# JEE Main 2025 April 2 Shift 1 Mathematics Question Paper with Solutions

Time Allowed: 3 Hours | Maximum Marks: 300 | Total Questions: 75

#### General Instructions

Read the following instructions very carefully and strictly follow them:

- 1. Multiple choice questions (MCQs)
- 2. Questions with numerical values as answers.
- 3. There are three sections: Mathematics, Physics, Chemistry.
- 4. **Mathematics:** 25 (20+5) 10 Questions with answers as a numerical value. Out of 10 questions, 5 questions are compulsory.
- 5. **Physics:** 25 (20+5) 10 Questions with answers as a numerical value. Out of 10 questions, 5 questions are compulsory..
- 6. **Chemistry:** 25 (20+5) 10 Questions with answers as a numerical value. Out of 10 questions, 5 questions are compulsory.
- 7. Total: 75 Questions (25 questions each).
- 8. 300 Marks (100 marks for each section).
- 9. MCQs: Four marks will be awarded for each correct answer and there will be a negative marking of one mark on each wrong answer.
- 10. Questions with numerical value answers: Candidates will be given four marks for each correct answer and there will be a negative marking of 1 mark for each wrong answer.

#### Mathematics

#### Section - A

- **1.** The largest  $n \in N$  such that  $3^n$  divides 50! is:
- (1) 21
- (2) 22
- (3) 23
- (4) 25
- **2.** Let one focus of the hyperbola  $\frac{x^2}{a^2} \frac{y^2}{b^2} = 1$  be at  $(\sqrt{10}, 0)$ , and the corresponding directrix be  $x = \frac{\sqrt{10}}{2}$ . If e and l are the eccentricity and the latus rectum respectively, then  $9(e^2 + l)$  is equal to:
- (1) 14
- $(2)\ 16$
- (3) 18
- (4) 12

**3.** The number of sequences of ten terms, whose terms are either 0 or 1 or 2, that contain exactly five 1's and exactly three 2's, is equal to:

(1) 360

(2) 45

(3) 2520

(4) 1820

**4.** Let  $f: R \to R$  be a twice differentiable function such that

$$f''(x)\sin\left(\frac{x}{2}\right) + f'(2x - 2y) = (\cos x)\sin(y + 2x) + f(2x - 2y)$$

for all  $x, y \in R$ . If f(0) = 1, then the value of  $24f^{(4)}\left(\frac{5\pi}{3}\right)$  is:

(1) 2

(2) -3

(3) 1

 $(4) \ 3$ 

**5.** Let  $A = \begin{bmatrix} \alpha & -1 \\ 6 & \beta \end{bmatrix}$ ,  $\alpha > 0$ , such that  $\det(A) = 0$  and  $\alpha + \beta = 1$ . If I denotes the  $2 \times 2$  identity matrix, then the matrix  $(1 + A)^5$  is:

 $(1) \begin{bmatrix} 4 & -1 \\ 6 & -1 \end{bmatrix} \quad (2) \begin{bmatrix} 257 & -64 \\ 514 & -127 \end{bmatrix} \quad (3) \begin{bmatrix} 1025 & -511 \\ 2024 & -1024 \end{bmatrix} \quad (4) \begin{bmatrix} 766 & -255 \\ 1530 & -509 \end{bmatrix}$ 

**6.** The term independent of x in the expansion of

$$\left(\frac{x+1}{x^{3/2}+1-\sqrt{x}}\cdot\frac{x+1}{x-\sqrt{x}}\right)^{10}$$

for x > 1 is:

(1) 210

(2) 150

(3) 240

(4) 120

7. If  $\theta \in [-2\pi, 2\pi]$ , then the number of solutions of

$$2\sqrt{2}\cos^{2}\theta + (2 - \sqrt{6})\cos\theta - \sqrt{3} = 0$$

is:

(1) 12

(2) 6

(3) 8

 $(4)\ 10$ 

**8.** Let  $a_1, a_2, a_3, \ldots$  be in an A.P. such that

$$\sum_{k=1}^{12} 2a_{2k-1} = \frac{72}{5}, \quad \text{and} \quad \sum_{k=1}^{n} a_k = 0,$$

then n is:

(1) 11

(2) 10

(3) 18

(4) 17

9. If the function  $f(x) = 2x^3 - 9ax^2 + 12a^2x + 1$ , where a > 0, attains its local maximum and minimum at p and q, respectively, such that  $p^2 = q$ , then f(3) is equal to:

(1) 55

 $(2)\ 10$ 

(3) 23

(4) 37

**10.** Let z be a complex number such that |z| = 1. If

$$\frac{2+kz}{k+z} = kz, \ k \in R,$$

then the maximum distance of  $k + ik^2$  from the circle |z - (1 + 2i)| = 1 is:

 $(1) \sqrt{5} + 1$ 

 $(2)\ 2$ 

 $(3) \ 3$ 

 $(4) \sqrt{5} + \sqrt{1}$ 

11. If  $\vec{a}$  is a non-zero vector such that its projections on the vectors  $2\hat{i} - \hat{j} + 2\hat{k}$ ,  $\hat{i} + 2\hat{j} - 2\hat{k}$ , and  $\hat{k}$  are equal, then a unit vector along  $\vec{a}$  is:

 $(1) \ \frac{1}{\sqrt{155}} (7\hat{i} + 9\hat{j} + 5\hat{k}) \qquad (2) \ \frac{1}{\sqrt{155}} (7\hat{i} + 9\hat{j} - 5\hat{k}) \qquad (3) \ \frac{1}{\sqrt{155}} (7\hat{i} + 9\hat{j} + 5\hat{k}) \qquad (4) \ \frac{1}{\sqrt{155}} (7\hat{i} + 9\hat{j} - 5\hat{k})$ 

**12.** Let A be the set of all functions  $f: Z \to Z$  and R be a relation on A such that

$$R = \{(f,g) : f(0) = g(1) \text{ and } f(1) = g(0)\}$$

Then R is:

(1) Symmetric and transitive but not reflective transitive

(2) Symmetric but neither reflective nor

(3) Reflexive but neither symmetric nor transitive symmetric

(4) Transitive but neither reflexive nor

**13.** For  $\alpha, \beta, \gamma \in R$ , if

$$\lim_{x \to 0} \frac{x^2 \sin \alpha x + (\gamma - 1)e^{x^2} - 3}{\sin 2x - \beta x} = 3,$$

then  $\beta + \gamma - \alpha$  is equal to:

(1) 7

(2) 4

(3) 6

(4) -1

**14.** If the system of equations:

$$3x + y + \beta z = 3$$

$$2x + \alpha y + z = 2$$

$$x + 2y + z = 4$$

has infinitely many solutions, then the value of  $22\beta - 9\alpha$  is:

(1) 49

(2) 31

(3) 43

(4) 37

**15.** Let  $P_n = \alpha^n + \beta^n$ ,  $n \in \mathbb{N}$ . If  $P_{10} = 123$ ,  $P_9 = 76$ ,  $P_8 = 47$  and  $P_1 = 1$ , then the quadratic equation having roots  $\alpha$  and  $\frac{1}{\beta}$  is:

(1)  $x^2 - x + 1 = 0$  (2)  $x^2 + x - 1 = 0$  (3)  $x^2 - x - 1 = 0$  (4)  $x^2 + x + 1 = 0$ 

**16.** If S and S' are the foci of the ellipse  $\frac{x^2}{18} + \frac{y^2}{9} = 1$ , and P is a point on the ellipse, then  $\min(\vec{SP} \cdot \vec{S'P}) + \max(\vec{SP} \cdot \vec{S'P})$  is equal to:

 $(1) \ 3(1+\sqrt{2})$ 

(2)  $3(6+\sqrt{2})$ 

(3) 9

(4) 27

17. Let the vertices Q and R of the triangle PQR lie on the line  $\frac{x+3}{5} = \frac{y-1}{2} = \frac{z+4}{3}$ , QR = 5, and the coordinates of the point P be (0,2,3). If the area of the triangle PQR is  $\frac{m}{n}$ , then:

(1)  $m - 5\sqrt{21}n = 0$ 

(2)  $2m - 5\sqrt{21}n = 0$ 

(3)  $5m - 2\sqrt{21}n = 0$ 

(4)  $5m - 21\sqrt{2}n = 0$ 

18. Let ABCD be a tetrahedron such that the edges AB, AC and AD are mutually perpendicular. Let the areas of the triangles ABC, ACD, and ADB be 5, 6 and 7 square units respectively. Then the area (in square units) of the tetrahedron ABCD is equal to:

 $(1) \sqrt{30}$ 

(2) 12

(3)  $\sqrt{10}$ 

(4)  $7\sqrt{5}$ 

**19.** Let  $A \in R$  be a matrix of order 3x3 such that

$$det(A) = -4 \text{ and } A + I = \begin{bmatrix} 1 & 1 & 1 \\ 2 & 0 & 1 \\ 4 & 1 & 2 \end{bmatrix}$$

where I is the identity matrix of order 3. If  $\det((A+I) \cdot \operatorname{adj}(A+I))$  is  $2^m$ , then m is equal to:

(1) 14

(2) 31

 $(3)\ 16$ 

(4) 13

**20.** Let the focal chord PQ of the parabola  $y^2 = 4x$  make an angle of  $60^{\circ}$  with the positive x-axis, where P lies in the first quadrant. If the circle, whose one diameter is PS, S being the focus of the parabola, touches the y-axis at the point  $(0, \alpha)$ , then  $5\alpha^2$  is equal to:

(1) 15

(2) 25

(3) 30

(4) 20

## Mathematics

### **SECTION-B**

21. Let [.] denote the greatest integer function. If

$$\int_{1}^{e} \frac{1}{xe^{x}} dx = \alpha - \log 2, \text{ then } \alpha^{2} \text{ is equal to:}$$

(1) 8

(2) 9

(3) 16

(4) 10

23. If the area of the region

$$\{(x,y): |4-x^2| \le y \le x^2, y \ge 0\}$$

is  $\frac{80\sqrt{2}}{\alpha-\beta}$ ,  $\alpha,\beta\in N$ , then  $\alpha+\beta$  is equal to:

(1) 16

(2) 12

(3) 22

(4) 18

**24.** Three distinct numbers are selected randomly from the set  $\{1, 2, 3, ..., 40\}$ . If the probability that the selected numbers are in an increasing G.P. is  $\frac{m}{n}$ , where gcd(m, n) = 1, then m + n is equal to:

(1) 14

(2) 31

(3) 16

(4) 13

**25.** The absolute difference between the squares of the radii of the two circles passing through the point (-9,4) and touching the lines x + y = 3 and x - y = 3, is equal to:

(1)768

(2) 550

(3) 860

(4) 999