avogadro's constant.

Avogadro's constant (N_A) is a fundamental physical constant that represents the number of constituent particles (usually atoms or molecules) in one mole of a substance.

Step 2: Recall the historical and standard definition.

Historically and by current international agreement, a mole is defined as the amount of substance of a system that contains $6.022140857 \times 10^{23}$ elementary entities (atoms, molecules, ions, etc.). This number is specifically related to the number of atoms in exactly 12 grams of carbon-12 (^{12}C). Carbon-12 was chosen as the reference standard for atomic mass and the definition of the mole.

Step 3: Evaluate the given options based on this definition.

- **(1) Carbon-12:** This is the internationally accepted reference isotope used in the definition of the mole and Avogadro's constant.
- **(2) Oxygen-16:** While Oxygen-16 is a common isotope, it is not the standard used for defining Avogadro's constant in terms of 12 grams.
- **(3) Nitrogen-14:** Nitrogen-14 is not used in the definition of Avogadro's constant in this context.
- **(4) Carbon-14:** Carbon-14 is an isotope of carbon, but Carbon-12 is the specific isotope used for the definition.

Step 4: Conclude the correct element.

The Avogadro constant is defined based on the number of atoms present in exactly 12 g of Carbon-12.

(1) Carbon-12

Quick Tip

The definition of a mole and Avogadro's constant is inextricably linked to Carbon-12 as the reference isotope.

106. The Law of Conservation of Mass-During a chemical reaction

- (1) the sum of the masses of all reactants is not equal to sum of masses of all products.
- (2) the sum of masses of all reactants is equal to the sum of masses of all products.
- (3) the sum of the masses of all reactants is equal to half of sum of masses of all products.
- (4) the sum of masses of all reactants is equal to double of sum of masses of all products.

Correct Answer: (2) the sum of masses of all reactants is equal to the sum of masses of all products.

Solution:

Step 1: Understand the Law of Conservation of Mass.

The Law of Conservation of Mass is a fundamental principle in chemistry. It states that mass in an isolated system is neither created nor destroyed by chemical reactions or physical transformations.

Step 2: Apply the law to a chemical reaction.

In the context of a chemical reaction, this law means that the total mass of the reactants before the reaction must be equal to the total mass of the products after the reaction. Atoms are rearranged, but their total quantity and mass remain constant.

Step 3: Evaluate the given options based on the law.

- **(1) the sum of the masses of all reactants is not equal to sum of masses of all products:** This statement contradicts the Law of Conservation of Mass.
- **(2) the sum of masses of all reactants is equal to the sum of masses of all products:** This statement accurately reflects the Law of Conservation of Mass.
- **(3) the sum of the masses of all reactants is equal to half of sum of masses of all products:** This statement contradicts the Law of Conservation of Mass.

- (4) the sum of masses of all reactants is equal to double of sum of masses of all products: This statement contradicts the Law of Conservation of Mass.

Step 4: Conclude the correct statement.

The Law of Conservation of Mass states that during a chemical reaction, the sum of the masses of all reactants is equal to the sum of the masses of all products.

- (2) the sum of masses of all reactants is equal to the sum of masses of all products.

Quick Tip

The Law of Conservation of Mass is often demonstrated by balancing chemical equations, where the number of atoms of each element remains constant on both sides of the reaction.

107. Composition of the nuclei of two atomic species A and B are given as under :

	A	B
Protons	6	6
Neutrons	6	8

Choose the correct relationship between A and B ?

- (1) A and B are Isotopes
- (2) A and B are Isobars
- (3) A and B are Isotones
- (4) A and B are Isomers

Correct Answer: (1) A and B are Isotopes

Solution: Step 1: Understand the definitions of isotopes, isobars, isotones, and isomers.

- **Isotopes:** Atoms of the same element that have the same number of protons but different numbers of neutrons. Consequently, they have the same atomic number but different mass numbers.

- **Isobars:** Atoms of different elements that have the same mass number (sum of protons and neutrons) but different atomic numbers (different number of protons).
- **Isotones:** Atoms of different elements that have the same number of neutrons but different numbers of protons.
- **Isomers:** Compounds with the same molecular formula but different arrangements of atoms in space. This term is used in organic chemistry and refers to molecules, not atomic species in this context.

Step 2: Analyze the composition of atomic species A and B.

- **Species A:**

- Protons = 6
- Neutrons = 6
- Mass number (Protons + Neutrons) = $6 + 6 = 12$

- **Species B:**

- Protons = 6
- Neutrons = 8
- Mass number (Protons + Neutrons) = $6 + 8 = 14$

Step 3: Compare A and B based on their composition.

- Both A and B have the same number of protons (6). This means they are atoms of the same element (Carbon, since atomic number 6 is Carbon).
- A has 6 neutrons, while B has 8 neutrons. They have different numbers of neutrons.
- A has a mass number of 12, while B has a mass number of 14. They have different mass numbers.

Step 4: Choose the correct relationship.

Since A and B have the same number of protons (same atomic number) but different numbers of neutrons (different mass numbers), they are isotopes.

(1) A and B are Isotopes

Quick Tip

Remember these definitions for atomic species:

- Isotopes: Same protons, different neutrons.
- Isobars: Different protons, same total mass (protons + neutrons).
- Isotones: Different protons, same neutrons.

Focus on the number of protons and neutrons to classify them correctly.

108. Which one of the following is a correct electronic configuration of Ne atom ?

- (1) 2,8
- (2) 2,7
- (3) 2,6
- (4) 2,5

Correct Answer: (1) 2,8

Solution: Step 1: Identify the element and its atomic number.

The element is Ne, which stands for Neon.

Neon (Ne) is an element in Group 18 of the periodic table, which are the noble gases.

The atomic number of Neon (Ne) is 10. The atomic number represents the total number of electrons in a neutral atom.

Step 2: Determine the electronic configuration based on the atomic number.

The electrons in an atom fill electron shells in a specific order:

- The first shell (K shell) can hold a maximum of 2 electrons.
- The second shell (L shell) can hold a maximum of 8 electrons.
- The third shell (M shell) can hold a maximum of 18 electrons, and so on.

For a neutral Neon atom with 10 electrons:

- The first shell will be completely filled with 2 electrons.
- The remaining electrons ($10 - 2 = 8$) will go into the second shell.

- The second shell will be completely filled with 8 electrons.

Therefore, the electronic configuration of Neon is 2, 8.

Step 3: Compare the derived configuration with the given options.

- (1) 2,8: This matches the derived electronic configuration.
- (2) 2,7: This configuration has a total of 9 electrons, corresponding to Fluorine (F).
- (3) 2,6: This configuration has a total of 8 electrons, corresponding to Oxygen (O).
- (4) 2,5: This configuration has a total of 7 electrons, corresponding to Nitrogen (N).

Step 4: Conclude the correct electronic configuration.

The correct electronic configuration for a Neon (Ne) atom is 2,8.

(1) 2,8

Quick Tip

Remember the maximum number of electrons each shell can hold (2 for K, 8 for L, 18 for M, etc.). For noble gases like Neon, their outermost shell is completely filled, which is why they are stable and unreactive.

109. Which one of the following pairs is showing a correct isotopes of Cl atom?

- (1) Chlorine. ^{34}Cl and ^{37}Cl
- (2) Chlorine. ^{35}Cl and ^{36}Cl
- (3) Chlorine. ^{35}Cl and ^{37}Cl
- (4) Chlorine. ^{35}Cl and ^{35}Cl

Correct Answer: (3) Chlorine. ^{35}Cl and ^{37}Cl

Solution:

Step 1: Understand the definition of isotopes.

Isotopes are atoms of the same element that have the same number of protons (and thus the same atomic number) but different numbers of neutrons. This difference in neutrons results in different mass numbers. For an element, the atomic number (Z) is fixed.

Step 2: Recall the atomic number of Chlorine (Cl).

Chlorine (Cl) has an atomic number of 17. This means all isotopes of chlorine must have 17 protons.

Step 3: Analyze the common isotopes of Chlorine.

The most common isotopes of chlorine are Chlorine-35 (^{35}Cl) and Chlorine-37 (^{37}Cl).

- ^{35}Cl has 17 protons and $35 - 17 = 18$ neutrons.
- ^{37}Cl has 17 protons and $37 - 17 = 20$ neutrons.

Both have the same atomic number (17) but different mass numbers (35 and 37), which fits the definition of isotopes.

Step 4: Evaluate the given options.

- **(1) Chlorine. ^{34}Cl and ^{37}Cl :** While ^{34}Cl is an isotope, ^{35}Cl and ^{37}Cl are the most prevalent and typically referred to common stable isotopes. However, fundamentally, ^{34}Cl and ^{37}Cl would also be isotopes of chlorine as long as they both have 17 protons. But when asked for "correct isotopes," it usually refers to the most recognized or stable ones.
- **(2) Chlorine. ^{35}Cl and ^{36}Cl :** ^{36}Cl is a radioactive isotope of chlorine. This pair shows two isotopes.
- **(3) Chlorine. ^{35}Cl and ^{37}Cl :** This pair represents the two most abundant and stable natural isotopes of chlorine. They both have the same atomic number (17) but different mass numbers (35 and 37). This is a correct pair of isotopes.
- **(4) Chlorine. ^{35}Cl and ^{35}Cl :** This represents the same isotope, not a pair of different isotopes.

Step 5: Select the best fit.

Among the given options, the pair ^{35}Cl and ^{37}Cl is the most commonly recognized and correct example of naturally occurring isotopes of Chlorine.

(3) Chlorine. ^{35}Cl and ^{37}Cl

Quick Tip

Isotopes of an element always have the same atomic number (number of protons) but different mass numbers (due to different numbers of neutrons).

110. The atomic number of an element is the same as the number of :

- (1) Neutrons in the nucleus of its atom.
- (2) sum of the number of protons and Neutrons in the nucleus of its atom.
- (3) sum of the number of protons and electrons in the nucleus of its atom.
- (4) protons in the nucleus of its atom.

Correct Answer: (4) protons in the nucleus of its atom.

Solution:

Step 1: Define atomic number.

The atomic number (Z) of a chemical element is defined as the number of protons found in the nucleus of every atom of that element. It uniquely identifies a chemical element.

Step 2: Evaluate each option based on the definition.

- **(1) Neutrons in the nucleus of its atom:** The number of neutrons can vary for isotopes of the same element, so it does not define the atomic number.
- **(2) sum of the number of protons and Neutrons in the nucleus of its atom:** This sum defines the mass number (or atomic mass number), not the atomic number.
- **(3) sum of the number of protons and electrons in the nucleus of its atom:** Electrons are located outside the nucleus, not in it. Also, the sum of protons and electrons is not the definition of the atomic number. In a neutral atom, the number of electrons equals the number of protons, but the atomic number is fundamentally defined by protons.
- **(4) protons in the nucleus of its atom:** This statement perfectly matches the definition of the atomic number.

Step 3: Conclude the correct statement.

The atomic number of an element is solely determined by the number of protons in the nucleus of its atom.

(4) protons in the nucleus of its atom.

Quick Tip

Atomic number = Number of protons. Mass number = Number of protons + Number of neutrons. In a neutral atom, Number of protons = Number of electrons.

111. Rutherford's alpha-particle scattering experiment was responsible for the discovery of:

- (1) atomic nucleus
- (2) electron
- (3) number of proton
- (4) number of neutron

Correct Answer: (1) atomic nucleus

Solution:

Step 1: Understand Rutherford's Alpha-Particle Scattering Experiment.

In 1909, Ernest Rutherford conducted an experiment where alpha particles were directed at a thin gold foil. The results of this experiment led to the discovery of the atomic nucleus. Key observations from the experiment include:

1. Most alpha particles passed straight through the foil without deflection.
2. A small fraction of alpha particles were deflected at large angles, indicating that they encountered a concentrated region of positive charge within the atom.

These observations contradicted the prevailing "plum pudding" model of the atom proposed by J.J. Thomson, which suggested that the positive charge was uniformly distributed throughout the atom. Instead, Rutherford concluded that the positive charge (and most of the mass) must be concentrated in a small, dense region at the center of the atom, now known as the atomic nucleus.

Step 2: Analyze Each Option.

Option (1): atomic nucleus — Correct, as Rutherford's experiment directly led to the discovery of the atomic nucleus.

Option (2): electron — Incorrect, as electrons were discovered earlier by J.J. Thomson using cathode ray experiments.

Option (3): number of proton — Incorrect, as the number of protons was not directly

determined by this experiment.

Option (4): number of neutron — Incorrect, as neutrons were discovered later by James Chadwick in 1932.

Step 3: Final Answer.

(1) atomic nucleus

Quick Tip

Rutherford's alpha-particle scattering experiment provided crucial evidence for the existence of the atomic nucleus. It demonstrated that the positive charge and most of the mass of an atom are concentrated in a very small region at the center, challenging the previous models of atomic structure.

112. In which conditions rusting of iron takes place in presence of:

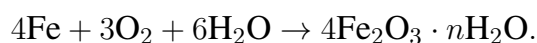
- (1) 'air'
- (2) H_2O
- (3) 'air' and ' H_2O '
- (4) Only ' N_2 '

Correct Answer: (3) 'air' and ' H_2O '

Solution:

Step 1: Understand Rusting of Iron.

Rusting is the process of corrosion of iron or steel due to the reaction with oxygen and water. The chemical reaction involved in rusting can be summarized as:



This equation shows that both oxygen (from air) and water are essential for the rusting process. Without either of these components, rusting cannot occur.

Step 2: Analyze Each Option.

Option (1): 'air' — Incorrect, as rusting requires both air (for oxygen) and water.

Option (2): H_2O — Incorrect, as rusting requires both air (for oxygen) and water.

Option (3): 'air' and ' H_2O ' — Correct, as both air (for oxygen) and water are necessary for

rusting.

Option (4): Only ' N_2 ' — Incorrect, as nitrogen (N_2) does not participate in the rusting process.

Step 3: Final Answer.

(3) 'air' and ' H_2O '

Quick Tip

Rusting of iron is an electrochemical process that requires both oxygen (from air) and water. The presence of both air and water creates the ideal conditions for the formation of iron oxide hydrate (rust). Nitrogen does not play a role in this process.

113. Which metals are kept in kerosene?

- (1) Na & K
- (2) Zn
- (3) Cu
- (4) Fe

Correct Answer: (1) Na & K

Solution: Step 1: Understand the reactivity of metals.

Some metals are highly reactive and readily react with air (oxygen and moisture) and water. To prevent these reactions and ensure their safe storage, they are often stored under a protective layer of a substance that prevents contact with air and moisture.

Step 2: Evaluate the reactivity of the given metals.

- **Sodium (Na) and Potassium (K):** These are alkali metals, located in Group 1 of the periodic table. They are extremely reactive metals. They react vigorously with oxygen in the air (even at room temperature, causing them to tarnish rapidly) and violently with water, releasing hydrogen gas which can ignite due to the heat generated. Therefore, they need to be stored in an inert medium.
- **Zinc (Zn):** Zinc is a moderately reactive metal. It reacts with oxygen in the air to form a protective layer of zinc oxide, which prevents further corrosion. It does not react vigorously with water at room temperature.

- **Copper (Cu):** Copper is a relatively unreactive metal. It slowly reacts with atmospheric gases over time to form a greenish patina (copper carbonate), but it does not react with water or oxygen rapidly at room temperature.
- **Iron (Fe):** Iron is a moderately reactive metal. It reacts with oxygen and moisture in the air to form rust (hydrated iron(III) oxide), but this process is slow and does not require storage in kerosene.

Step 3: Determine the appropriate storage method.

Kerosene is an organic solvent and does not react with highly reactive metals like sodium and potassium. It acts as a barrier, preventing their contact with air and moisture. Therefore, sodium and potassium are stored in kerosene to prevent their highly exothermic reactions with oxygen and water.

(1) Na & K

Quick Tip

Highly reactive metals like alkali metals (Group 1 elements such as Na and K) are stored under kerosene or paraffin oil to prevent their rapid and dangerous reactions with atmospheric oxygen and moisture. Less reactive metals do not require such specialized storage.

114. Conductivity of metal's is due to :

- (1) Free Electrons
- (2) Ions
- (3) atoms
- (4) Nutrons

Correct Answer: (1) Free Electrons

Solution: Step 1: Understand the nature of metallic bonding.

Metals are characterized by metallic bonding, where a "sea" of delocalized electrons exists. These electrons are not rigidly associated with any single atom but are free to move throughout the entire metallic structure. The metal atoms (nuclei and inner-shell electrons)

form a fixed lattice of positive ions within this sea of electrons.

Step 2: Relate metallic bonding to electrical conductivity.

For a material to conduct electricity, it must have mobile charge carriers. In metals, these mobile charge carriers are the free (delocalized) electrons. When a potential difference (voltage) is applied across a metal, these free electrons move collectively towards the positive terminal, constituting an electric current.

Step 3: Evaluate the given options.

- (1) **Free Electrons:** This aligns perfectly with the explanation of metallic conductivity. The presence of delocalized electrons allows for the flow of charge.
- (2) **Ions:** While metals consist of positive metal ions, these ions are generally fixed in the crystal lattice and do not move freely to conduct electricity in solid metals. (Ions are mobile in molten metals or ionic solutions, leading to conductivity there, but not typically in solid metals as the primary mechanism).
- (3) **atoms:** Atoms themselves are neutral and fixed in the lattice; they do not directly contribute to the flow of electric current as charge carriers.
- (4) **Neutrons:** Neutrons are neutral particles found in the nucleus of an atom. They do not carry an electric charge and therefore do not contribute to electrical conductivity.

Step 4: Conclude the primary reason for metal conductivity.

The conductivity of metals is primarily due to the presence of free (delocalized) electrons.

(1) Free Electrons

Quick Tip

The key to understanding electrical conductivity in metals is the concept of "free" or "delocalized" electrons. These electrons are loosely bound to the atoms and can move freely throughout the metal lattice, carrying electric charge.

115. What is the formula of plaster of Paris?

(1) CaSO_4

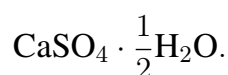


Correct Answer: (2) $\text{CaSO}_4 \cdot \frac{1}{2}\text{H}_2\text{O}$

Solution:

Step 1: Understand Plaster of Paris.

Plaster of Paris is a form of calcium sulfate hemihydrate, which is obtained by heating gypsum ($\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$). Its chemical formula is:



Step 2: Analyze Each Option.

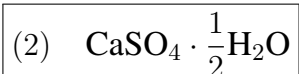
Option (1): CaSO_4 — Incorrect, as this is the formula for anhydrous calcium sulfate, not plaster of Paris.

Option (2): $\text{CaSO}_4 \cdot \frac{1}{2}\text{H}_2\text{O}$ — Correct, as this matches the formula for plaster of Paris.

Option (3): $\text{CaSO}_4 \cdot \text{H}_2\text{O}$ — Incorrect, as this is the formula for gypsum, not plaster of Paris.

Option (4): CaSO_3 — Incorrect, as this is the formula for calcium sulfite, not plaster of Paris.

Step 3: Final Answer.



Quick Tip

Plaster of Paris is a specific form of calcium sulfate hemihydrate, with the formula $\text{CaSO}_4 \cdot \frac{1}{2}\text{H}_2\text{O}$. It is commonly used in construction and medical applications due to its rapid setting properties when mixed with water.

116. Bleaching Powder is mixed in drinking water. Why?

(1) To kill the germs

(2) As an oxidizing agent

(3) '1' & '2'

(4) None of these

Correct Answer: (3) '1' & '2'

Solution:

Step 1: Understand Bleaching Powder.

Bleaching powder, also known as calcium hypochlorite ($\text{Ca}(\text{OCl})_2$), is a strong oxidizing agent. When added to drinking water, it serves two primary purposes:

1. To Kill Germs:

Bleaching powder acts as a disinfectant, killing bacteria and other microorganisms present in the water. This ensures that the water is safe for consumption by eliminating harmful pathogens.

2. As an Oxidizing Agent:

The oxidizing properties of bleaching powder help break down organic matter and contaminants in the water, improving its purity and safety.

Step 2: Analyze Each Option.

Option (1): To kill the germs — Partially correct, as bleaching powder does kill germs, but it has another function.

Option (2): As an oxidizing agent — Partially correct, as bleaching powder is indeed an oxidizing agent, but it has another function.

Option (3): '1' & '2' — Correct, as bleaching powder serves both functions: killing germs and acting as an oxidizing agent.

Option (4): None of these — Incorrect, as options (1) and (2) are valid reasons.

Step 3: Final Answer.

(3) '1' '2'

Quick Tip

Bleaching powder is added to drinking water primarily for its dual role as a disinfectant (to kill germs) and an oxidizing agent (to remove impurities). Both functions contribute to ensuring the water is safe and clean for consumption.

117. Which acid is produced in our stomach ?

(1) HBr

(2) HCl

(3) H_2SO_4

(4) HNO_3

Correct Answer: (2) HCl

Solution:

Step 1: Recall the digestive process in the stomach.

The stomach plays a crucial role in digestion, primarily through the action of gastric juice. Gastric juice contains several components, including enzymes and acid.

Step 2: Identify the specific acid produced in the stomach.

The parietal cells (also called oxyntic cells) in the lining of the stomach are responsible for producing hydrochloric acid (HCl). This acid creates a highly acidic environment (pH 1.5-3.5) necessary for the activation of digestive enzymes like pepsin and for killing harmful bacteria ingested with food.

Step 3: Evaluate the given options.

- **(1) HBr (Hydrobromic acid):** Not produced in the stomach.
- **(2) HCl (Hydrochloric acid):** This is the strong acid produced in the stomach.
- **(3) H_2SO_4 (Sulfuric acid):** Not produced in the stomach; it's a strong industrial acid.
- **(4) HNO_3 (Nitric acid):** Not produced in the stomach; it's a strong industrial acid.

Step 4: Conclude the correct acid.

Hydrochloric acid (HCl) is the acid produced in our stomach.

(2) HCl

Quick Tip

Hydrochloric acid (HCl) in the stomach aids digestion by breaking down food and activating enzymes, as well as providing a defense against pathogens.

118. A Solution turns blue Litmus red, its pH is likely to be :

- (1) 11
- (2) 14
- (3) 5
- (4) 10

Correct Answer: (3) 5

Solution:

Step 1: Understand the litmus paper test and pH scale.

Litmus paper is a common indicator used to test the acidity or alkalinity of a solution.

- Acids turn blue litmus paper red.
- Bases (alkaline solutions) turn red litmus paper blue.
- Neutral solutions do not change the color of either red or blue litmus paper.

The pH scale ranges from 0 to 14:

- $\text{pH} < 7$ indicates an acidic solution.
- $\text{pH} = 7$ indicates a neutral solution.
- $\text{pH} > 7$ indicates a basic (alkaline) solution.

Step 2: Apply the litmus test result to determine the nature of the solution.

The problem states that "A Solution turns blue Litmus red". This indicates that the solution is acidic.

Step 3: Use the pH scale to find a likely pH value for an acidic solution.

Since the solution is acidic, its pH must be less than 7.

Step 4: Evaluate the given options.

- **(1) 11:** This pH is greater than 7, indicating a basic solution. A basic solution would turn red litmus blue, not blue litmus red.
- **(2) 14:** This pH is strongly basic. A strongly basic solution would turn red litmus blue.
- **(3) 5:** This pH is less than 7, indicating an acidic solution. An acidic solution would turn blue litmus red. This is a likely pH.
- **(4) 10:** This pH is greater than 7, indicating a basic solution.

Step 5: Conclude the likely pH.

Based on the litmus test, the solution is acidic, and among the given options, pH 5 is the only value that corresponds to an acidic solution.

Quick Tip

"Acids turn blue litmus RED, Bases turn red litmus BLUE." Remember the mnemonic: "Acid-Red" or "BAR" (Blue to Acid to Red). A pH value below 7 confirms acidity.

119. A Solution reacts with egg-shell to give CO₂ gas, the Solution contains :

- (1) Mg Cl₂
- (2) Na Cl
- (3) KCl
- (4) HCl

Correct Answer: (4) HCl

Solution: Step 1: Understand the composition of egg-shell.

Egg-shells are primarily composed of calcium carbonate (CaCO₃).

Step 2: Recall the reaction of carbonates with acids.

Carbonates react with acids to produce carbon dioxide (CO₂) gas, water (H₂O), and a salt.

This is a characteristic test for the presence of carbonates.

Step 3: Analyze the given options.

- (1) MgCl₂ (Magnesium Chloride): This is a salt and typically does not react with calcium carbonate to produce CO₂ gas.
- (2) NaCl (Sodium Chloride): This is a salt and typically does not react with calcium carbonate to produce CO₂ gas.
- (3) KCl (Potassium Chloride): This is a salt and typically does not react with calcium carbonate to produce CO₂ gas.
- (4) HCl (Hydrochloric Acid): This is a strong acid. When HCl reacts with calcium carbonate, it produces calcium chloride (a salt), water, and carbon dioxide gas.

Step 4: Write the chemical reaction.



Step 5: Conclude the correct solution.

Since the reaction with egg-shell (calcium carbonate) produces CO_2 gas, the solution must contain an acid. Among the given options, HCl is an acid.

(4) HCl

Quick Tip

Remember that carbonates (like in egg-shells) react with acids to produce carbon dioxide gas. This is a common chemical test for both carbonates and acids.

120. What happens; When dilute ' HCl ' is added to granulated ' Zn ' ?

- (1) ' H_2 ' gas and ' ZnCl_2 ' are Produced
- (2) No Reaction Produced
- (3) ' H_2O ' and ' ZnO ' are Produced
- (4) H_2O and ZnSO_4 are Produced

Correct Answer: (1) ' H_2 ' gas and ' ZnCl_2 ' are Produced

Solution: Step 1: Identify the reactants.

The reactants are dilute hydrochloric acid (HCl) and granulated zinc (Zn). Zinc is a metal, and hydrochloric acid is a strong acid.

Step 2: Recall the reaction of metals with acids.

When a reactive metal reacts with a dilute acid, it typically displaces hydrogen from the acid to form a salt and hydrogen gas. The reactivity series of metals helps determine if a metal will react with an acid. Zinc is more reactive than hydrogen, so it will displace hydrogen from HCl .

Step 3: Write the chemical reaction.

The reaction between zinc and hydrochloric acid is a single displacement reaction: $\text{Zn(s)} + 2\text{HCl(aq)} \rightarrow \text{ZnCl}_2\text{(aq)} + \text{H}_2\text{(g)}$

- Zinc (Zn) reacts with hydrochloric acid (HCl).
- Zinc chloride (ZnCl_2) is formed as the salt.
- Hydrogen gas (H_2) is released.

Step 4: Evaluate the given options.

- (1) 'H₂' gas and 'ZnCl₂' are Produced: This matches the predicted products of the reaction.
- (2) No Reaction Produced: This is incorrect as zinc is more reactive than hydrogen.
- (3) 'H₂O' and 'ZnO' are Produced: This is incorrect. ZnO would be produced if zinc reacted with oxygen, and H₂O is not a primary product of this type of displacement reaction.
- (4) H₂O and ZnSO₄ are Produced: This is incorrect. ZnSO₄ (zinc sulfate) would be formed if zinc reacted with sulfuric acid, not hydrochloric acid.

Step 5: Conclude the correct products.

When dilute HCl is added to granulated Zn, hydrogen gas and zinc chloride are produced.

(1) 'H₂' gas and 'ZnCl₂' are Produced**Quick Tip**

Remember the general rule for reactive metals and dilute acids: Metal + Acid → Salt + Hydrogen gas. This is a fundamental type of displacement reaction.

121. Among the following, what is used to check the rate of transpiration?

- (1) Barometer
- (2) Potometer
- (3) Hygrometer
- (4) Galvanometer

Correct Answer: (2) Potometer

Solution:**Step 1: Understand Transpiration.**

Transpiration is the process by which plants lose water through their leaves, stems, or other parts. To measure the rate of transpiration, a device called a potometer is commonly used.

Step 2: Analyze Each Option.

Option (1): Barometer — Incorrect, as a barometer measures atmospheric pressure, not transpiration.

Option (2): Potometer — Correct, as a potometer is specifically designed to measure the rate of water uptake by plants, which is directly related to transpiration.

Option (3): Hygrometer — Incorrect, as a hygrometer measures humidity, not transpiration.

Option (4): Galvanometer — Incorrect, as a galvanometer measures electrical current, not transpiration.

Step 3: Final Answer.

(2) Potometer

Quick Tip

A potometer is a specialized instrument used to measure the rate of water uptake by plants, which is closely linked to the rate of transpiration. It works by monitoring the movement of water through a plant's xylem under controlled conditions.

122. New plants grown up by using the tip of a plant is known as:

- (1) Regeneration
- (2) Tissue culture
- (3) Grafting
- (4) Layering

Correct Answer: (4) Layering

Solution:

Step 1: Understand Plant Propagation Methods.

Plants can be propagated using various methods, including:

1. **Regeneration:** This refers to the natural process by which plants regrow damaged or lost parts, such as roots or shoots. It is not specific to growing new plants from tips.
2. **Tissue Culture:** This is a laboratory technique where plant tissues are grown in a nutrient medium to produce new plants. While effective, it does not involve using the tip of a plant.
3. **Grafting:** This involves joining parts of two different plants together to form a single plant. It is not specific to using the tip of a plant.

4. Layering: This is a method of propagation where a branch or stem is bent down and buried in soil while still attached to the parent plant. The tip of the branch is often used to initiate root growth, resulting in a new plant.

Step 2: Analyze Each Option.

Option (1): Regeneration — Incorrect, as regeneration is not specific to using the tip of a plant.

Option (2): Tissue culture — Incorrect, as tissue culture is a laboratory technique and does not involve using the tip of a plant. Option (3): Grafting — Incorrect, as grafting involves joining two plants, not using the tip of a single plant.

Option (4): Layering — Correct, as layering specifically uses the tip of a plant to grow new roots and form a new plant.

Step 3: Final Answer.

(4) Layering

Quick Tip

Layering is a propagation technique where a branch or stem is bent down and buried in soil, allowing the tip to develop roots and eventually form a new plant. It is a common method for propagating many types of plants, especially those with flexible stems.

123. Respiration is a :

- (1) Biochemical reaction
- (2) Electro Chemical reaction
- (3) Physical action
- (4) None of these

Correct Answer: (1) Biochemical reaction

Solution: Step 1: Define Respiration.

Respiration, in biology, refers to the metabolic process by which living organisms obtain energy (ATP) by oxidizing nutrients and releasing waste products. This process involves a series of complex chemical reactions occurring within cells.

Step 2: Characterize the nature of these reactions.

- **Biochemical reaction:** These are chemical reactions that occur within living organisms, catalyzed by enzymes. Respiration fits this description perfectly as it involves the breakdown of glucose (or other organic molecules) through a series of enzyme-catalyzed steps to release energy.
- **Electrochemical reaction:** These involve the transfer of electrons and are related to electricity generation (like in batteries) or electrolysis. While cellular respiration involves electron transport (e.g., in the electron transport chain), the overall process is broadly classified as a biochemical reaction due to its complexity and occurrence within biological systems. It's not primarily an electrochemical reaction in the sense of a battery.
- **Physical action:** A physical action involves movement or mechanical changes without altering the chemical composition of substances (e.g., breathing, walking). Respiration, while involving physical acts like breathing (external respiration), fundamentally involves chemical changes at the cellular level.

Step 3: Conclude the most accurate classification. Given that respiration involves a complex series of enzyme-catalyzed chemical transformations of organic molecules within living cells to produce energy, it is most accurately classified as a biochemical reaction.

(1) Biochemical reaction

Quick Tip

Respiration is a fundamental biological process involving the chemical breakdown of food to release energy. Any chemical reaction occurring within a living system and mediated by biological molecules (like enzymes) is termed a biochemical reaction.

124. The enzyme 'pepsin' is inactive in stomach without the presence of :

- (1) Nitric Acid
- (2) Hydrochloric Acid
- (3) Acetic Acid
- (4) Butyric Acid

Correct Answer: (2) Hydrochloric Acid

Solution:

Step 1: Understand the function of pepsin.

Pepsin is a protease enzyme in the stomach that initiates protein digestion. It is secreted by the chief cells of the stomach lining in an inactive form called pepsinogen to prevent it from digesting the stomach wall itself.

Step 2: Identify the condition required for pepsin's activation.

Pepsinogen requires an acidic environment to convert into active pepsin. The stomach provides this acidic environment through the secretion of a specific acid.

Step 3: Determine which acid is present in the stomach.

The stomach secretes hydrochloric acid (HCl), which creates a highly acidic environment (pH typically between 1.5 and 3.5). This low pH is crucial for the activation of pepsinogen to pepsin and for pepsin's optimal activity.

Step 4: Evaluate the given options.

- (1) Nitric Acid: Not naturally present in the stomach.
- (2) Hydrochloric Acid: This is the acid secreted by the stomach lining, essential for activating pepsinogen to pepsin and for its function.
- (3) Acetic Acid: Not naturally present in the stomach in significant amounts to activate pepsin.
- (4) Butyric Acid: Not naturally present in the stomach.

Step 5: Conclude the correct acid.

The enzyme pepsin is inactive in the stomach without the presence of Hydrochloric Acid, which provides the necessary acidic environment for its activation.

(2) Hydrochloric Acid

Quick Tip

The stomach's highly acidic environment, primarily due to hydrochloric acid, is vital for two main reasons: activating pepsinogen into active pepsin for protein digestion and killing most bacteria ingested with food.

125. Contraction of the protoplast of a plant cell as a result of loss of water from the cell is :

- (1) Endocytosis
- (2) Plasmolysis
- (3) Exocytosis
- (4) Lysis

Correct Answer: (2) Plasmolysis

Solution:

Step 1: Understand the process of water movement in cells.

Water moves across cell membranes by osmosis, from an area of higher water concentration (lower solute concentration) to an area of lower water concentration (higher solute concentration).

Step 2: Define the terms related to cell volume changes.

- **Plasmolysis:** This is the process where the protoplast (the living part of the plant cell, including the cell membrane, cytoplasm, and nucleus) shrinks and pulls away from the cell wall when the cell loses water due to being placed in a hypertonic solution (a solution with a higher solute concentration than the cell's cytoplasm).
- **Endocytosis:** This is the process by which cells take in substances from outside by engulfing them in a vesicle formed from the cell membrane. It involves the inward budding of the cell membrane.
- **Exocytosis:** This is the process by which cells release substances outside the cell by fusing a vesicle containing the substance with the cell membrane. It involves the outward budding of the cell membrane.

- **Lysis:** This refers to the bursting or disintegration of a cell, typically due to excessive water intake (in hypotonic solutions for animal cells) or damage to the cell membrane. Plant cells are usually protected from lysis by their rigid cell wall in hypotonic solutions.

Step 3: Relate the given description to the definitions.

The question describes "Contraction of the protoplast of a plant cell as a result of loss of water from the cell". This precisely matches the definition of plasmolysis.

Step 4: Conclude the correct term.

The phenomenon described is plasmolysis.

(2) Plasmolysis

Quick Tip

Plasmolysis is a unique phenomenon observed in plant cells due to their rigid cell wall. When a plant cell loses water in a hypertonic environment, its protoplast shrinks and pulls away from the cell wall, but the cell wall itself retains its shape.

126. Two cell organelles who has its own genetic material:

- (1) Mitochondria and vacuoles
- (2) Plastids and vacuoles
- (3) Mitochondria and Plastids
- (4) Endoplasmic Reticulum and Mitochondria

Correct Answer: (3) Mitochondria and Plastids

Solution:

Step 1: Understand what "own genetic material" implies for organelles.

Having "own genetic material" means the organelle contains its own DNA and often its own ribosomes, allowing it to synthesize some of its own proteins, independent of the cell's nucleus. This is a key feature supporting the endosymbiotic theory.

Step 2: Review the common organelles and their genetic material status.

- **Mitochondria:** These are known as the "powerhouses" of the cell. They contain their own circular DNA (mtDNA) and ribosomes, which enable them to produce some of their own proteins.

- **Plastids:** This group includes chloroplasts (in plant cells, responsible for photosynthesis), chromoplasts, and leucoplasts. Chloroplasts, in particular, possess their own circular DNA (cpDNA) and ribosomes, similar to mitochondria.
- **Vacuoles:** These are membrane-bound sacs involved in storage and waste removal. They do not have their own genetic material.
- **Endoplasmic Reticulum (ER):** This is a network of membranes involved in protein and lipid synthesis. It does not have its own genetic material; its functions are directed by nuclear DNA.

Step 3: Evaluate the given pairs based on the information.

- **(1) Mitochondria and vacuoles:** Mitochondria have genetic material, but vacuoles do not.
- **(2) Plastids and vacuoles:** Plastids have genetic material, but vacuoles do not.
- **(3) Mitochondria and Plastids:** Both mitochondria and plastids (like chloroplasts) are known to contain their own DNA and ribosomes. This is a correct pair.
- **(4) Endoplasmic Reticulum and Mitochondria:** Mitochondria have genetic material, but the Endoplasmic Reticulum does not.

Step 4: Conclude the correct pair.

Mitochondria and Plastids are the two cell organelles that possess their own genetic material.

(3) Mitochondria and Plastids

Quick Tip

Mitochondria and chloroplasts (a type of plastid) are unique among organelles for having their own DNA, which supports the endosymbiotic theory suggesting they originated from free-living prokaryotes.

127. Plasma contains:

- (1) Red Blood Cells, White Blood Cells, and Platelets.
- (2) Red Blood Cells, Fats, Hormones, and Platelets.

(3) White Blood Cells, Fats, Hormones, and Platelets.

(4) Red Blood Cells, Plastids, and Platelets.

Correct Answer: (3) White Blood Cells, Fats, Hormones, and Platelets.

Solution:

Step 1: Understand Plasma Composition. Plasma is the liquid component of blood that makes up about 55% of its volume. It is primarily composed of water (about 90%) and dissolved substances such as:

Proteins: Including albumin, globulins, and fibrinogen.

Electrolytes: Such as sodium, potassium, calcium, and chloride ions.

Hormones: Various hormones produced by endocrine glands.

Fats: Lipids and cholesterol.

Other Solutes: Nutrients, waste products, and gases like carbon dioxide.

However, plasma does not contain cells such as red blood cells, white blood cells, or platelets. These cellular components are suspended in the plasma but are not part of it.

Step 2: Analyze Each Option.

Option (1): Red Blood Cells, White Blood Cells, and Platelets. — Incorrect, as these are not components of plasma; they are suspended in plasma.

Option (2): Red Blood Cells, Fats, Hormones, and Platelets. — Incorrect, as red blood cells and platelets are not components of plasma.

Option (3): White Blood Cells, Fats, Hormones, and Platelets. — Incorrect, as white blood cells and platelets are not components of plasma.

Option (4): Red Blood Cells, Plastids, and Platelets. — Incorrect, as red blood cells and platelets are not components of plasma, and plastids are organelles found in plant cells, not blood components.

Step 3: Final Answer.

(3) White Blood Cells, Fats, Hormones, and Platelets.

Quick Tip

Plasma is the fluid component of blood that contains dissolved substances like proteins, electrolytes, hormones, and fats. It does not include blood cells or platelets, which are suspended within it.

128. Name the type of epithelial tissue which forms the lining of kidney tubules and ducts of salivary glands:

- (1) Cuboidal epithelium
- (2) Stratified squamous epithelium
- (3) Ciliated Columnar epithelium
- (4) Glandular epithelium

Correct Answer: (3) Ciliated Columnar epithelium

Solution:

Step 1: Understand Epithelial Tissue Types.

Epithelial tissues are classified based on their shape and arrangement. The specific type of epithelial tissue that lines kidney tubules and ducts of salivary glands is ciliated columnar epithelium. This tissue is characterized by:

Columnar cells: Tall, column-shaped cells that provide a large surface area for absorption or secretion.

Cilia: Hair-like structures on the free surface of the cells that help move substances along the surface (e.g., mucus in the respiratory tract).

Step 2: Analyze Each Option.

Option (1): Cuboidal epithelium — Incorrect, as cuboidal epithelium consists of cube-shaped cells and is not typically found in kidney tubules or salivary gland ducts.

Option (2): Stratified squamous epithelium — Incorrect, as stratified squamous epithelium consists of multiple layers of flat cells and is found in areas requiring protection, such as the skin and lining of the mouth.

Option (3): Ciliated Columnar epithelium — Correct, as this is the type of epithelium found in kidney tubules and salivary gland ducts.

Option (4): Glandular epithelium — Incorrect, as glandular epithelium is specialized for

secretion and does not form the lining of kidney tubules or salivary gland ducts.

Step 3: Final Answer.

(3) Ciliated Columnar epithelium

Quick Tip

Ciliated columnar epithelium is characterized by tall, column-shaped cells with cilia on their free surface. It is commonly found in structures like kidney tubules and salivary gland ducts, where it helps facilitate movement of substances through ciliary action.

129. Antedon (Feather Star) is an example of :

- (1) Protochordata
- (2) Echinodermata
- (3) Mollusca
- (4) Arthropoda

Correct Answer: (2) Echinodermata

Solution:

Step 1: Identify the organism in question.

The organism is Antedon, also commonly known as Feather Star.

Step 2: Recall the characteristics of the major animal phyla.

- **Protochordata:** These are primitive chordates, typically marine, filter feeders, and include organisms like tunicates and lancelets. They possess a notochord at some stage of development.
- **Echinodermata:** This phylum consists of marine invertebrates characterized by radial symmetry (usually pentaradial in adults), a spiny skin, and a water vascular system. Examples include starfish, sea urchins, brittle stars, sea cucumbers, and crinoids (like feather stars).
- **Mollusca:** This phylum includes soft-bodied invertebrates, many of which have a hard shell. Examples include snails, clams, octopuses, and squids.
- **Arthropoda:** This is the largest phylum in the animal kingdom, characterized by

segmented bodies, jointed appendages, and an exoskeleton. Examples include insects, spiders, crustaceans, and myriapods.

Step 3: Classify Antedon based on its characteristics.

Antedon, or the Feather Star, belongs to the class Crinoidea within the phylum Echinodermata. They exhibit radial symmetry and possess features characteristic of echinoderms.

Step 4: Compare with the given options.

(1) Protochordata: Incorrect.

(2) Echinodermata: Correct, as Feather Stars are a type of echinoderm. (3) Mollusca: Incorrect.

(4) Arthropoda: Incorrect.

(2) Echinodermata

Quick Tip

Echinoderms are exclusively marine animals known for their radial symmetry, often spiny skin, and tube feet operated by a water vascular system. Feather stars are a classic example of this group.

130. Sleeping sickness is caused by:

(1) Protozoan Trypanosoma

(2) SARS Bacteria

(3) Staphylococcus Bacteria

(4) Protozoan Leishmania

Correct Answer: (1) Protozoan Trypanosoma

Solution:

Step 1: Identify the disease in question.

The disease is Sleeping Sickness, also known as Human African Trypanosomiasis (HAT).

Step 2: Recall the causative agents of common diseases.

- **Sleeping Sickness (Human African Trypanosomiasis):** This disease is caused by protozoan parasites of the genus Trypanosoma. Specifically, Trypanosoma brucei

rhodesiense and Trypanosoma brucei gambiense are the subspecies responsible for the disease in humans. It is transmitted by the tsetse fly.

- **SARS:** SARS (Severe Acute Respiratory Syndrome) is caused by a virus (SARS-CoV), not bacteria.
- **Staphylococcus Bacteria:** Staphylococcus bacteria cause various infections, including skin infections (like boils, impetigo), food poisoning, and more serious conditions like sepsis, but not sleeping sickness.
- **Protozoan Leishmania:** Leishmania protozoans cause Leishmaniasis, a disease with different forms affecting the skin, mucous membranes, or internal organs, transmitted by sandflies. It is distinct from sleeping sickness.

Step 3: Evaluate the given options.

- (1) Protozoan Trypanosoma: This is the correct causative agent for sleeping sickness.
- (2) SARS Bacteria: Incorrect; SARS is viral.
- (3) Staphylococcus Bacteria: Incorrect; Staphylococcus causes different types of bacterial infections.
- (4) Protozoan Leishmania: Incorrect; Leishmania causes Leishmaniasis.

Step 4: Conclude the correct causative agent.

Sleeping sickness is caused by the Protozoan Trypanosoma.

(1) Protozoan Trypanosoma

Quick Tip

Many parasitic diseases are caused by protozoa. Sleeping sickness is a classic example of a protozoan disease, transmitted by an insect vector (tsetse fly).

131. The enzyme that breaks down protein during digestion :

- (1) Trypsin
- (2) Amylase
- (3) Pepsin
- (4) Chymotrypsin

Correct Answer: (3) Pepsin

Solution: Step 1: Understand the role of enzymes in digestion.

Enzymes are biological catalysts that speed up chemical reactions in the body. Different enzymes are specialized to break down specific types of macromolecules like proteins, carbohydrates, and fats.

Step 2: Evaluate each option in the context of protein digestion.

- **(1) Trypsin:** Trypsin is a proteolytic enzyme (protease) secreted by the pancreas into the small intestine, where it helps in breaking down proteins and polypeptides.
- **(2) Amylase:** Amylase is an enzyme that breaks down carbohydrates (starches) into simpler sugars. It is found in saliva and pancreatic juice.
- **(3) Pepsin:** Pepsin is a major proteolytic enzyme found in the stomach. It is responsible for initiating protein digestion in the highly acidic environment of the stomach.
- **(4) Chymotrypsin:** Chymotrypsin is another proteolytic enzyme secreted by the pancreas into the small intestine, working alongside trypsin to further break down proteins.

Step 3: Determine the enzyme that breaks down protein during digestion from the options.

All of Trypsin, Pepsin, and Chymotrypsin break down protein. However, the question asks for "the enzyme" implying a single best fit from the options, or the most prominent one associated with general protein digestion as opposed to a specific stage or location like the small intestine for Trypsin and Chymotrypsin. Pepsin is the enzyme that begins protein digestion in the stomach. Without additional context about where "during digestion" refers to (e.g., stomach, small intestine), Pepsin is a fundamental answer as it initiates the process. However, if multiple options can be considered correct, usually the "best" or most general answer is expected. Trypsin and Chymotrypsin are also correct in that they break down protein during digestion. But often in basic biology questions, Pepsin is highlighted for its role in the stomach.

Given the typical level of these types of questions, Pepsin is the primary enzyme for protein breakdown specifically in the stomach, which is an early and crucial stage of digestion.

(3) Pepsin

Quick Tip

Remember that digestion is a multi-stage process. Pepsin starts protein digestion in the stomach, while trypsin and chymotrypsin continue it in the small intestine. Amylase is for carbohydrate digestion.

132. A plant hormone that cause wilting of leaves is :

- (1) Auxin
- (2) Gibberellin
- (3) Cytokinin
- (4) Absciscic Acid

Correct Answer: (4) Absciscic Acid

Solution: Step 1: Understand the functions of various plant hormones (phytohormones).

Plant hormones are chemical messengers that regulate various physiological processes in plants, including growth, development, and responses to environmental stimuli.

Step 2: Evaluate the function of each hormone listed in the options.

- **(1) Auxin:** Auxins are primarily involved in cell elongation, phototropism, gravitropism, and apical dominance. They generally promote growth.
- **(2) Gibberellin:** Gibberellins play roles in stem elongation, seed germination, and flowering. They generally promote growth.
- **(3) Cytokinin:** Cytokinins promote cell division and differentiation, delay senescence (aging) in leaves, and promote bud development. They generally promote growth.
- **(4) Absciscic Acid (ABA):** Absciscic acid is a stress hormone. It plays a crucial role in regulating plant responses to environmental stresses, such as drought. ABA promotes stomatal closure to reduce water loss, inhibits seed germination, and plays a role in dormancy and leaf senescence (aging and detachment), which can lead to wilting.

Specifically, during water stress, ABA levels increase, causing stomata to close, which reduces transpiration but also leads to wilting if water uptake is insufficient.

Step 3: Identify the hormone associated with wilting.

Absciscic acid is known for its role in stress responses, including causing stomatal closure and promoting processes that lead to wilting and dormancy, especially under water deficit conditions.

(4) Absciscic Acid

Quick Tip

Absciscic Acid (ABA) is often called the "stress hormone" in plants because it mediates responses to adverse conditions like drought, leading to water conservation mechanisms such as stomatal closure and, in severe cases, wilting.

133. The process of purifying blood by an artificial kidney is known as:

- (1) Dialysis
- (2) Haemodialysis
- (3) Filtration
- (4) None of these

Correct Answer: (2) Haemodialysis

Solution:

Step 1: Understand the Process of Blood Purification.

An artificial kidney is used to perform dialysis, a process that removes waste products and excess fluids from the blood when the kidneys are unable to function properly. The specific type of dialysis performed using an artificial kidney is called haemodialysis.

Step 2: Analyze Each Option.

Option (1): Dialysis — Incorrect, as "dialysis" is a general term for the process of removing waste products from the blood. While haemodialysis is a type of dialysis, this option is too broad.

Option (2): Haemodialysis — Correct, as this is the specific process performed using an

artificial kidney.

Option (3): Filtration — Incorrect, as filtration is a broader term that describes the separation of substances based on size, not the specific medical procedure performed by an artificial kidney.

Option (4): None of these — Incorrect, as haemodialysis is a valid and well-known medical procedure.

Step 3: Final Answer.

(2) Haemodialysis

Quick Tip

Haemodialysis is the specific medical procedure performed using an artificial kidney to remove waste products and excess fluids from the blood. It is a critical treatment for patients with kidney failure.

134. What is the energy currency of the cell?

- (1) Fat
- (2) Protein
- (3) ADP
- (4) ATP

Correct Answer: (4) ATP

Solution:

Step 1: Understand Cellular Energy Currency. The primary energy currency of cells is adenosine triphosphate (ATP). ATP is a high-energy molecule that stores and releases energy in cells through its chemical bonds. Cells use ATP to power various cellular processes, such as muscle contraction, active transport, and biosynthesis.

Step 2: Analyze Each Option.

Option (1): Fat — Incorrect, as fats are stored energy sources but not the primary energy currency of cells.

Option (2): Protein — Incorrect, as proteins are essential macromolecules involved in structure and function but not the direct energy currency.

Option (3): ADP — Incorrect, as ADP (adenosine diphosphate) is a product of ATP hydrolysis and does not serve as the primary energy currency.

Option (4): ATP — Correct, as ATP is the universal energy currency of cells.

Step 3: Final Answer.

(4) ATP

Quick Tip

ATP (adenosine triphosphate) is the primary energy currency of cells because it can store and release energy efficiently through its phosphate bonds. This makes ATP crucial for powering cellular activities.

135. The change of radiant energy into chemical energy is known as :

- (1) Photosynthesis
- (2) Chemical Synthesis
- (3) Respiration
- (4) Transpiration

Correct Answer: (1) Photosynthesis

Solution:

Step 1: Understand the process of energy conversion in biological systems.

Living organisms require energy, and this energy often originates from external sources. The question asks about the conversion of radiant energy (light energy) into chemical energy.

Step 2: Define the given options.

- **(1) Photosynthesis:** This is the process used by green plants, algae, and some bacteria to convert light energy into chemical energy, in the form of glucose and other organic compounds. This process uses carbon dioxide and water.
- **(2) Chemical Synthesis (or Chemosynthesis):** This is the biological conversion of one or more carbon molecules (usually carbon dioxide or methane) and nutrients into organic matter using the oxidation of inorganic molecules (e.g., hydrogen gas, hydrogen sulfide) or methane as a source of energy, rather than sunlight. It does not involve radiant energy.

- **(3) Respiration:** This is the process where organisms break down glucose and other food molecules to release chemical energy (ATP) for cellular activities. It involves the conversion of chemical energy (stored in food) into other forms of chemical energy (ATP), often with the release of heat, but it does not convert radiant energy into chemical energy.
- **(4) Transpiration:** This is the process of water movement through a plant and its evaporation from aerial parts, such as leaves, stems, and flowers. It is a physical process related to water transport, not energy conversion.

Step 3: Relate the given description to the definitions.

The description "The change of radiant energy into chemical energy" directly corresponds to the definition of photosynthesis.

Step 4: Conclude the correct term.

Photosynthesis is the process by which radiant energy is converted into chemical energy.

(1) Photosynthesis

Quick Tip

Photosynthesis is the cornerstone of most ecosystems, converting light energy into usable chemical energy for life on Earth.

ENGLISH

136. Choose an antonym (opposite in meaning) for 'short':

- (1) small
- (2) less
- (3) long
- (4) tall

Correct Answer: (3) long

Solution:

Step 1: Understand the meaning of 'antonym'.

An antonym is a word that means the opposite of another word.

Step 2: Understand the meaning of 'short'.

'Short' can refer to a small length, distance, or duration. It can also refer to a small height (e.g., a short person).

Step 3: Evaluate each option as a potential antonym for 'short'.

- **(1) small:** While 'small' can sometimes be related to 'short' (e.g., a small object can be short in dimension), it is a synonym in certain contexts, not a direct antonym for all meanings of short. 'Small' refers to overall size, while 'short' often refers to a specific dimension like length or height.
- **(2) less:** 'Less' is a comparative adjective or adverb meaning a smaller amount or degree. It is not an antonym for 'short' in terms of length or height.
- **(3) long:** 'Long' is a direct antonym for 'short' when referring to length or duration (e.g., a long rope vs. a short rope, a long journey vs. a short journey).
- **(4) tall:** 'Tall' is a direct antonym for 'short' when referring specifically to height (e.g., a tall person vs. a short person). However, 'long' is a more general antonym covering both length and duration, and is often the primary antonym for 'short' in many contexts.

Step 4: Select the best antonym.

Considering the common usage of 'short' in terms of length and duration, 'long' is the most comprehensive and direct antonym. While 'tall' is an antonym for 'short' when referring to height, 'long' is a more universally applicable opposite.

(3) long

Quick Tip

When choosing an antonym, consider the primary or most common meaning of the word. 'Long' is the most direct and broadly applicable opposite for 'short'.

137. Choose the correct form of verb :

Her hair crisp and black.

- (1) are
- (2) were

(3) is

(4) am

Correct Answer: (3) is

Solution: Step 1: Identify the subject of the sentence.

The subject of the sentence is "Her hair".

Step 2: Determine the grammatical number of the subject.

In English, the word "hair" is generally treated as an uncountable noun and takes a singular verb, even when referring to multiple strands of hair. For example, "Her hair is long," not "Her hair are long."

Step 3: Choose the verb form that agrees with the singular subject.

- (1) are: Plural form of "to be". Incorrect.
- (2) were: Plural past tense form of "to be". Incorrect.
- (3) is: Singular present tense form of "to be". Correct.
- (4) am: First person singular form of "to be". Incorrect.

Step 4: Complete the sentence with the correct verb. The correct sentence is: "Her hair is crisp and black."

(3) is

Quick Tip

Remember that "hair" as a collective noun, referring to the hair on a person's head, is typically treated as uncountable and takes a singular verb. If referring to individual strands, then it can be countable (e.g., "There are two hairs on my shirt").

138. Choose the correct word to fill the blank :

..... is good for health.

- (1) Walking
- (2) Writing
- (3) Waiting

(4) Reading

Correct Answer: (1) Walking

Solution: Step 1: Analyze the sentence structure and context.

The sentence requires a subject that is an activity which can be described as "good for health." The options provided are gerunds (verb + -ing acting as a noun).

Step 2: Evaluate each option in the context of "good for health."

- **(1) Walking:** Walking is a form of physical exercise and is widely known to have numerous health benefits, such as improving cardiovascular health, strengthening muscles, and helping with weight management. Therefore, "Walking is good for health" makes logical sense.
- **(2) Writing:** While writing can be mentally beneficial and a form of expression, it is not typically categorized as an activity that is universally "good for health" in the same physical sense as exercise.
- **(3) Waiting:** Waiting is a passive state and does not inherently contribute to physical or mental health benefits.
- **(4) Reading:** Reading is an excellent mental activity that can improve cognitive function and reduce stress, but it's not typically described as "good for health" in the broad, common understanding that implies physical well-being.

Step 3: Choose the option that best fits the blank.

Among the given choices, "Walking" is the most appropriate word that describes an activity universally considered "good for health."

(1) Walking

Quick Tip

When filling in blanks, consider the common associations and benefits of the activities described by the words. In general health contexts, physical activities like walking are directly linked to being "good for health."

139. Choose the correct option:

Mohan _____ this book yesterday.

- (1) buy
- (2) bought
- (3) will buy
- (4) buying

Correct Answer: (2) bought

Solution:

Step 1: Understand the Context.

The sentence states that Mohan performed an action "yesterday," which indicates a past event. Therefore, the verb must be in the past tense to correctly describe the action that occurred in the past.

Step 2: Analyze Each Option.

Option (1): buy — Incorrect, as "buy" is the base form of the verb and does not indicate past tense.

Option (2): bought — Correct, as "bought" is the past tense of "buy," which matches the context of the sentence.

Option (3): will buy — Incorrect, as "will buy" indicates future tense, not past tense.

Option (4): buying — Incorrect, as "buying" is the present participle form and does not indicate past tense.

Step 3: Final Answer.

(2) bought

Quick Tip

When describing actions that occurred in the past, use the past tense of the verb. In this case, "bought" is the correct choice because it reflects the past action of Mohan purchasing the book yesterday.

140. Find the one word that can substitute the following:

"The act of afforestation by planting many trees."

- (1) Deforestation
- (2) Afforestation
- (3) Forest
- (4) Defrost

Correct Answer: (2) Afforestation

Solution:

Step 1: Understand the Definition. The phrase "The act of afforestation by planting many trees" refers to the process of planting trees to create or expand forests. The term that best describes this activity is afforestation.

Step 2: Analyze Each Option.

Option (1): Deforestation — Incorrect, as deforestation refers to the removal of forests, which is the opposite of planting trees.

Option (2): Afforestation — Correct, as afforestation specifically means planting trees to create or expand forests.

Option (3): Forest — Incorrect, as "forest" is a noun referring to a large area covered with trees, not the act of planting them.

Option (4): Defrost — Incorrect, as defrosting refers to removing frost or ice, which is unrelated to planting trees.

Step 3: Final Answer.

(2) Afforestation

Quick Tip

Afforestation is the process of planting trees to create or expand forests. It is the correct term to describe the act of planting many trees to increase forest cover.

141. Find the correct option for the following jumbled words :

indoor/and/there/are/outdoor/kind of/various/games

- (1) There are various kind of indoor and outdoor games.
- (2) There are indoor and outdoor kind of various games.
- (3) Various kind of indoor and outdoor games are there.

(4) Indoor and outdoor kind of various games are there.

Correct Answer: (1) There are various kind of indoor and outdoor games.

Solution:

Step 1: Analyze the jumbled words and their potential grammatical roles.

The words provided are: "indoor", "and", "there", "are", "outdoor", "kind of", "various", "games". We need to form a grammatically correct and coherent sentence.

Step 2: Consider common sentence structures (Subject-Verb-Object/Complement).

A typical English sentence starts with a subject, followed by a verb. "There are" is a common introductory phrase indicating existence.

Step 3: Evaluate each option for grammatical correctness and logical flow.

- **(1) There are various kind of indoor and outdoor games.:** "There are" - correct opening. "various kind of" - indicates a type. "Kind of" should ideally be followed by "kinds of" if "various" is used, but "kind of" is often colloquially accepted with plural nouns, especially when referring to a category. However, in formal grammar, it would be "various kinds of". Let's keep evaluating. "indoor and outdoor games" - clearly describes the games. This sentence structure is mostly logical and grammatically acceptable in informal contexts.
- **(2) There are indoor and outdoor kind of various games.:** "There are" - correct opening. "indoor and outdoor kind of various games" - the order of "kind of" and "various" is awkward. "Various kind of" makes more sense than "kind of various."
- **(3) Various kind of indoor and outdoor games are there.:** Starting with "Various kind of indoor and outdoor games" followed by "are there" is grammatically acceptable, but less natural than starting with "There are". Also, "kind of" is still problematic with "various".
- **(4) Indoor and outdoor kind of various games are there.:** Starting with "Indoor and outdoor kind of various games" is awkward and less natural. The placement of "kind of various" is also less preferred.

Step 4: Choose the best option.

Option (1) "There are various kind of indoor and outdoor games" is the most natural and

grammatically sound sentence among the choices, despite the minor "kind vs kinds" nuance. It correctly conveys the meaning that different types of indoor and outdoor games exist.

(1) There are various kind of indoor and outdoor games.

Quick Tip

When unscrambling sentences, look for common sentence structures like "There is/are..." or Subject-Verb-Object. Pay attention to noun-adjective agreement and the natural flow of phrases.

142. Fill the correct choice : The of flowers.

- (1) group
- (2) collection
- (3) bunch
- (4) heap

Correct Answer: (3) bunch

Solution:

Step 1: Understand the concept of collective nouns.

A collective noun is a word used to denote a group of individuals or things. The question asks for the most appropriate collective noun for "flowers".

Step 2: Evaluate each option as a collective noun for flowers.

- **(1) group:** "Group" is a very general collective noun and can be used for almost any collection of things or people. While not incorrect, it's not the most specific or common term for flowers.
- **(2) collection:** "Collection" refers to items gathered together, often implies a deliberate gathering or an assortment. While flowers can be part of a "collection" (e.g., a collection of different flower types in a garden), it's not the standard term for a quantity of cut flowers.
- **(3) bunch:** "Bunch" is a specific and very common collective noun used for a group of things, especially flowers, grapes, or keys, that are held or tied together. "A bunch of flowers" is a widely recognized idiom.

- **(4) heap:** "Heap" refers to a disorderly pile or mass of things. This term is not appropriate for flowers, as it implies disarray rather than a neatly gathered or grown set.

Step 3: Choose the most appropriate collective noun.

"Bunch" is the most fitting and idiomatic collective noun for flowers.

(3) bunch

Quick Tip

Collective nouns are specific to the items they describe. For flowers, 'bunch' is the most commonly used and appropriate collective noun.

143. Find the correct verb for the word 'advice' :

- (1) advise
- (2) advisor
- (3) advisable
- (4) advisory

Correct Answer: (1) advise

Solution: Step 1: Understand the difference between 'advice' and its related forms.

- **Advice** (with 'c') is a noun, meaning guidance or recommendations offered with regard to prudent future action.
- We are looking for the verb form, which describes the action of giving advice.

Step 2: Evaluate each option.

- **(1) advise** (with 's'): This is the verb form of 'advice', meaning to offer suggestions about the best course of action. For example, "I advise you to study hard."
- **(2) advisor:** This is a noun, referring to a person who gives advice.
- **(3) advisable:** This is an adjective, meaning to be recommended or sensible.
- **(4) advisory:** This can be an adjective (e.g., an advisory committee) or a noun (e.g., a weather advisory), typically relating to giving advice or information. It is not the verb form of 'advice'.

Step 3: Conclude the correct verb form.

The correct verb form for the word 'advice' is 'advise'.

(1) advise

Quick Tip

Remember the 'c' vs. 's' rule for similar-sounding words: 'advice' (noun, with 'c') and 'advise' (verb, with 's'). This pattern applies to other pairs like 'practice' (noun) and 'practise' (verb in British English, though 'practice' is both in American English).

144. Find the correct option for the underline idiom :

He got fame by leaps and bounds.

- (1) slowly
- (2) silently
- (3) surprisingly
- (4) rapidly

Correct Answer: (4) rapidly

Solution: Step 1: Understand the meaning of the idiom "by leaps and bounds."

The idiom "by leaps and bounds" means to progress or increase very quickly or rapidly. It conjures an image of large, quick jumps or movements.

Step 2: Analyze the context of the sentence.

The sentence states, "He got fame by leaps and bounds," implying that his fame increased at a fast pace.

Step 3: Evaluate each option based on the idiom's meaning.

- **(1) slowly:** This is the opposite of the idiom's meaning.
- **(2) silently:** The idiom does not relate to the sound or lack thereof.
- **(3) surprisingly:** While rapid progress can be surprising, "surprisingly" is not the direct meaning of "by leaps and bounds." The primary meaning is about speed of progress.
- **(4) rapidly:** This perfectly matches the meaning of "by leaps and bounds," indicating

very fast progress or increase.

Step 4: Conclude the correct option.

The correct option that represents the meaning of "by leaps and bounds" is "rapidly."

(4) rapidly

Quick Tip

Idioms are phrases whose meaning cannot be understood from the ordinary meaning of its words. To understand them, it's best to learn their established definitions. "By leaps and bounds" consistently means "very quickly."

145. Fill in the blank with the correct preposition:

He died ----- hunger.

- (1) of
- (2) from
- (3) by
- (4) with

Correct Answer: (1) of

Solution:

Step 1: Understand the Context.

The phrase "died ----- hunger" refers to a cause of death. In English, when describing death caused by a specific condition or disease, the preposition "of" is typically used. For example: "He died of hunger" means he died because of starvation.

Step 2: Analyze Each Option.

Option (1): of — Correct, as "died of hunger" is the standard expression to indicate death caused by starvation.

Option (2): from — Incorrect, as "from" is not commonly used in this context for death caused by a condition.

Option (3): by — Incorrect, as "by" is used to indicate the agent or cause of an action but is less common in this specific construction. Option (4): with — Incorrect, as "with" does not

convey the idea of causation in this context.

Step 3: Final Answer.

(1) of

Quick Tip

When describing death caused by a condition or disease, use the preposition "of." For example, "died of hunger," "died of cancer," etc. This is the standard usage in formal and informal contexts.

146. Which is the correct passive form of the following sentence:

Pradeep writes a letter.

- (1) A letter was written by Pradeep.
- (2) A letter has been written by Pradeep.
- (3) A letter is written by Pradeep.
- (4) A letter will be written by Pradeep.

Correct Answer: (1) A letter was written by Pradeep.

Solution:

Step 1: Understand Passive Voice Formation.

To convert an active sentence into its passive form, follow these steps:

1. Identify the subject, verb, and object in the active sentence.

Active sentence: "Pradeep writes a letter."

Subject: Pradeep

Verb: writes

Object: a letter

2. In the passive voice, the object becomes the subject, and the verb changes to reflect the passive form. The structure is:

Object+be verb (in appropriate tense)+past participle of the main verb+by+agent (optional).

Step 2: Analyze Each Option.

Option (1): A letter was written by Pradeep. — Correct, as this is the simple past passive form of the sentence. It matches the original meaning and tense.

Option (2): A letter has been written by Pradeep. — Incorrect, as this uses the present perfect tense, which implies that the action has been completed recently or has relevance to the present. The original sentence does not suggest this.

Option (3): A letter is written by Pradeep. — Incorrect, as this uses the simple present tense, which does not match the original sentence's tense.

Option (4): A letter will be written by Pradeep. — Incorrect, as this uses the future tense, which does not match the original sentence's tense.

Step 3: Final Answer.

(1) A letter was written by Pradeep.

Quick Tip

To form the passive voice, identify the object of the active sentence and make it the subject of the passive sentence. Use the appropriate form of the "be" verb based on the tense of the original sentence. For example, if the active sentence is in the simple present, the passive form should also be in the simple present.

147. Fill in the blank with a suitable article :

His wife is actress.

- (1) an
- (2) a
- (3) the
- (4) am

Correct Answer: (1) an

Solution:

Step 1: Understand the use of articles in English.

Articles (a, an, the) are used before nouns to specify whether the noun is definite or indefinite.

- **'A'** is used before singular countable nouns that begin with a consonant sound.
- **'An'** is used before singular countable nouns that begin with a vowel sound.
- **'The'** is used before specific or particular nouns, whether singular or plural, countable

or uncountable.

Step 2: Identify the noun following the blank.

The noun following the blank is "actress".

Step 3: Determine the sound of the initial letter of the noun.

The word "actress" begins with the vowel sound /æ/.

Step 4: Choose the appropriate article.

Since "actress" starts with a vowel sound, the indefinite article "an" should be used.

(1) an

Quick Tip

Remember to consider the sound of the first letter of the word, not just the letter itself, when deciding between 'a' and 'an'. For example, 'an hour' (silent 'h'), but 'a horse'.

148. Choose correct form of verb :

Ansha to be a space scientist.

- (1) want
- (2) wants
- (3) wanting
- (4) become

Correct Answer: (2) wants

Solution:

Step 1: Identify the subject of the sentence.

The subject of the sentence is "Ansha".

Step 2: Determine the number and person of the subject.

"Ansha" is a singular noun, referring to a third person (he/she/it).

Step 3: Apply the rules of subject-verb agreement for the simple present tense.

In the simple present tense, for a third-person singular subject (he, she, it), the verb typically takes an "-s" or "-es" ending.

Step 4: Evaluate the given verb options.

- **(1) want:** This form is used with plural subjects (we, you, they) or the first-person

singular (I).

- **(2) wants:** This form is correctly used with a third-person singular subject like "Ansha" in the simple present tense.
- **(3) wanting:** This is a present participle and would typically be used with a form of "to be" (e.g., "Ansha is wanting"), or as an adjective/noun. It is not a standalone verb in this context.
- **(4) become:** While "become" is a verb, it doesn't fit the context of wanting to be something. "Ansha wants to become a space scientist" would be grammatically correct if "wants" were followed by "to become," but "become" alone doesn't convey the same meaning as "wants to be." The sentence structure "Ansha [...] to be" specifically calls for a verb that completes the desire or intention.

Step 5: Conclude the correct verb form.

"Wants" is the correct form of the verb for the singular third-person subject "Ansha" in the simple present tense.

(2) wants

Quick Tip

For singular third-person subjects (he, she, it, or a singular name) in the simple present tense, remember to add 's' or 'es' to the base form of the verb.

149. Fill in the blank with a suitable modal :

Soldiers obey the orders of their officers.

- (1) need
- (2) might
- (3) could
- (4) must

Correct Answer: (4) must

Solution: Step 1: Understand the meaning of modals.

Modals (or modal verbs) are auxiliary verbs that express necessity, possibility, permission,

obligation, etc. We need to choose the modal that best conveys the required sense in the sentence.

Step 2: Analyze the context of the sentence.

The sentence describes the relationship between soldiers and the orders of their officers. In a military context, obeying orders is not optional; it is a strict requirement and a duty. This implies a strong sense of obligation or compulsion.

Step 3: Evaluate each option's meaning.

- **(1) need:** "Need" implies a requirement or necessity, but it can sometimes be softer than 'must'. For example, "You need to finish your homework."
- **(2) might:** "Might" expresses possibility or a weak likelihood. For example, "It might rain tomorrow." This doesn't fit the context of military orders.
- **(3) could:** "Could" expresses possibility or ability, often in the past, or a polite suggestion. For example, "He could speak French." or "You could try calling him." This doesn't fit the context of a strict obligation.
- **(4) must:** "Must" expresses strong obligation, necessity, or certainty. In the context of military discipline, "must" conveys the absolute requirement for soldiers to obey orders.

Step 4: Choose the most suitable modal.

Given the context of soldiers and orders, the strongest sense of obligation is required. "Must" perfectly conveys this.

(4) must

Quick Tip

When choosing modals, consider the degree of obligation, possibility, or permission implied by the sentence. "Must" is used for strong obligations, commands, or deductions.

150. Choose the word similar in meaning to the word 'kind' :

- (1) rude
- (2) merciful

(3) eager

(4) cruel

Correct Answer: (2) merciful

Solution: Step 1: Define the word 'kind'.

The word 'kind' refers to having or showing a friendly, generous, and considerate nature. It implies compassion, gentleness, and benevolence towards others.

Step 2: Evaluate each option for similarity in meaning.

- **(1) rude:** This means offensively impolite or ill-mannered. This is an antonym (opposite) of 'kind'.
- **(2) merciful:** This means showing compassion or forgiveness, especially towards someone who is in one's power. This aligns well with the sense of being compassionate and benevolent, which are facets of being 'kind'.
- **(3) eager:** This means strongly wanting to do or have something. This is unrelated to the meaning of 'kind'.
- **(4) cruel:** This means willfully causing pain or suffering to others, or feeling no concern about it. This is also an antonym (opposite) of 'kind'.

Step 3: Conclude the most similar word.

Among the given options, 'merciful' is the closest in meaning to 'kind' as both convey a sense of compassion and benevolence.

(2) merciful

Quick Tip

When looking for synonyms, consider the core meaning and emotional tone of the word. 'Kind' evokes positive feelings of care and compassion, which 'merciful' also shares.