

JEE-Main-03-04-2025 (Memory Based)
[EVENING SHIFT]
Physics

Question: The ratio of intensities of two coherent is 1 : 9. The ratio of the maximum to the minimum intensities is

Options:

- (a) 9:1
- (b) 16:1
- (c) 8:1
- (d) 4:1

Answer: (d)

Question: Excess pressure inside bubble A is half of that of bubble B. Find ratio of volume of bubble A to bubble B.

Options:

- (a) 8
- (b) 4
- (c) 27
- (d) 16

Answer: (a)

Question: In a resonance tube experiment at one end, resonance is obtained at two consecutive length $l_1 = 100$ cm and $l_2 = 14$ cm. If the frequency of the sound is 400 Hz, the velocity of sound is

Options:

- (a) 320 m/s
- (b) 340 m/s
- (c) 380 m/s
- (d) 300 m/s

Answer (a)

Question: A magnetic dipole experiences a torque of $80\sqrt{3}$ Nm when placed in uniform magnetic field in such a way that dipole moment makes an angle of 60° with magnetic field. The potential energy of the dipole is

Options:

- (a) 90 J
- (b) 80 J
- (c) 70 J
- (d) 75 J

Answer: (b)

Question: Physical quantity S is given as $S = \frac{pq}{r^3\sqrt{t}}$. Find to percentage change in S if percentage change in p , q , r and t are 1, 1, 3 and 2 respectively.

Options:

- (a) 7%
- (b) 9%
- (c) 5%
- (d) 12%

Answer: (d)

Question: In a medium of refractive index 2, the frequency of light is 5×10^{14} Hz, the wavelength of the light is

Options:

- (a) 200 nm
- (b) 300 nm
- (c) 500 nm
- (d) 600 nm

Answer: (b)

Question: A capacitor $C_1 = 100$ pF is connected to a 60 V cell then disconnected. C_1 is now connected to an uncharged capacitor C_2 such that the final potential across C_1 becomes 20 V. Find C_2 .

Options:

- (a) 200 pF
- (b) 300 nF
- (c) 500 nF
- (d) 600 nF

Answer: (a)

Question: A block of mass 1 kg, moving along x axis with speed $v_i = 10$ m/s enters a rough region ranging from $x = 0.1$ m to $x = 1.9$ m. The retarding force acting on the block in this range is $F_r = -kx$ N, with $k = 1$ N/m. Then the final speed of the block as it crosses rough region is

Options:

- (a) 1 m/s
- (b) 2 m/s
- (c) 8 m/s
- (d) 10 m/s

Answer: (c)

Question: A bulb rated 100 W, 220 V connected to an ac supply of 220 V. Find peak current in the bulb.

Options:

- (a) 8 A
- (b) 0.64 A
- (c) 3.2 A
- (d) 2 A

Answer: (b)

Question: Statement-I: O^{2-} and H^+ are projected in a magnetic field perpendicular to the field with same speed. The radius of curvature of O^{2-} will be less than H^+ .

Statement-II: e^- and p^+ are projected in a magnetic field perpendicular to the field with same speed. The radius of curvature of e^- will be more the proton.

Options:

- (a) Statement-I is correct, statement-II is incorrect
- (b) Both statement-I and statement-II are correct
- (c) Both statement-I and statement-II are incorrect
- (d) Statement-I is incorrect, statement-II is correct

Answer: (c)

Question: The pressure of an ideal gas is increased by 0.4% keeping the volume constant. Find the initial temperature of the gas if there is a $1^\circ C$ rise in temperature.

Options:

- (a) 250 K
- (b) $250^\circ C$
- (c) 2500 K
- (d) $2500^\circ C$

Answer: (a)

Question: Match the List-I with the List-II.

A.	Boltzmann constant	I.	ML^2T^{-1}
B.	Coefficient of viscosity	II.	$MLT^{-3}K^{-1}$
C.	Planck's constant	III.	$ML^2T^{-2}K^{-1}$
D.	Thermal conductivity	IV.	$ML^{-1}T^{-1}$

Options:

- (a) (A - iii, B - iv, C - i, D - ii)
- (b) (A - ii, B - iv, C - i, D - iii)
- (c) (A - ii, B - i, C - iv, D - iii)
- (d) (A - iii, B - i, C - iv, D - iii)

Answer: (a)

Question: In a H^+ atom, electron makes transition from 4th excited state to a state with principal quantum number 'n' emitting photon of energy 2.86 eV. Then the value of n is _____

Options:

- (a) 3
- (b) 5
- (c) 2
- (d) 1

Answer: (c)

Question: If distance is given by $S = C_0(2 - t)^2 + c(2 - t)$. Find its acceleration.

Options:

- (a) $a = 2C_0$

- (b) $a = C_0(2 - t)$
 (c) $a = -2C_0$
 (d) $a = C_0 + C$

Answer: (a)

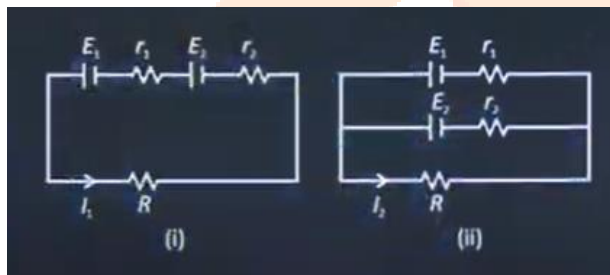
Question: For a projectile, range is 3 times the height. Given $R = \frac{nv^2}{25g}$ where v , speed of projection. Find the value of n .

Options:

- (a) 50
 (b) 34
 (c) 15
 (d) 24

Answer: (d)

Question: In two situations given in figures (i) and (ii) current through R is I_1 and I_2 respectively. If $E_1 = 2\text{ V}$, $r_1 = 1\Omega$, $E_2 = 1\text{ V}$, $r_2 = 2\Omega$, $R = 6\Omega$ then find $\frac{I_1}{I_2}$.

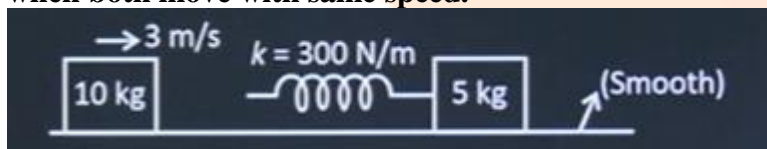


Options:

- (a) $3/4$
 (b) $4/3$
 (c) $9/4$
 (d) $4/9$

Answer: (b)

Question: A block of mass 10 kg is moving with speed 3 m/s collides with a spring connected to another block of mass 5 kg initially at rest. Find the compression in spring when both move with same speed.



Options:

- (a) 0.1 m
 (b) 0.2 m
 (c) 1 m
 (d) 2 m

Answer: (a)

Question: Two cylindrical vessels of equal cross sectional area of 2m^2 contain water upto heights 1 m and 6 m, respectively. If the vessels are connected at their bottom then the work done by the force of gravity is (Density of water is 10^3 kg/m^3 and $g = 10 \text{ m/s}^2$)

Options:

- (a) $8 \times 10^4 \text{ J}$
- (b) $8 \times 10^5 \text{ J}$
- (c) $7 \times 10^4 \text{ J}$
- (d) $7 \times 10^5 \text{ J}$

Answer: (a)

Question: Statement 1: Two charge particle having charge $-2e$ and $+e$ respectively enter in a region of uniform transverse magnetic field B with same momentum. Both particle move along a circular path with radii R_1 and R_2 respectively where $R_1 < R_2$.

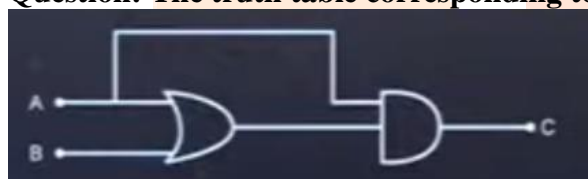
Statement 2: If a proton and an electron enter in a region of uniform transverse magnetic field B with same momentum. Both particle move along a circular path with radii R_1 and R_2 respectively where $R_p < R_e$

Options:

- (a) Both Statement I and Statement II are false
- (b) Statement I is true but Statement II are false
- (c) Both Statement I and Statement II are true
- (d) Statement I is false but Statement II is true

Answer: (b)

Question: The truth table corresponding to the circuit given below is:



Options:

(a)

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

(b)

A	B	Y
0	0	1
0	1	1
1	0	0
1	1	0

(c)

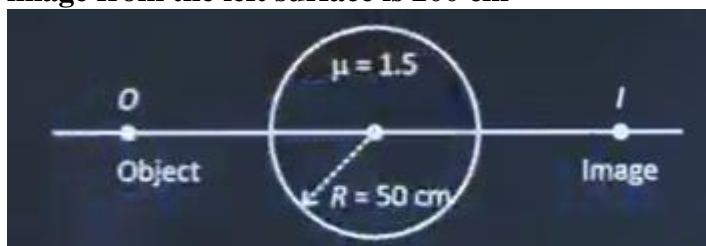
A	B	Y
0	0	0
0	1	0
1	0	1
1	1	1

(d)

A	B	Y
0	0	0
0	1	1
1	0	0
1	1	1

Answer: (c)

Question: Find the distance of the object from the left surface, if the distance of the final image from the left surface is 200 cm



Options:

- (a) 100 cm
- (b) 50 cm
- (c) 200 cm
- (d) 75 cm

Answer: (a)



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[EVENING SHIFT]

Chemistry

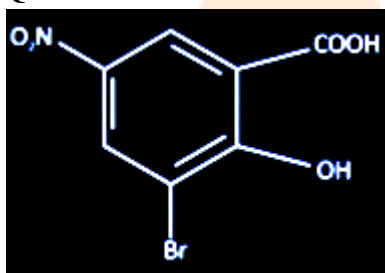
Question: Amount of magnesium (Mg) (in mg) required to liberate 224 mL of H_2 gas at STP, when reacted with HCl.

Options:

- (a) 340 mg
- (b) 450 mg
- (c) 240 mg
- (d) 100 mg

Answer: (c)

Question: The correct IUPAC Name of the given compound is:

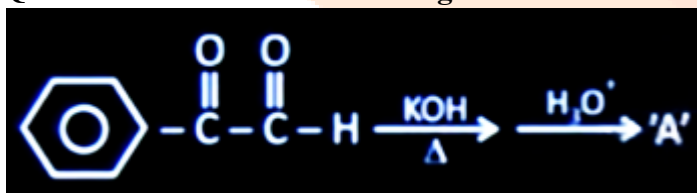


Options:

- (a) 2-Hydroxy-3-bromo-5-nitrobenzoic acid
- (b) 3-Bromo-2-Hydroxy-5-nitrobenzoic acid
- (c) 5-Bromo-6-hydroxy-3-nitrobenzoic acid
- (d) 3-Nitro-6-hydroxy-6-bromo-benzoic acid

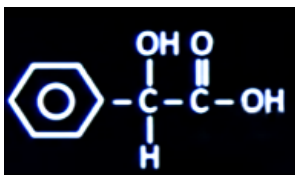
Answer: (b)

Question: Consider the following reaction.

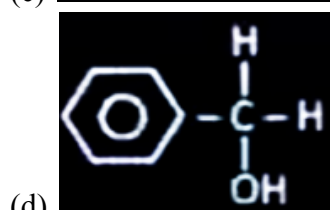
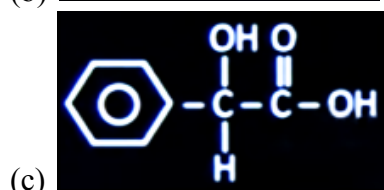
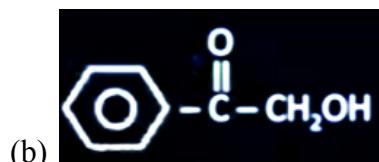


What is the product 'A'?

Options:



(a)



Answer: (a)

Question: At 715 mm pressure, 300 K, volume of $N_2(g)$ evolved was 80 mL by a 0.4 g sample of organic compound. Find % of N in organic compound Aq. tension at 300 K = 15 mm

Options:

- (a) 20.95
- (b) 25.85
- (c) 30.25
- (d) 15.83

Answer: (a)

Question: Statement-I: Wet cotton cloths made up of cellulose based carbohydrate Takes comparatively longer time to get dried than wet nylon based clothes

Statement-2: Intermolecular hydrogen bonding with water molecule is more in nylon based clothes than in cotton clothes.

Options:

- (a) Statement-I and Statement-II are correct
- (b) Statement-I and Statement-II are incorrect
- (c) Statement-I is true and Statement-II is false
- (d) Statement-I is true and Statement-II is true

Answer: (c)

Question: Statement-I: Hyper conjugation is not a permanent effect

Statement-II: In general, greater the number of Alkyl groups attached to a positively charged carbon atom greater is the Hyper conjugation interaction and stabilization of the cation.

Options:

- (a) Statement-I and Statement-II are correct
- (b) Statement-I and Statement-II are incorrect
- (c) Statement-I is true and Statement-II is false
- (d) Statement-I is true and Statement-II is true

Answer: (d)

Question: Fat soluble vitamin is

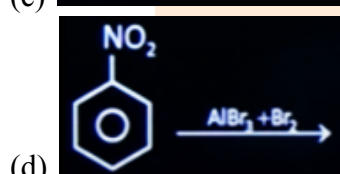
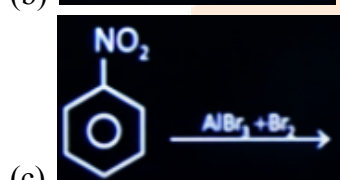
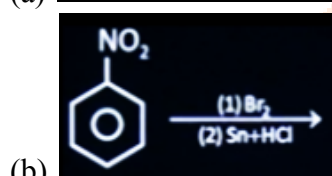
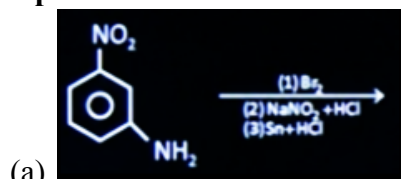
Options:

- (a) Vitamin B₁
- (b) Vitamin C
- (c) Vitamin B₁₂
- (d) Vitamin K

Answer: (d)

Question: Which of the following reagent is used to prepare tribromoaniline

Options:



Answer: (d)

Question: Match the following list-I with list-II

List-I (Groups)	List-II (Elements)
A. Pnictogens	(I) Rn
(B) Chalcogens	(II) At
(C) Halogens	(III) Te
(D) Noble gases	(IV) Bi

Options:

- (a) A-I, B-II, C-III, D-IV
- (b) A-IV, B-III, C-II, D-I
- (c) A-IV, B-II, C-III, D-I
- (d) A-I, B-III, C-II, D-IV

Answer: (b)

Question: Find orbital angular momentum for 2s and 2p energy levels

Options:

- (a) $0, \frac{h}{(\sqrt{2})\pi}$
- (b) $0, \frac{h}{\sqrt{2}\pi}$
- (c) $\frac{h}{\pi}, \frac{h}{\pi}$
- (d) $0, \frac{h}{2\pi}$

Answer: (a)

Question: Statement-I: Bohr model is applicable for hydrogen and hydrogen like species.

Statement-2: Bohr model does not consider electron-electron repulsion.

Options:

- (a) Both Statements are correct
- (b) Both Statements are incorrect
- (c) Statement-I is incorrect and statement-2 is correct
- (d) Statement-I is correct and statement-2 is incorrect

Answer: (a)

Question: Which of the following order is correct?

(A) Electronegativity : $B > Tl > In$. $Ga > Al$

(B) Ionisation energy: $B > Tl > Ga > Al > In$

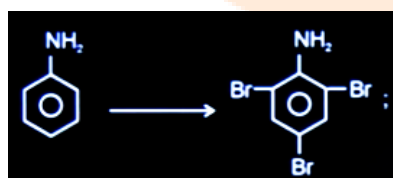
(C) Density: $Tl > In > Ga > Al > B$

(D) Size: $B > Al > Ga > In > Tl$

Options:

- (a) (A, B, C) only
- (b) (B, C, D) only
- (c) (A, B, D) only
- (d) (A, B, C, D)

Answer: (a)



Question: Reagent X in this reaction is

Options:

- (a) Br_2/CCl_4
- (b) Br_2/H_2O
- (c) HBr/H_2SO_4
- (d) $Br_2/acetone$

Answer: (b)

Question: Statement-I: CrO_3 is a strong oxidizing agent

Statement-II: Cr^{+5} is more stable than Mo^{+6} considering the above statements, choose the correct option.

Options:

- (a) Both Statement-I and Statement-II are correct
- (b) Both Statement-I and Statement-II are incorrect
- (c) Both Statement-I is correct but Statement-II is incorrect
- (d) Both Statement-I is incorrect but Statement-II is correct

Answer: (c)

Question: Which of the following compound or complex ions is/are diamagnetic in nature

- (a) CrO_3
- (b) $[\text{Fe}(\text{CN})_6]^{4-}$
- (c) $[\text{Co}(\text{H}_2\text{O})_3\text{F}_3]$
- (d) $[\text{Cr}(\text{NH}_3)_6]^{3+}$

Options:

- (a) a and b only
- (b) a, b and c only
- (c) a, b, c and d
- (d) c and d only

Answer: (b)

Question: 20 mL 1M NaOH is mixed with 10 mL 2M HCl which is further diluted to 100 mL. Find concentration for the final solution?

Options:

- (a) $2 \times 10^{-3} \text{ M}$
- (b) 0.2 M
- (c) $2 \times 10^{-2} \text{ M}$
- (d) 0.1 M

Answer: (b)

Question: Which of the following statements is correct w.r.t Arrhenius equation?

Options:

- (a) Dimension of K and A are same
- (b) K decreases with increase in temperature generally
- (c) A decreases with increase in temperature always
- (d) K increases as value of E_a increase

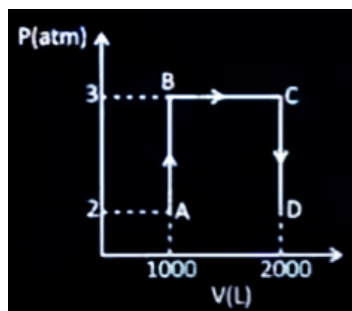
Answer: (a)

Question: Among Sc, Ti, Mn and Co, Calculate the spin only magnetic moment in +2 oxidation state of metal having highest heat of atomisation.

Options:

Answer: (3)

Question: Find out magnitude of work done in the process ABCD (in kJ) (1 atm. Lit = 101.3 J)



Options:

Answer: (304)

Question: Structural isomers of C_9H_{12} (with benzene ring)

Answer: (8)

JEE-Main-03-04-2025 (Memory Based)

[EVENING SHIFT]

Maths

Question: If $\lim_{x \rightarrow 0} \left(\frac{\tan x}{x} \right)^{\frac{1}{x^2}} = p$, then $96 \ln p$ is

Answer: (32)

$$p = \lim_{x \rightarrow 0} \left(\frac{\tan x}{x} \right)^{\frac{1}{x^2}}$$

$$p = \lim_{x \rightarrow 0} e^{\left(\frac{\tan x}{x} - 1 \right) \cdot \frac{1}{x^2}}$$

$$= \lim_{x \rightarrow 0} e^{\frac{\tan x - x}{x^3}} = \lim_{x \rightarrow 0} e^{\frac{x + \frac{x^3}{3} + \frac{2}{15}x^5 + \dots - x}{x^3}}$$

$$p = e^{\frac{1}{3}} \Rightarrow 96 \ln p = 32$$

Question: Let $A = \{-3, -2, -1, 0, 1, 2, 3\}$. A relation R is defined such that xRy if $y = \max\{x, 1\}$. Number of elements required to make it reflexive is l , number of elements required to make it symmetric is m and number of elements in the relation R is n . Then value of $l + m + n$ is equal to

Answer: (15)

$$r = \{(-3, 1), (-2, 1), (-1, 1), (0, 1), (1, 1), (2, 2), (3, 3)\}$$

$$\text{for } \ell: (-3, 3), (-2, -2), (-1, -1), (0, 0) \rightarrow 4$$

$$m = (1, 3), (1, -2), (1, -1), (1, 0) \rightarrow 4$$

$$l + m + n = 4 + 4 + 7 = 15$$

Question: Let a circle C with radius r passes through four distinct points $(0, 0)$, $(k, 3k)$, $(2, 3)$ and $(-1, 5)$, such that $k \neq 0$, then $(10k + 2r^2)$ is equal to

Options:

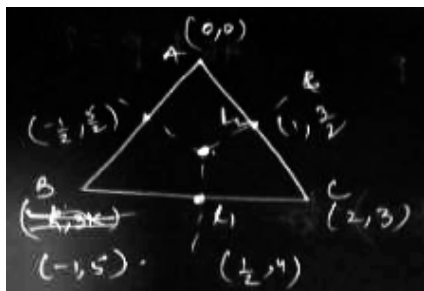
(a) 35

(b) 34

(c) 27

(d) 32

Answer: (c)



$$m_{BC} = \frac{3-5}{2+1} = \frac{-2}{3}$$

$$m_{AC} = \frac{3}{2}$$

$$m_{l_1} = \frac{3}{2}$$

$$m_{l_2} = \frac{-2}{3}$$

$$\text{equation } l_1 \Rightarrow y - 4 = \frac{3}{2} \left(x - \frac{1}{2} \right) \quad \text{equation } l_2 \Rightarrow y - \frac{3}{2} = \frac{-2}{3} (x - 1)$$

$$2y - 8 = 3x - \frac{3}{2}$$

$$3y - \frac{9}{2} = -2x + 2$$

$$2y - 3x = \frac{13}{2}$$

$$3y + 2x = \frac{13}{2}$$

$$4y - 6x = 13$$

$$6y + 4x = 13$$

$$x = -\frac{1}{2}, y = \frac{5}{2}$$

$$\text{for } r = \left(-\frac{1}{2}, \frac{5}{2} \right) \& (2, 3) \Rightarrow r = \sqrt{65}$$

$$\therefore 2r^2 = 13$$

for k; equation of circle

$$\left(x + \frac{1}{2} \right)^2 + \left(3k - \frac{5}{2} \right)^2 = \frac{13}{2}$$

$(k, 3k)$ should satisfy

$$\left(k + \frac{1}{2} \right)^2 + \left(3k - \frac{5}{2} \right)^2 = \frac{13}{2}$$

$$k^2 + \frac{1}{4} + k + 9k^2 + \frac{25}{4} - 15k = \frac{13}{2}$$

$$10k^2 - 14k + \frac{25}{4} = \frac{13}{2}$$

$$\therefore 10k = 14$$

$$10k + 24^2$$

$$= 14 + 13$$

$$= 27$$

Question: $\ell = \int_0^\pi \frac{8x}{4 \cos^2 x + \sin^2 x} dx$ equals to

Options:

(a) π^2

(b) $4\pi^2$

(c) $2\pi^2$

(d) $\frac{3}{2} \pi^2$

Answer: (c)

$$I = \int_0^{\pi} \frac{8x}{4\cos^2 x + \sin^2 x} dx \dots \dots \dots (1)$$

$$I = \int_0^{\pi} \frac{8(\pi - x)}{4\cos^2 x + \sin^2 x} dx \dots \dots \dots (2)$$

$$2I = \int_0^{\pi} \frac{8\pi}{4\cos^2 x + \sin^2 x} dx$$

$$I = 8\pi \int_0^{\frac{\pi}{2}} \frac{\sec^2 x dx}{\tan^2 x + 4} = 8\pi \int_0^{\infty} \frac{dt}{t^2 + 2^2}$$

$$= 8\pi \cdot \frac{1}{2} \left(\tan^{-1} \frac{t}{2} \right) \Big|_0^{\infty} = 4\pi \left(\frac{\pi}{2} - 0 \right) = 2\pi^2$$

Question: $S = 1 + \frac{1+3}{1!} + \frac{1+3+5}{2!} + \dots \infty$ The value of S is equal to

Options:

- (a) $4e-2$
- (b) $4e$
- (c) $5e$
- (d) $7e$

Answer: (c)

$$S = 1 + \frac{1+3}{1!} + \frac{1+3+5}{2!} + \dots \dots \dots$$

$$= \sum_{n=1}^8 \frac{n^2}{(n-1)!} = \sum_{n=1}^8 \frac{(n-1)(n+1) + 1}{(n-1)!}$$

$$= \sum_{n=1}^8 \frac{n+1}{(n-2)!} + \sum_{n=1}^8 \frac{1}{(n-1)!}$$

$$= \sum_{n=1}^8 \frac{n-2}{(n-2)!} + \sum_{n=1}^8 \frac{3}{(n-2)!} + e$$

$$= e + 3e + e = 5e$$

Question: Let $y = f(x)$ be the solution of the differential equation

$$\frac{dy}{dx} + 3y \tan^2 x + 3y = \sec^2 x \text{ such that } f(0) = \frac{e^3}{3} + 1, \text{ then } f\left(\frac{\pi}{4}\right)$$

Options:

- (a) $(1 + e^{-3})$
- (b) $\frac{2}{3} \left(1 + \frac{1}{e^3} \right)$
- (c) $\frac{1}{3} \left(1 - \frac{1}{e^3} \right)$
- (d) $\frac{1}{3} \left(1 + \frac{1}{e^3} \right)$

Answer: (b)

$$\frac{dy}{dx} + 3y \sec^2 x + \sec^2 x$$

$$If = e^{\int 3 \sec^2 x dx} = e^{3 \tan x}$$

$$ye^{3 \tan x} = \int e^{3 \tan x} \sec^2 x dx$$

$$ye^{3 \tan x} = \frac{3 \tan x}{3} + C$$

$$\text{At } x = 0, r = \frac{e^3}{3} + 1 \Rightarrow c = \frac{e^3}{3} + \frac{2}{3}$$

$$\text{At } x = \frac{\pi}{4}, ye^3 = \frac{e^3}{3} + \frac{e^3}{3} + \frac{2}{3} = \frac{2}{3}(e^3 + 1)$$

$$y = \frac{2}{3} \left(1 + \frac{1}{e^3} \right)$$

Question: Area bounded by $|x - y| \leq y \leq 4\sqrt{x}$ is equal to (in square units)

Options:

(a) $\frac{2048}{3}$

(b) $\frac{1024}{3}$

(c) $\frac{512}{3}$

(d) $\frac{128}{3}$

Answer: (b)

Question: If $(1 + x + x^2)^{10} = 1 + a_1 + a_2x^2 + \dots$, then $(a_1 + a_3 + a_5 + \dots + a_{19}) - 11a_2$ equals to

Answer: (55)

$$(1 + x + x^2)^{10} = (1 + a_1x + a_2x^2 + \dots + a_{20}x^{20}) \text{ then } (a_1 + a_3 + \dots + a_{19}) - 11a_2$$

$$x = 1, 3^{10} = (1 + a_1 + a_2 + a_3 + \dots + a_{20})$$

$$x = -1, 1 = 1 - a_1 + a_2 - a_3 + \dots + a_{20}$$

$$3^{10} - 1 = 2(a_1 + a_3 + \dots + a_{19})$$

$$(a_1 + a_3 + \dots + a_{19}) = \left(\frac{3^{10} - 1}{2} \right) - 11a_2$$

$$= \frac{3^{10} - 1 - 22a_2}{2}$$

$$= \frac{3^{10} - 1211}{2}$$

$$\text{Also, } 10(1 + x + x^2)^9(2x + 1) = a_1 + 2a_2x + \dots + 20a_{19}x^{19}$$

$$10a(1 + x + x^2)^8(2x + 1)^2 + 10(1 + x + x^2)^9(2) = 2a_2$$

$$90 \cdot 1 + 20 = 2a_2$$

$$a_2 = 55$$

Question: Let $A(z_1)$, $B(z_2)$ and $C(z_3)$ are the vertices of an equilateral triangle. If z_0 is the centroid of triangle ABC and $|z_1 - z_2| = 1$, then the value of $\sum_{i=1}^3 |z_i - z_0|^2$ is equal to

Options:

(a) 1

- (b) 2
- (c) 3
- (d) 9

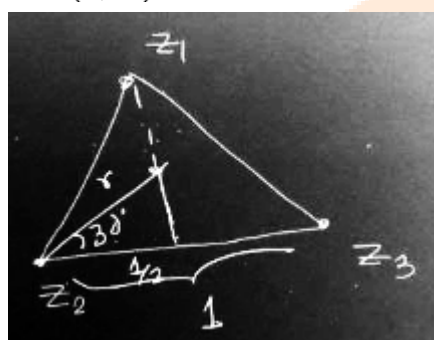
Answer: (a)

$$|z_1 - z_2| = 1$$

$$\sum_{i=1}^3 |z_i - z_0|^2$$

$$= |z_1 - z_0|^2 + |z_2 - z_0|^2 + |z_3 - z_0|^2$$

$$= \left(\frac{1}{\sqrt{3}}\right)^2 3 = 1$$



$$\cos 30^\circ = \frac{1}{2r}$$

$$\frac{\sqrt{3}}{2} = \frac{1}{2r}$$

$$r = \frac{1}{\sqrt{3}}$$

Question: If $f(x) = ||x+2| - 2|x||$, then number of points of local maxima and local minima is

Options:

- (a) 5
- (b) 3
- (c) 2
- (d) 7

Answer: (c)

$$f(x) = ||x + 2| - 2|x||$$

$$C_1 x < -1 \quad C_2 : -2 \leq x < 0 \quad C_3 x \geq 0$$

$$f(x) = -x + 2 \quad f(x) = 3x + 2 \quad f(x) = x - 2$$

$$\text{at } x = -2, \quad \text{at } x = 0 \quad \text{at } x = 2$$

$$f'(x) = -1 \quad f'(x) = 3 \quad f'(x) = -1$$

\therefore Minima at $x = 2$

maxima at $x = 0$

minima at $x = 2$

Question: $x(x - 2)(12 - k) = 2$ has both roots same. The distance of $\left(k, \frac{k}{2}\right)$ from the line $3x + 4y + 5 = 0$ is

Options:

(a) 24

(b) 14

(c) 15

(d) 20

Answer: (c)

$$x(x - 2)(12 + k) = 2 \text{ as same roots}$$

$$D = 0$$

$$(x^2 - 2x)(12 - k)$$

$$(12 - k)x^2 - 2(12 - k)x - 2 = 0$$

$$D = 0$$

$$4(12 - k)^2 + 8(12 - k) = 0$$

$$(12 - k)^2 + 2(12 - k) = 0$$

$$(12 - k)(12 - k + 2) = 0$$

$$k = 12, 14$$

$$k = 12 \text{ rejected}$$

$$k = 14$$

$$\therefore \left(k, \frac{k}{2}\right) = (14, 7)$$

$$3x + 4y + 5$$

$$d = \left| \frac{3 \times 14 + 4 \times 7 + 5}{\sqrt{3^2 + 4^2}} \right| = \left| \frac{42 + 28 + 5}{5} \right|$$

$$= \left| \frac{75}{5} \right| = 15$$

Question: The shortest distance between the parabola $y^2 = 8x$ and the circle $x^2 + y^2 + 12y + 35 = 0$ is

Options:

(a) $(2\sqrt{2} - 1)$ units

(b) $(\sqrt{2} - 1)$ units

(c) $(2\sqrt{2} + 1)$ units

(d) $(\sqrt{2} + 1)$ units

Answer: (a)

Shortest distance = Normal

$$y^2 = 8x$$

$$4a = 8$$

$$a = 2$$

$$x^2 + y^2 + 12y + 35 = 0$$

$$\text{centre}(0, -6)$$

$$y^2 = 8x$$

$$2yy' = 8$$

$$4y' = 4$$

$$y' = \frac{4}{y}$$

$$\text{stope of normal} = -\frac{y}{4} \rightarrow \frac{4t}{4} = -t$$

$$\frac{4t+6}{2+2} = -t$$

$$4t + 6 = -2t^3$$

$$2t^3 + 4t + 6 = 0$$

$$t = -1$$

$$P(2t^2, 4t)$$

$$P(2, -4)$$

$$\text{Centre } O(0, -6)$$

$$\text{radius} = 1$$

$$\text{Shortest distance} = OP - \text{radius}$$

$$= \sqrt{4 + 4} - 1$$

$$= 2\sqrt{2} - 1$$

Question 14: The no of solutions of the equation

$$(4 - \sqrt{3}) \sin x - 2\sqrt{3} \cos^2 x = \frac{-4}{1 + \sqrt{3}}, x \in \left[-2\pi, \frac{5\pi}{2}\right]$$

Answer: $([-2\pi, 5\frac{\pi}{2}])$

$$(4 - \sqrt{3}) \sin x - 2\sqrt{3} \cos^2 x = \frac{-4}{1+\sqrt{3}}$$

$$(4 - \sqrt{3})s - 2\sqrt{3}(1 - s^2) = -\frac{4(\sqrt{3}-1)}{2}$$

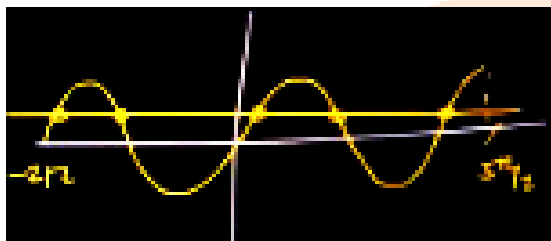
$$(4 - \sqrt{3})s - 2\sqrt{3} + 2\sqrt{3}s^2 = -2\sqrt{3} + 2$$

$$2\sqrt{3}s^2 + (4 - \sqrt{3})s - 2 = 0$$

$$\sin x = \frac{\sqrt{3}}{2\sqrt{3}} \& \frac{-4}{2\sqrt{3}}$$

$$\therefore \sin x = \frac{1}{2}$$

$$\text{from } [-2r, 5\frac{\pi}{2}]$$



Question: The distance of the point (7, 10, 11) from the line

$$\frac{x-4}{1} = \frac{y-4}{0} = \frac{z-2}{3} \text{ along the line } \frac{x-9}{2} = \frac{y-13}{3} = \frac{z-17}{6} \text{ is}$$

Answer: (PQ = 14 = d)

$$\frac{x-4}{1} = \frac{y-4}{0} = \frac{z-2}{3} = \lambda \quad L_1$$

$$\frac{\lambda+4-9}{2} = \frac{4-1}{3} = \frac{3\lambda+z-17}{6} \quad L_2$$

$$\frac{\lambda-5}{2} = -3$$

$$\lambda = -1$$

$$\therefore Q(3, 4, -1)$$

$$PQ = \sqrt{4^2 + 6^2 + 12^2}$$

$$= \sqrt{16 + 36 + 144}$$

$$PQ = 14 = d$$

