JEE Main 2025 April 2 Shift 2 Mathematics Question Paper

Time Allowed :3 Hours | Maximum Marks :300 | Total Questions :75

General Instructions

Read the following instructions very carefully and strictly follow them:

- 1. Multiple choice questions (MCQs)
- 2. Questions with numerical values as answers.
- 3. There are three sections: Mathematics, Physics, Chemistry.
- 4. **Mathematics:** 25 (20+5) 10 Questions with answers as a numerical value. Out of 10 questions, 5 questions are compulsory.
- 5. **Physics:** 25 (20+5) 10 Questions with answers as a numerical value. Out of 10 questions, 5 questions are compulsory..
- 6. **Chemistry:** 25 (20+5) 10 Questions with answers as a numerical value. Out of 10 questions, 5 questions are compulsory.
- 7. Total: 75 Questions (25 questions each).
- 8. 300 Marks (100 marks for each section).
- 9. MCQs: Four marks will be awarded for each correct answer and there will be a negative marking of one mark on each wrong answer.
- 10. Questions with numerical value answers: Candidates will be given four marks for each correct answer and there will be a negative marking of 1 mark for each wrong answer.

Mathematics

SECTION-A

- 1. If the image of the point P(1,0,3) in the line joining the points A(4,7,1) and B(3,5,3) is $Q(\alpha,\beta,\gamma)$, then $\alpha+\beta+\gamma$ is equal to:
- (1) 47/3
- (2) 46/3
- (3) 18
- (4) 13
- **2.** Let $f:[1,\infty)\to [2,\infty)$ be a differentiable function, If $\int_1^x f(t) dt = 5xf(x) x^5 9$ for all $x\geq 1$, then the value of f(3) is:
- (1) 18
- (2) 32
- (3) 22
- (4) 26

3. The number of terms of an A.P. is even; the sum of all the odd terms is 24, the sum of all the even terms is 30 and the last term exceeds the first by $\frac{21}{2}$. Then the number of terms which are integers in the A.P. is:

(1) 4

 $(2)\ 10$

(3) 6

(4) 8

4. Let $A = \{1, 2, 3, ..., 10\}$ and R be a relation on A such that $R = \{(a, b) : a = 2b + 1\}$. Let $(a_1, a_2), (a_3, a_4), (a_5, a_6), \ldots, (a_k, a_{k+1})$ be a sequence of k elements of R such that the second entry of an ordered pair is equal to the first entry of the next ordered pair. Then the largest integer k, for which such a sequence exists, is equal to:

(1) 6

(2) 7

 $(3)\ 5$

(4) 8

4. Continued. For maximum number of ordered pairs in the sequence, the second element of each ordered pair is given by:

$$\lambda - \frac{2r-2}{2^{r-2}}$$

For maximum number of ordered pairs in such sequence:

$$\lambda - \frac{2r-2}{2^{r-2}} = 1$$
 or 2 ; $1 \le \lambda \le 25$
 $\lambda = 2^{r-1}$ or $\lambda = 3 \times 2^{r-2}$

Case 1: $\lambda = 2r - 1$

$$\lambda = 2, 2^2, 2^3, 2^4$$

$$r = 2, 3, 4, 5$$

Hence, the maximum value of r is 5 when $\lambda = 16$.

Case 2: $\lambda = 3 \times 2^{r-2}$

$$\lambda = 3, 6, 12, 24$$

$$r = 2, 3, 4, 5$$

The final maximum value of r is also 5 when $\lambda = 24$.

Quick Tip

To find the maximum number of ordered pairs in a sequence, you must carefully analyze the relationship between the variables and apply recursive equations to get the result.

5. If the length of the minor axis of an ellipse is equal to one fourth of the distance between the foci, then the eccentricity of the ellipse is:

(1) $\frac{4}{\sqrt{17}}$ (2) $\frac{\sqrt{5}}{16}$ (3) $\frac{3}{\sqrt{19}}$ (4) $\frac{\sqrt{5}}{7}$

- **6.** The line L_1 is parallel to the vector $\mathbf{a} = -3\hat{i} + 2\hat{j} + 4\hat{k}$ and passes through the point (7,6,2), and the line L_2 is parallel to the vector $\mathbf{b} = 2\hat{i} + \hat{j} + 3\hat{k}$ and passes through the point (5,3,4). The shortest distance between the lines L_1 and L_2 is:
- $(1) \frac{23}{\sqrt{38}}$
- $(2) \frac{21}{\sqrt{57}}$
- (3) $\frac{23}{\sqrt{57}}$
- $(4) \frac{21}{\sqrt{38}}$
- 7. Let (a, b) be the point of intersection of the curve $x^2 = 2y$ and the straight line y = 2x 6 in the second quadrant. Then the integral

$$I = \int_{a}^{b} \frac{9x^2}{1 + 5x^3} \, dx$$

is equal to:

- (1) 24
- (2) 27
- (3) 18
- (4) 21
- 8. If the system of equation

$$2x + \lambda y + 3z = 53x + 2y - z = 74x + 5y + \mu z = 9$$

has infinitely many solutions, then $\lambda^2 + \mu^2$ is equal to:

- (1) 22
- (2) 18
- (3) 26
- (4) 30
- **9.** If $\theta \in \left[\frac{7\pi}{6}, \frac{4\pi}{3}\right]$, then the number of solutions of

$$\sqrt{3}\csc^2\theta - 2(\sqrt{3} - 1)\csc\theta - 4 = 0,$$

is equal to:

- (1) 6
- (2) 8
- $(3)\ 10$
- (4) 7
- 10. Given three identical bags each containing 10 balls, whose colours are as follows:

Bag I 3 Red 2 Blue 5 Green

Bag II 4 Red 3 Blue 3 Green

Bag III 5 Red 1 Blue 4 Green

A person chooses a bag at random and takes out a ball. If the ball is Red, the probability that it is from Bag I is p and if the ball is Green, the probability that it is from Bag III is q, then the value of $\frac{1}{p} + \frac{1}{q}$ is:

(1) 6

(2) 9

(3) 7

(4) 8

11. If the mean and the variance of 6, 4, 8, 8, b, 12, 10, 13 are 9 and 9.25 respectively, then a + b + ab is equal to:

 $(1)\ 105$

 $(2)\ 103$

(3) 100

(4) 106

12. If the domain of the function $f(x) = \frac{1}{\sqrt{10+3x-x^2}}$ is (a,b), then $(1+a)^2 + b$ is equal to:

(1) 26

(2) 29

(3) 25

(4) 30

13.

$$\int \frac{1}{\sqrt{3+x^2}+\sqrt{1+x^2}} dx - 3\log\left(\sqrt{3}\right)$$

is equal to:

(1) $2 + \sqrt{2} + \log(1 + \sqrt{2})$ (2) $2 - \sqrt{2} - \log(1 + \sqrt{2})$ (3) $2 + \sqrt{2} - \log(1 + \sqrt{2})$ (4) $2 - \sqrt{2} + \log(1 + \sqrt{2})$

14. If $\lim_{x\to 0} \frac{\cos(2x) + a\cos(4x) - b}{x^4}$ is finite, then (a+b) is equal to:

 $(1) \frac{1}{2}$

 $(2)\ 0$

 $(3) \frac{3}{4}$

(4) -1

15. If $\sum_{r=0}^{10} (10^{r+1} - 1) \binom{10}{r} = \alpha^{11} - 1$, then α is equal to :

(1) 15

(2) 11

(3) 24

(4) 20

16. The number of ways, in which the letters A, B, C, D, E can be placed in the 8 boxes of the figure below so that no row remains empty and at most one letter can be placed in a box, is:

(1) 5880

(2)960

(3)840

(4) 5760

17. Let the point P of the focal chord PQ of the parabola $y^2 = 16x$ be (1, -4). If the focus of the parabola divides the chord PQ in the ratio $m: n, \gcd(m,n) = 1$, then $m^2 + n^2$ is equal to:

- (2) 10
- (3) 37
- (4) 26

18. Let $\mathbf{a} = 2\hat{i} - 3\hat{j} + \hat{k}$, $\mathbf{b} = 3\hat{i} + 2\hat{j} + 5\hat{k}$ and a vector \mathbf{c} be such that $(\mathbf{a} - \mathbf{c}) \times \mathbf{b} = -18\hat{i} - 3\hat{j} + 12\hat{k}$ and $\mathbf{a} \cdot \mathbf{c} = 3$. If $\mathbf{b} \times \mathbf{c} = \mathbf{a}$, then $|\mathbf{a} \cdot \mathbf{c}|$ is equal to:

(1) 18

- (2) 12
- (3) 9
- (4) 15

19. Let the area of the triangle formed by a straight line L: x + by + c = 0 with co-ordinate axes be 48 square units. If the perpendicular drawn from the origin to the line L makes an angle of 45° with the positive x-axis, then the value of $b^2 + c^2$ is:

(1) 90

- (2) 93
- (3) 97
- (4) 83

20. Let A be a 3×3 real matrix such that $A^2(A-2I) - 4(A-I) = O$, where I and O are the identity and null matrices, respectively. If $A^3 = \alpha A^2 + \beta A + \gamma I$, where α , β , and γ are real constants, then $\alpha + \beta + \gamma$ is equal to:

(1) 12

- (2) 20
- (3) 76
- $(4) \ 4$

SECTION-B

21. Let y = y(x) be the solution of the differential equation

$$\frac{dy}{dx} + 2y\sec^2 x = 2\sec^2 x + 3\tan x \sec^2 x$$

such that $y(0) = \frac{5}{4}$. Then $12\left(y\left(\frac{\pi}{4}\right) - e^2\right)$ is equal to:

(1) 21

- (2) 22
- (3) 20
- (4) 25

22. If the sum of the first 10 terms of the series

$$\frac{4.1}{1+4.1^4} + \frac{4.2}{1+4.2^4} + \frac{4.3}{1+4.3^4} + \cdots$$

is $\frac{m}{n}$, where gcd(m, n) = 1, then m + n is equal to

(1) 15

- (2) 24
- (3) 41
- (4) 76

23. If $y = \cos\left(\frac{\pi}{3} + \cos^{-1}\frac{x}{2}\right)$, then $(x-y)^2 + 3y^2$ is equal to _____.

- (1) 6
- (2) 8
- $(3) \ 3$
- (4) 7

24. Let A(4, -2), B(1, 1) and C(9, -3) be the vertices of a triangle ABC. Then the maximum area of the parallelogram AFDE, formed with vertices D, E and F on the sides BC, CA and AB of the triangle ABC respectively, is _____.

- (1) 4
- (2) 6
- $(3) \ 3$
- (4) 9

25. If the set of all $a \in R \setminus \{1\}$, for which the roots of the equation $(1-a)x^2 + 2(a-3)x + 9 = 0$ are positive is $(-\infty, -\alpha] \cup [\beta, \gamma]$, then $2\alpha + \beta + \gamma$ is equal to

- (1) 7
- $(2)\ 10$
- $(3) \ 3$
- (4) 9